

Some quite obvious  
observational constraints  
on cosmological models

*Standard Cosmology at the threshold of change?*

Aristotle University of Thessaloniki

02-06 June 2023

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*c/o Argelander-Institut für Astronomie  
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# The SMOc

(Standard Model of Cosmology)



# The Standard Modell of Cosmology (SMoC)

**2 fundamental  
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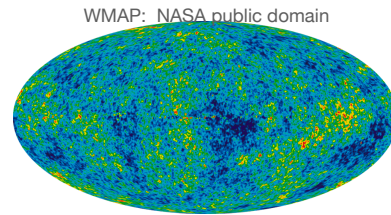
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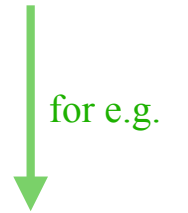
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galaxy  
rotation  
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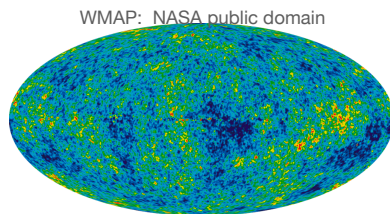
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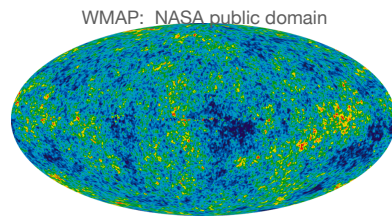
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## auxiliary assumptions

inflation  
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dark matter      **needed**  
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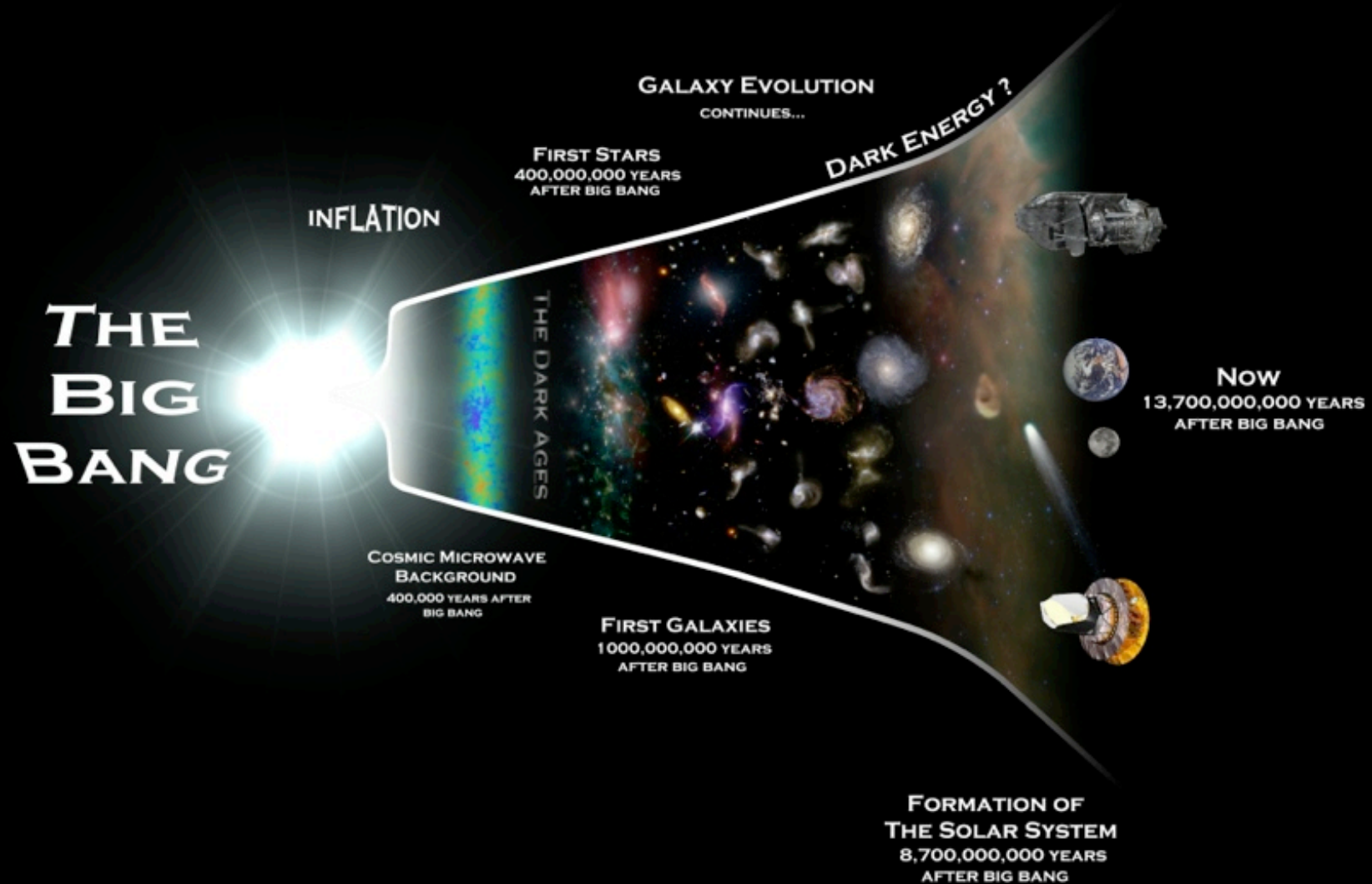


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Note: "dark matter" = cold, warm, fuzzy, axion  
(results for structure formation and properties of galaxies similar)

(eg. May & Springel 2021 arXiv)

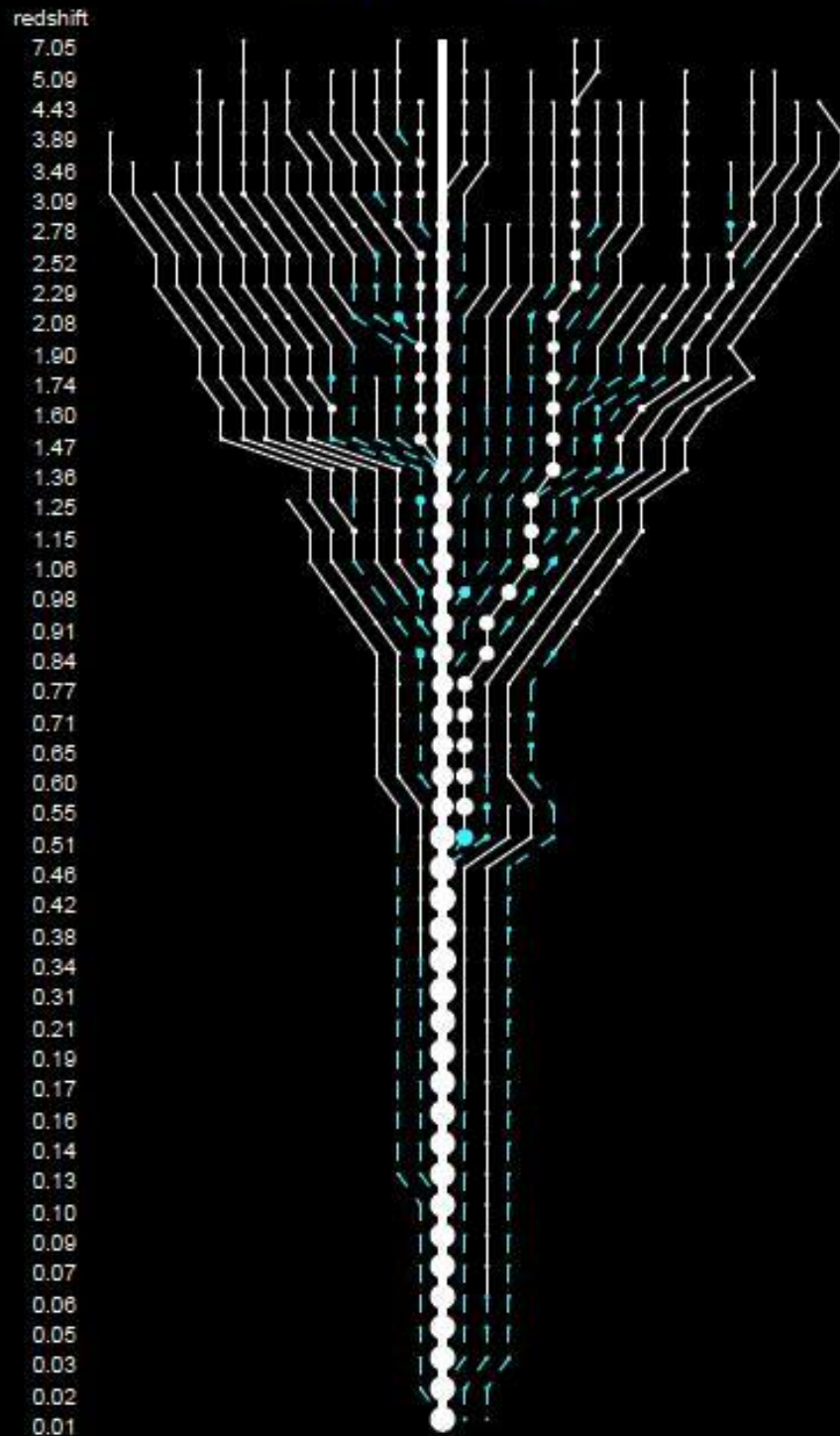


*The expanding Universe. Image credit: Rhys Taylor*

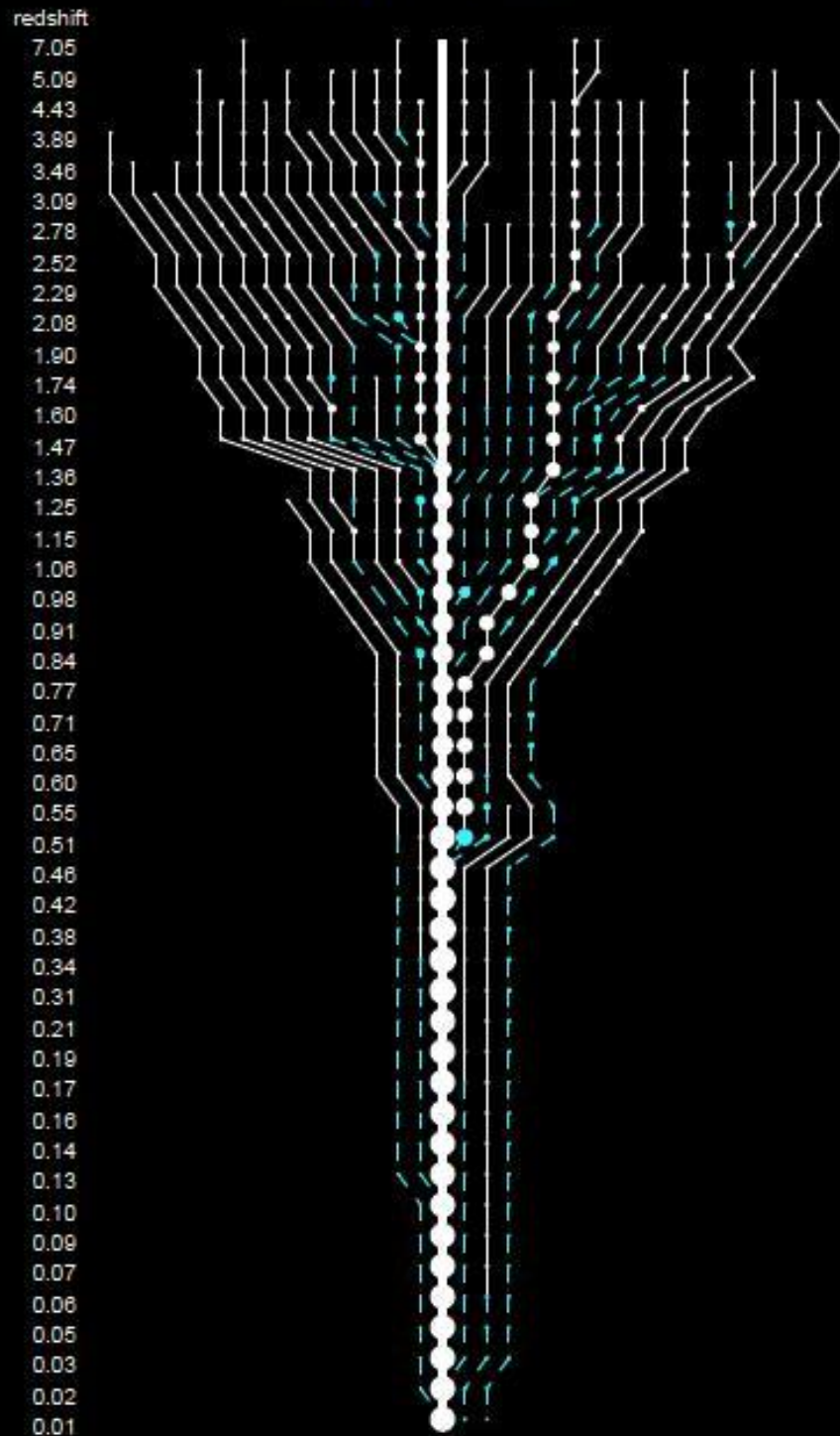
<https://blogs.cardiff.ac.uk/physicsoutreach/2019/04/02/pythagorean-astronomy-flying-space-shrapnel-and-a-misbehaving-universe/>

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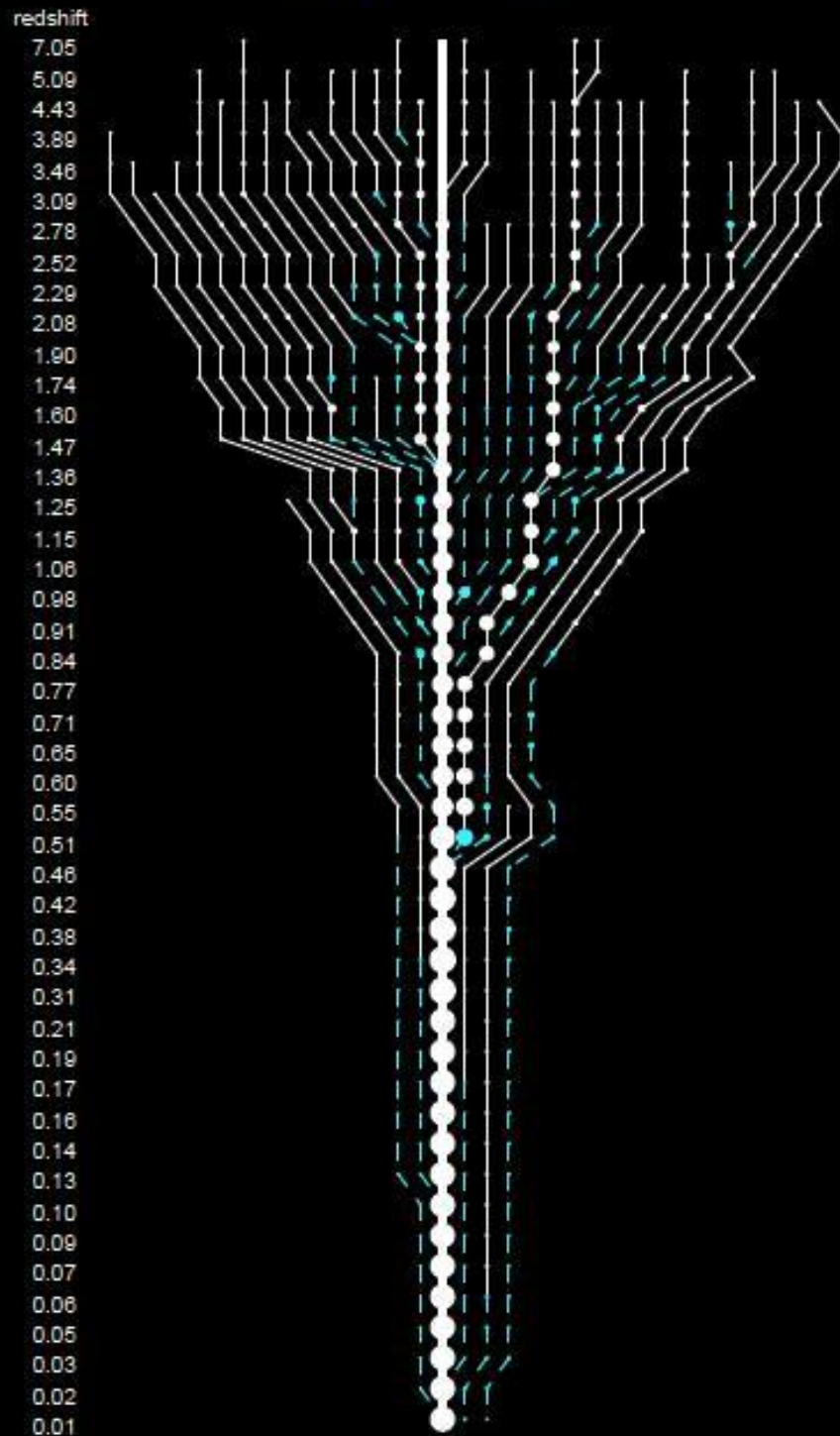


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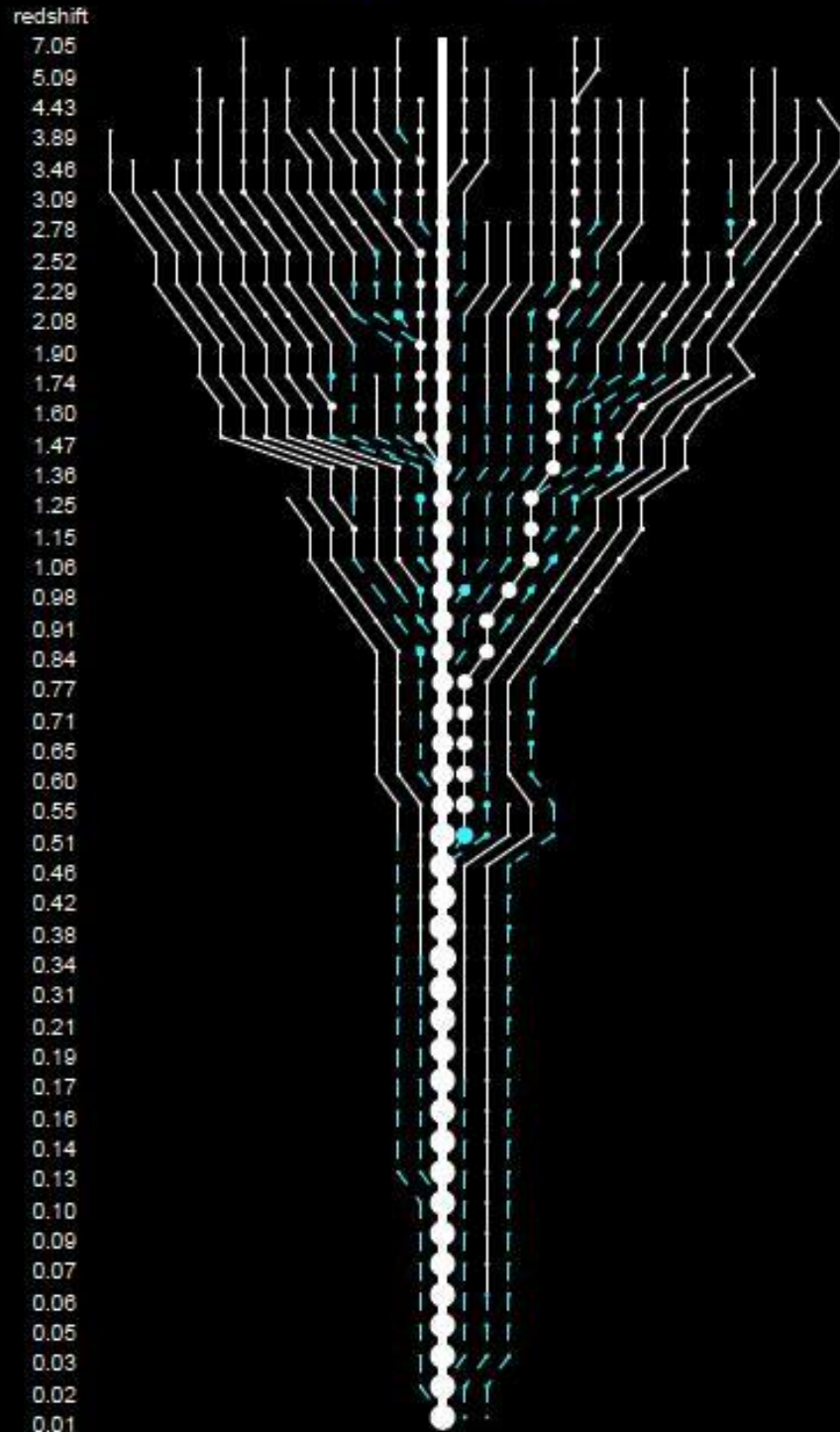
... why ?



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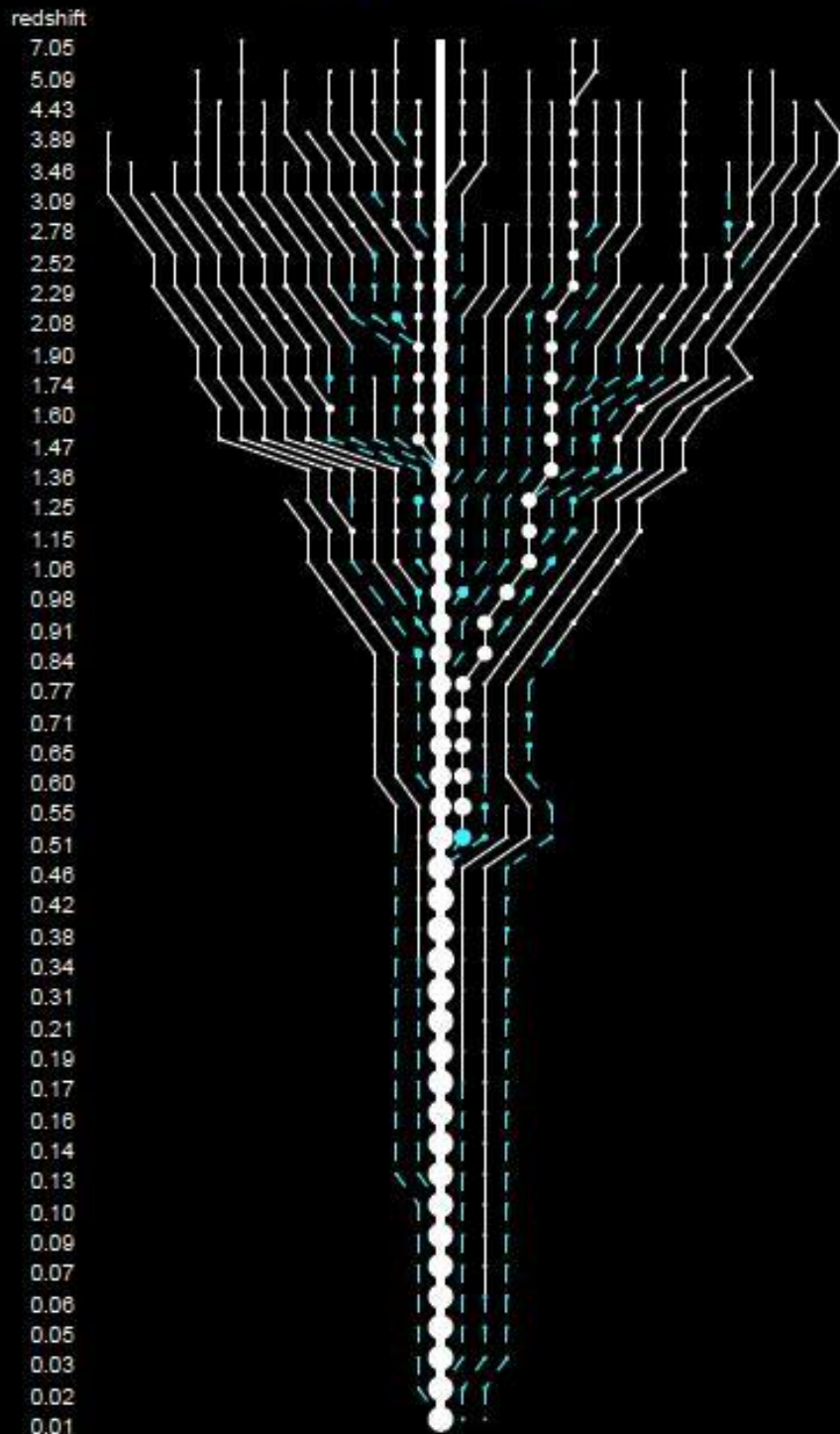


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... and why then do real elliptical galaxies form in <1Gyr and extremely early?

---> Yan, Jerabkova+21; Eappen+2022, 2024

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How can  
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- galaxies would look different (e.g. E galaxies in galaxy clusters), e.g. Gnedin & Ostriker 2001
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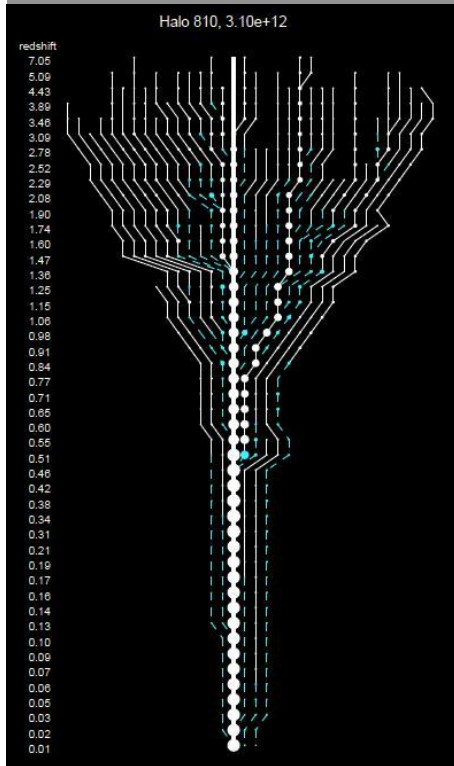


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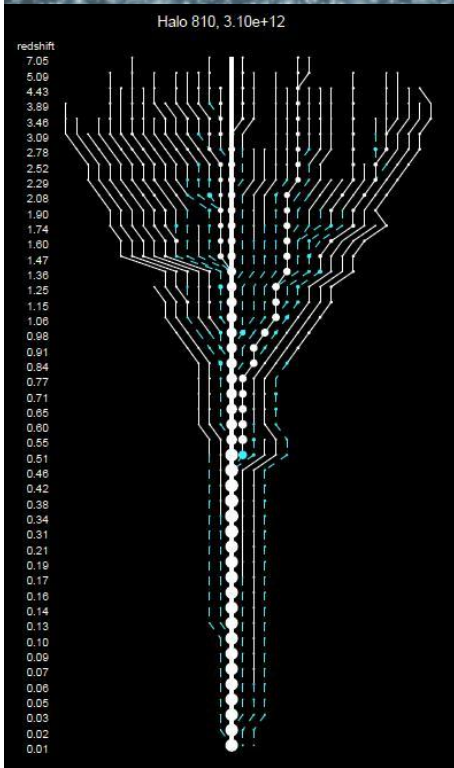
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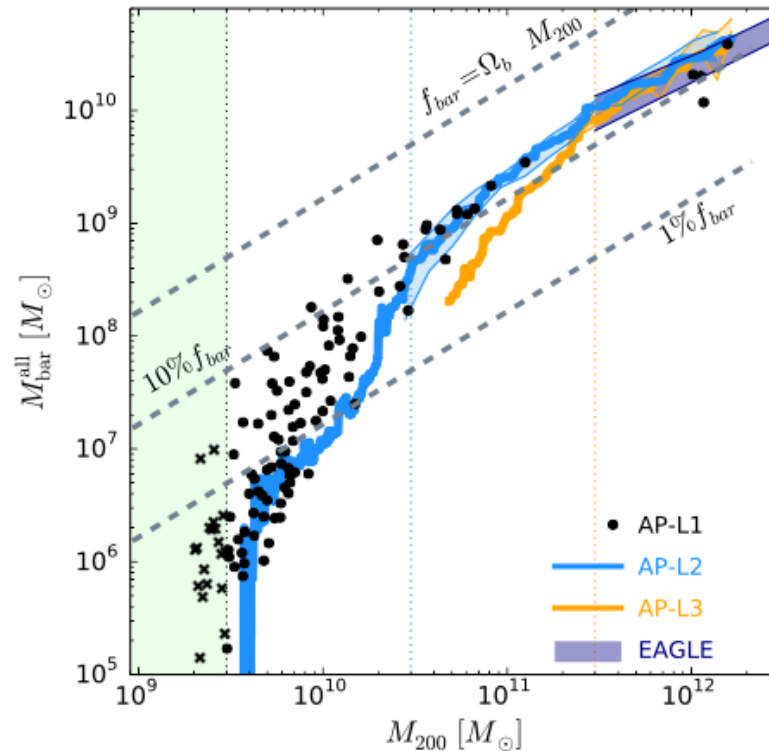
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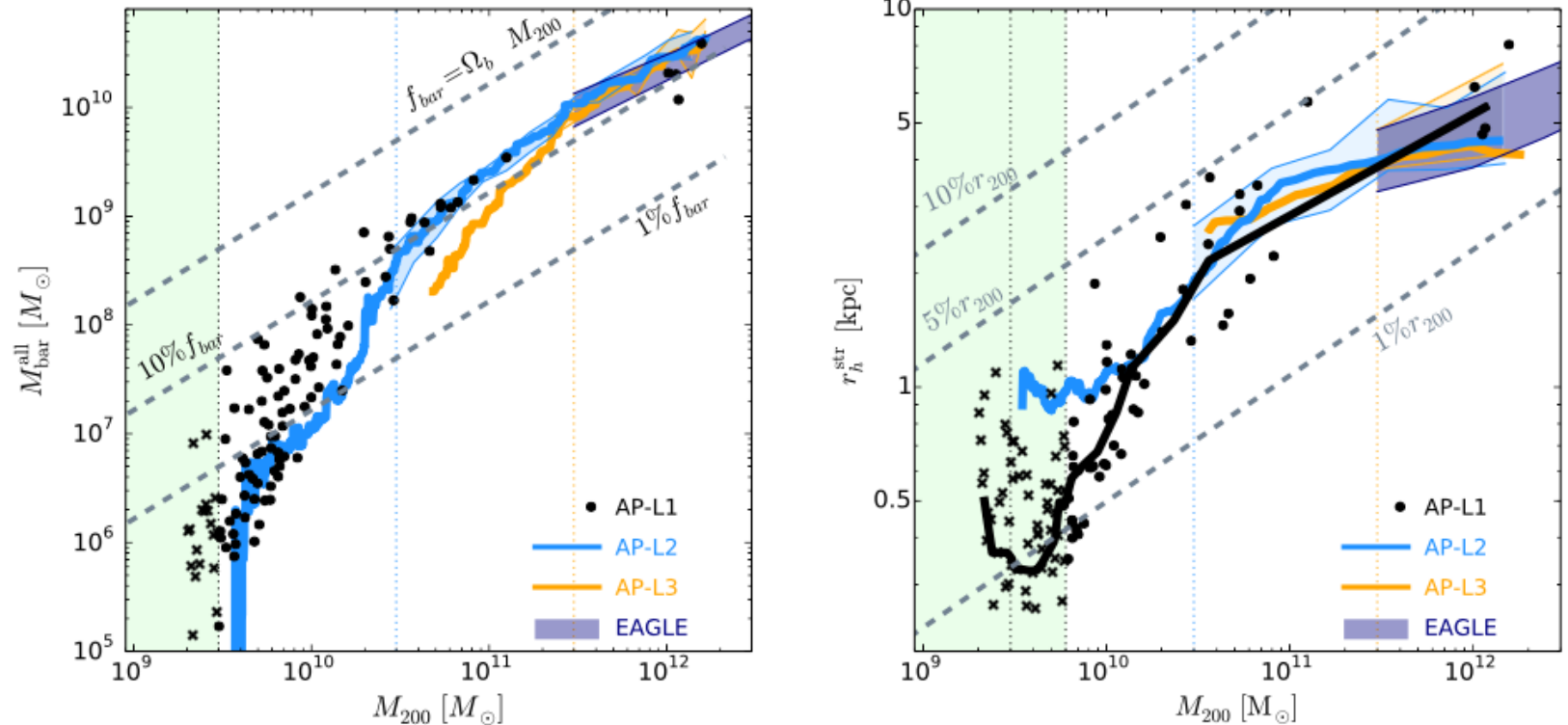


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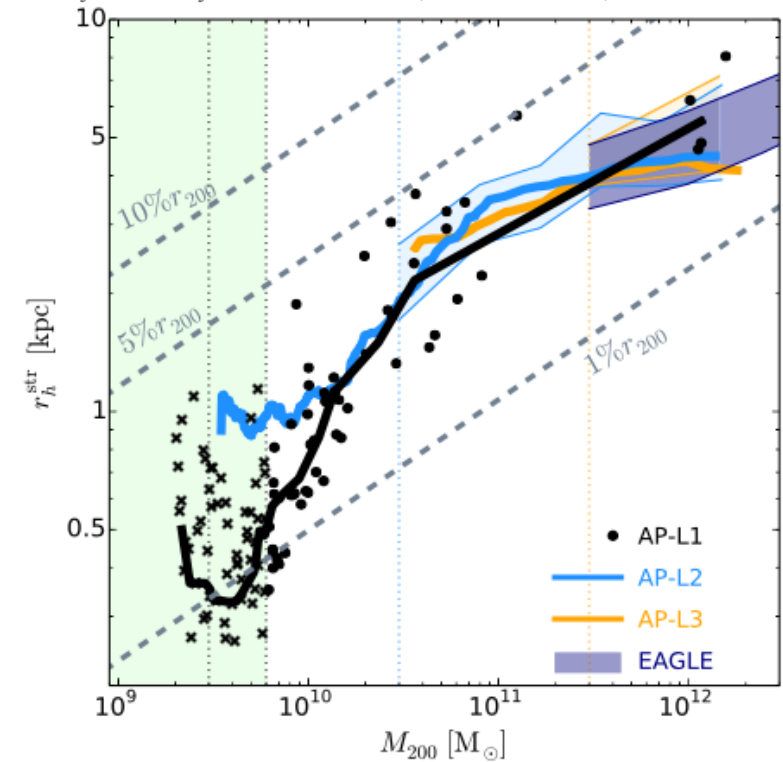
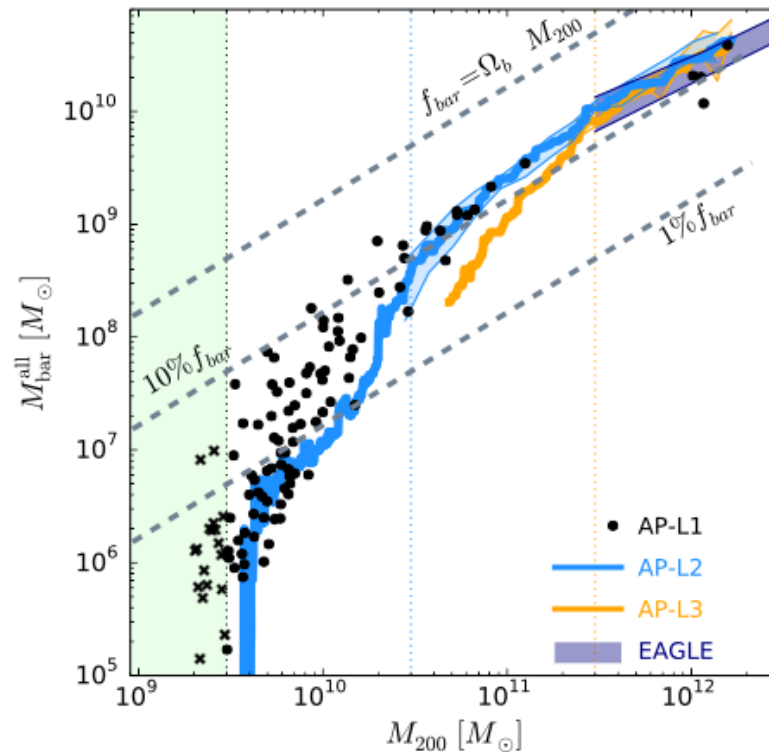


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Testing for the existence  
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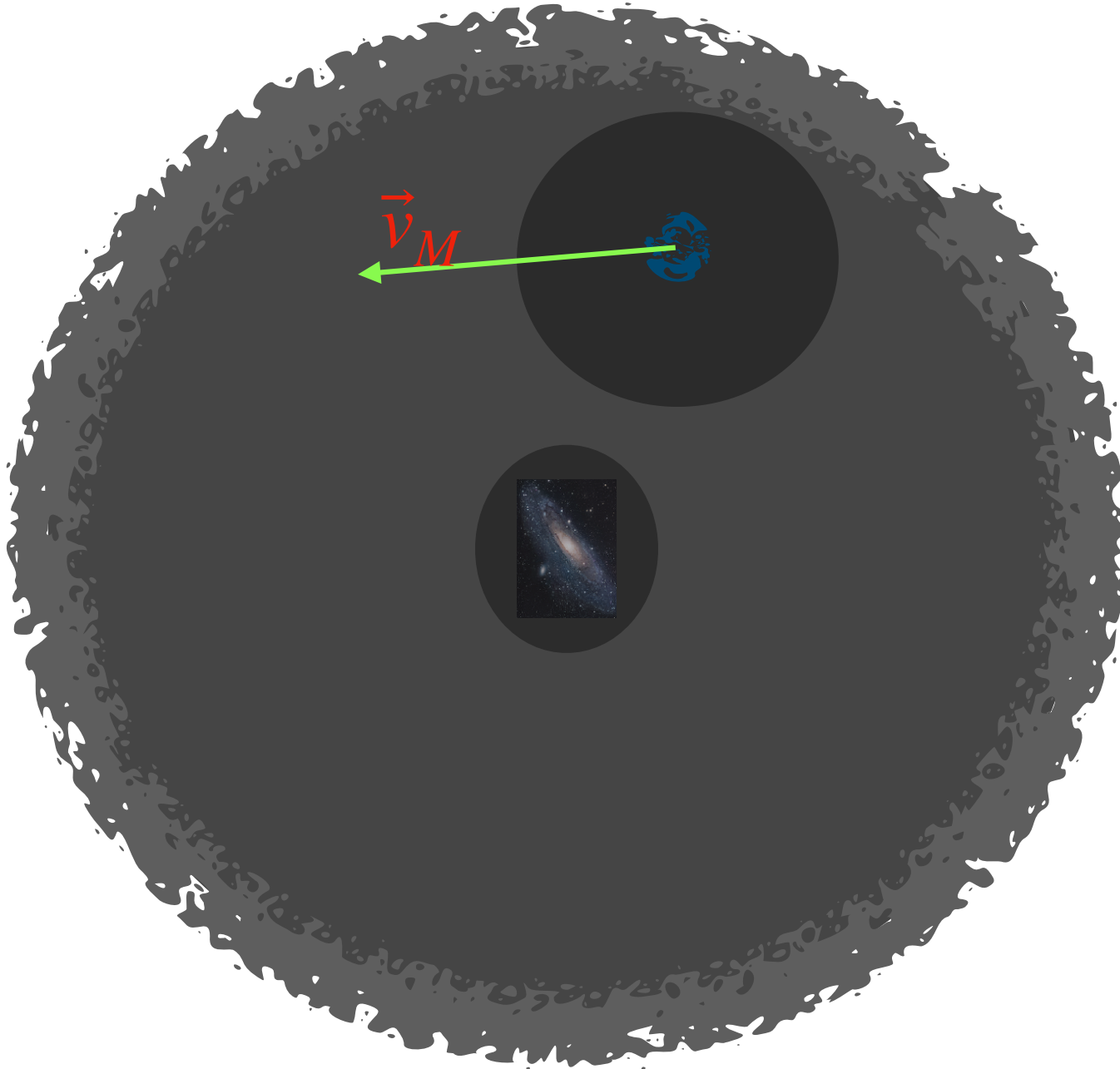
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If there is dark matter, then there must be *Chandrasekhar dynamical friction*.

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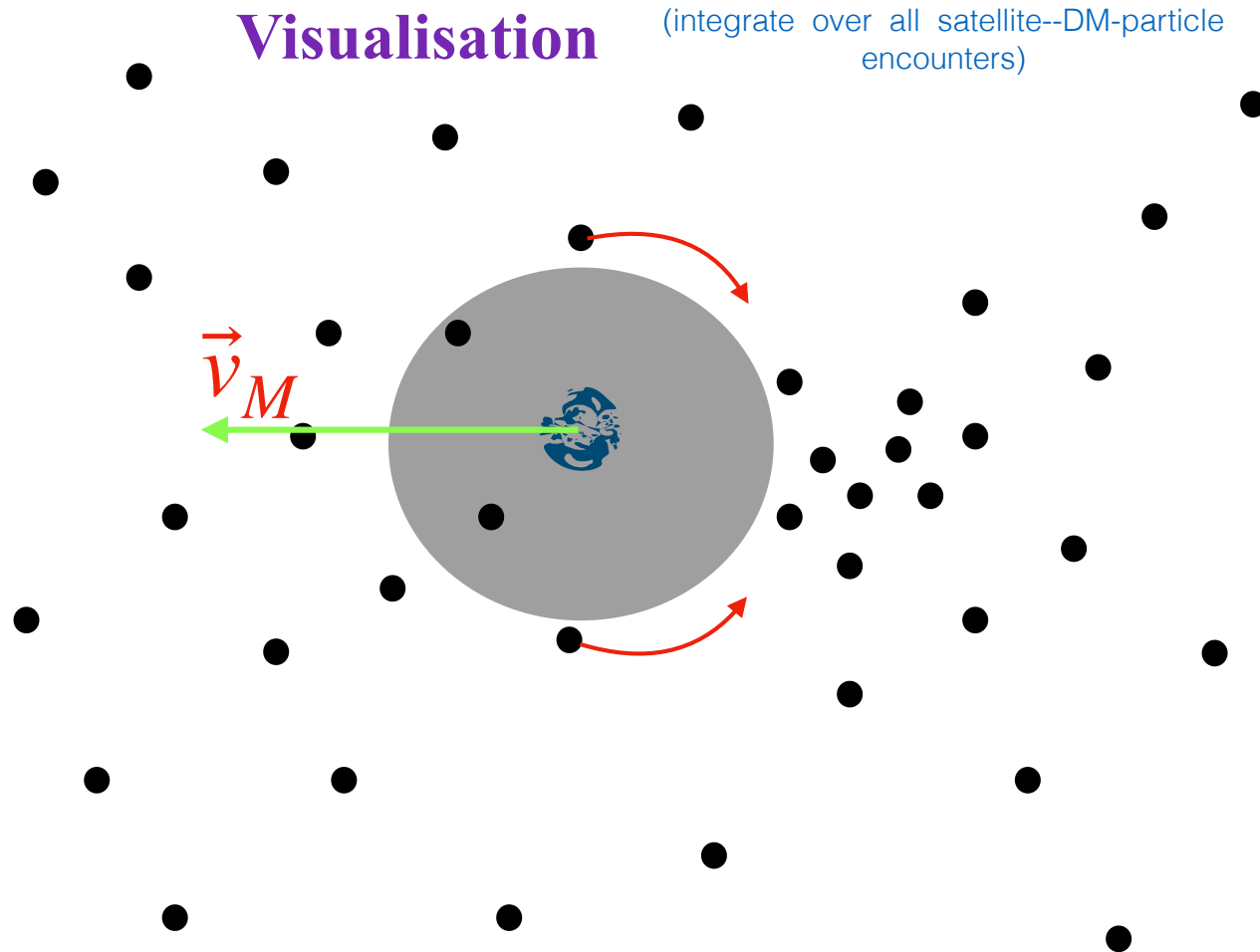
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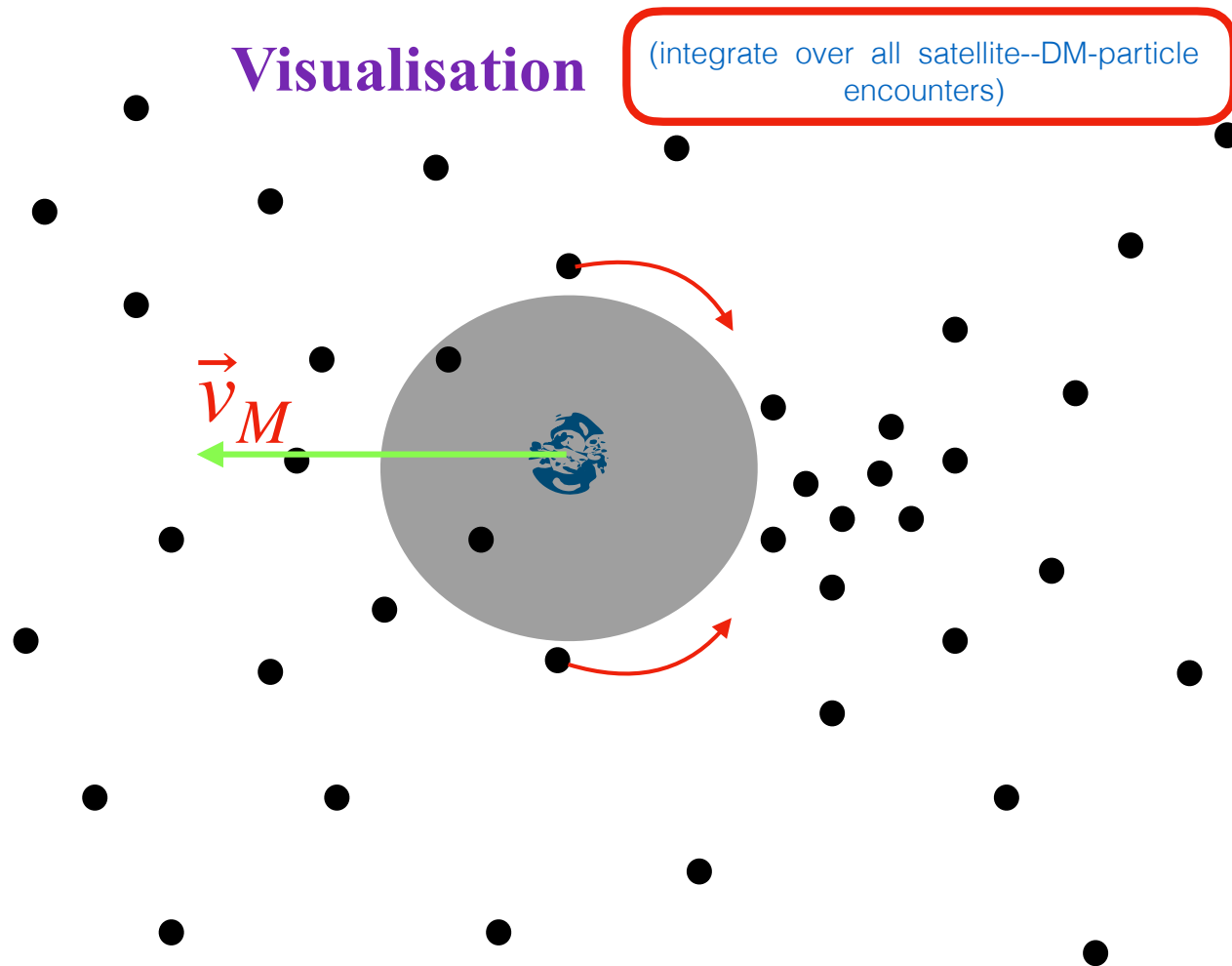
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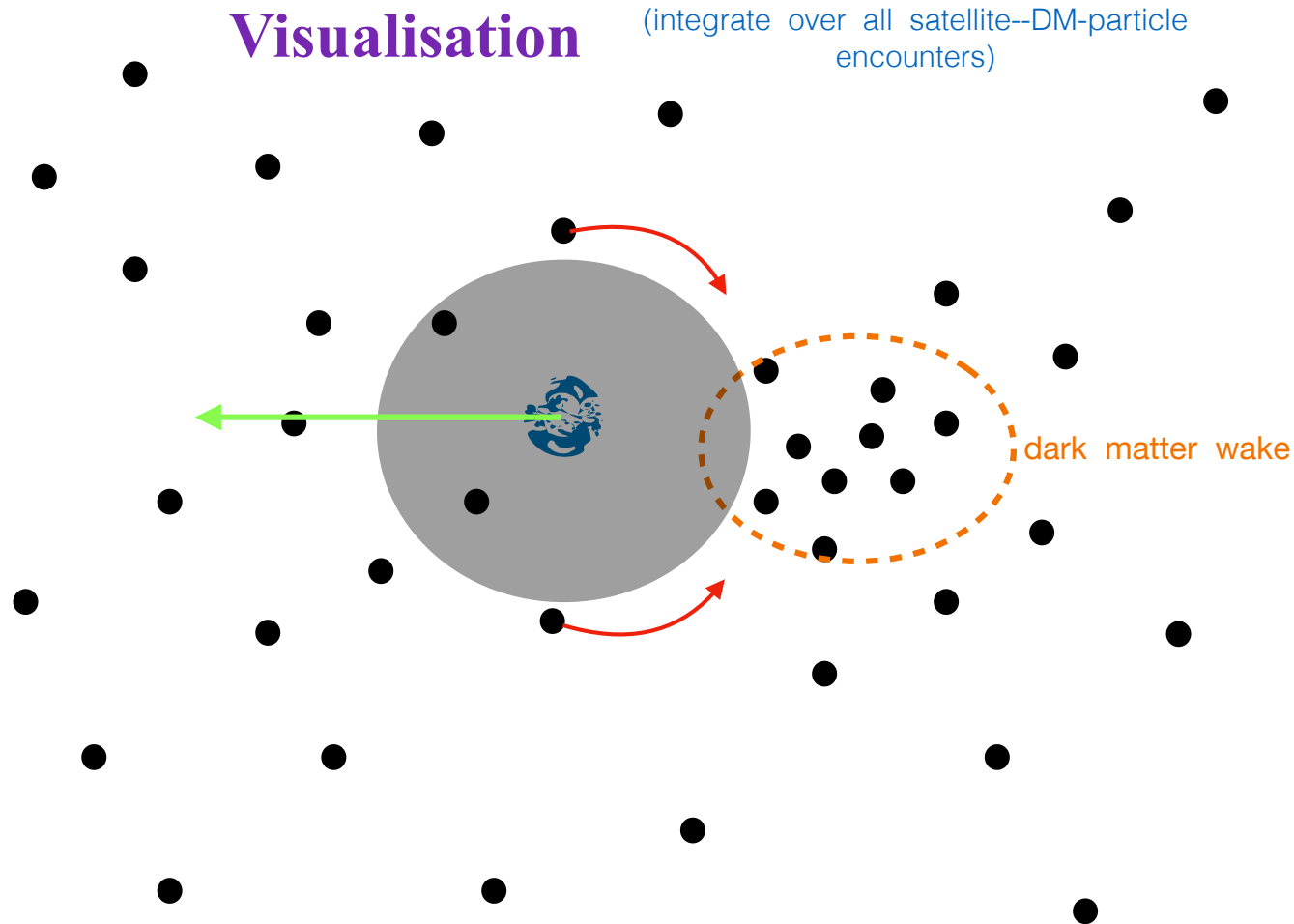
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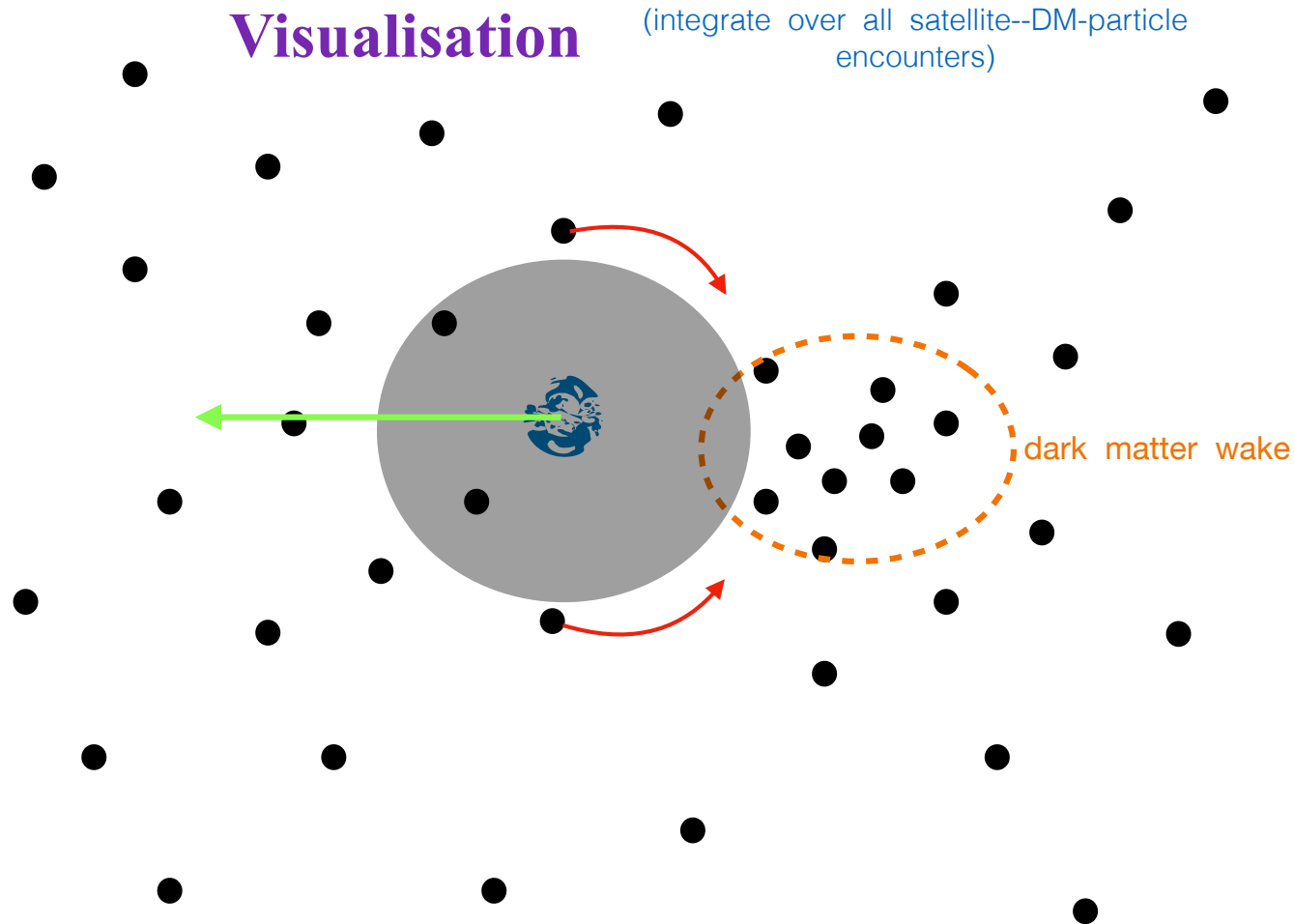
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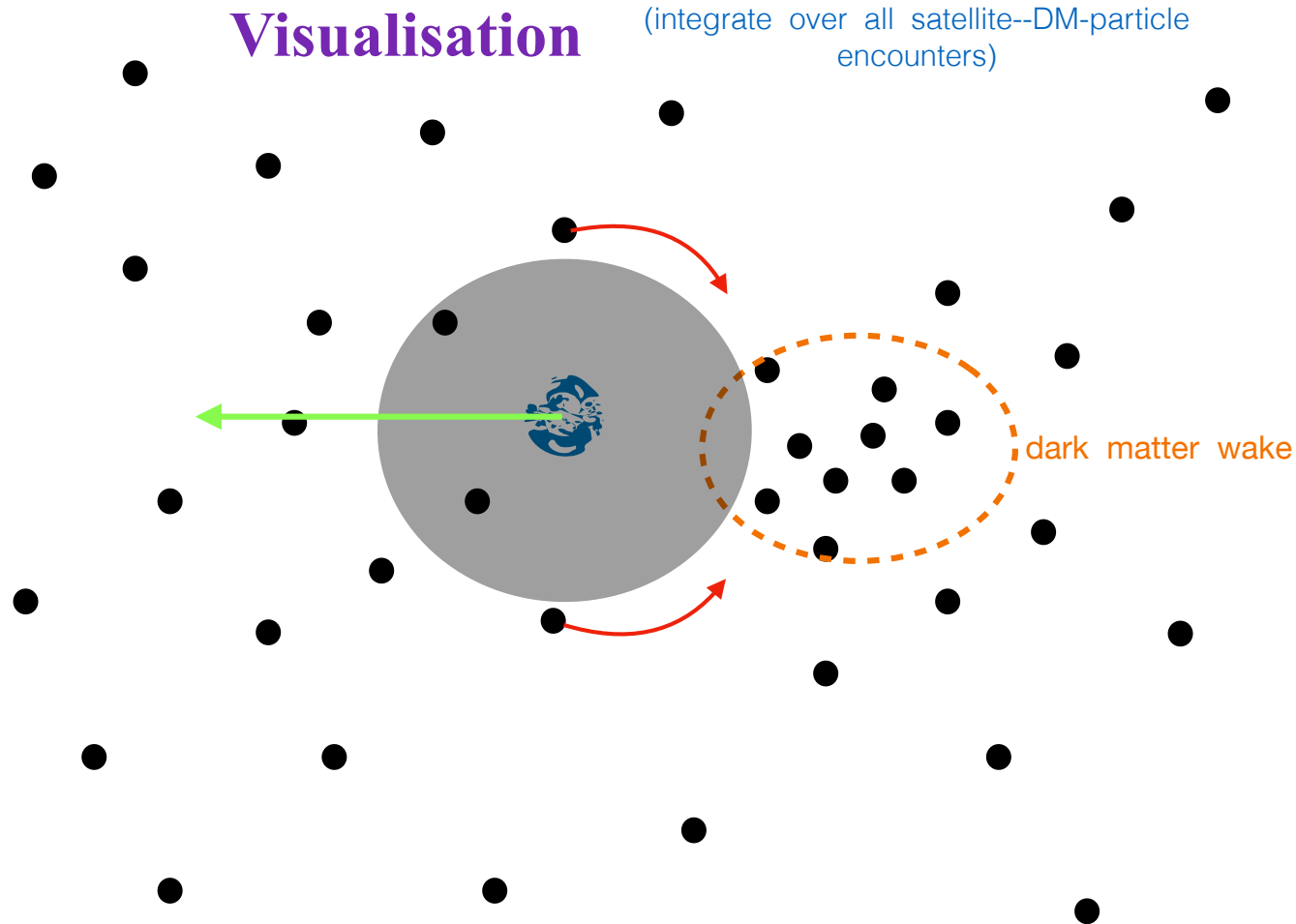
➔

$$\frac{d\vec{v}_M}{dt} = - \frac{4 \pi \ln \Lambda G^2 (M + m) \rho_0 m}{v_M^3} \left[ \operatorname{erf}(X) - \frac{2 X}{\sqrt{\pi}} e^{-X^2} \right] \vec{v}_M$$

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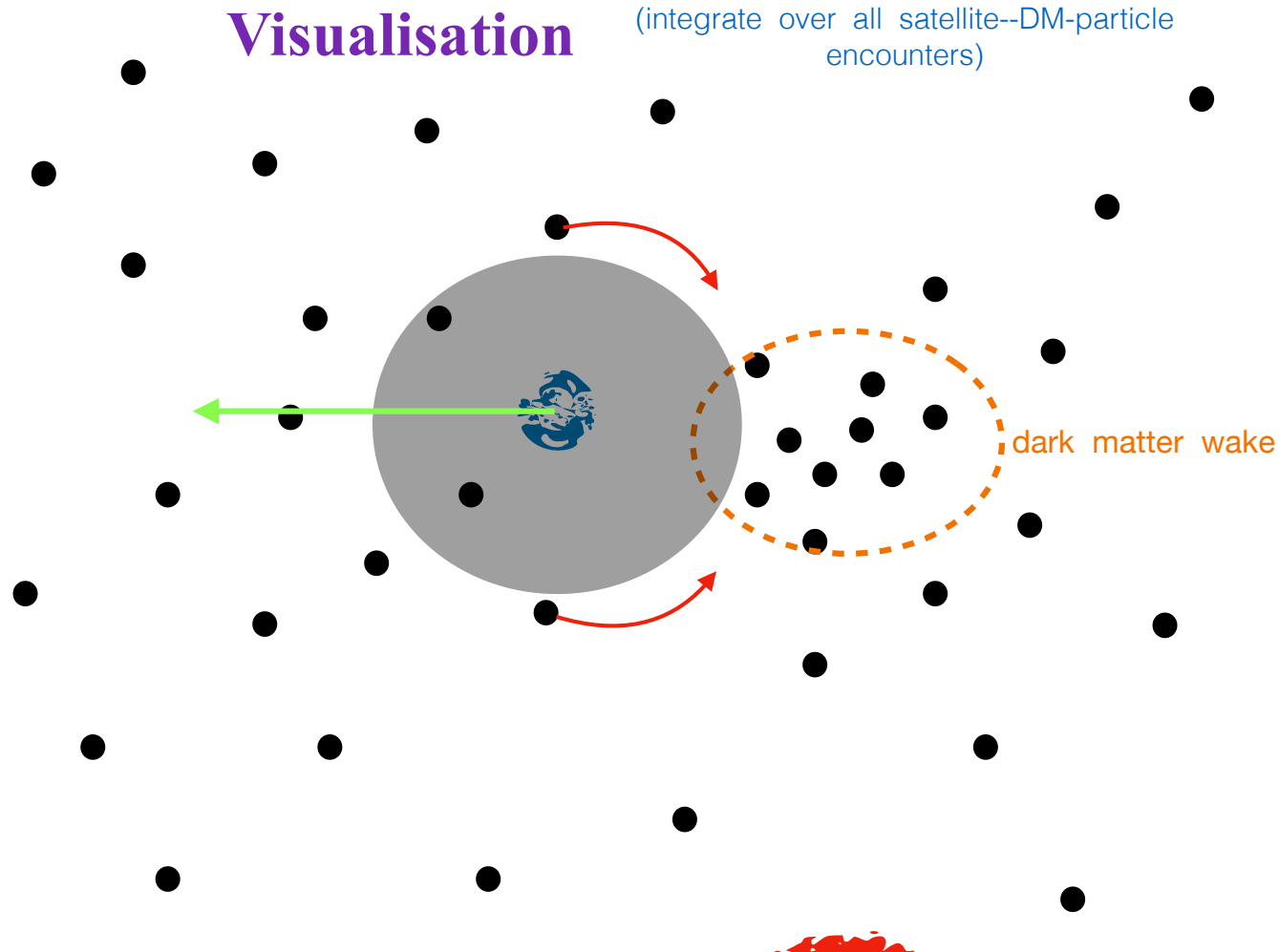
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**fixed by the CMB / SMOc**

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This test  
*insensitive*  
to mass,  $m$ ,  
of  
dark matter  
particle



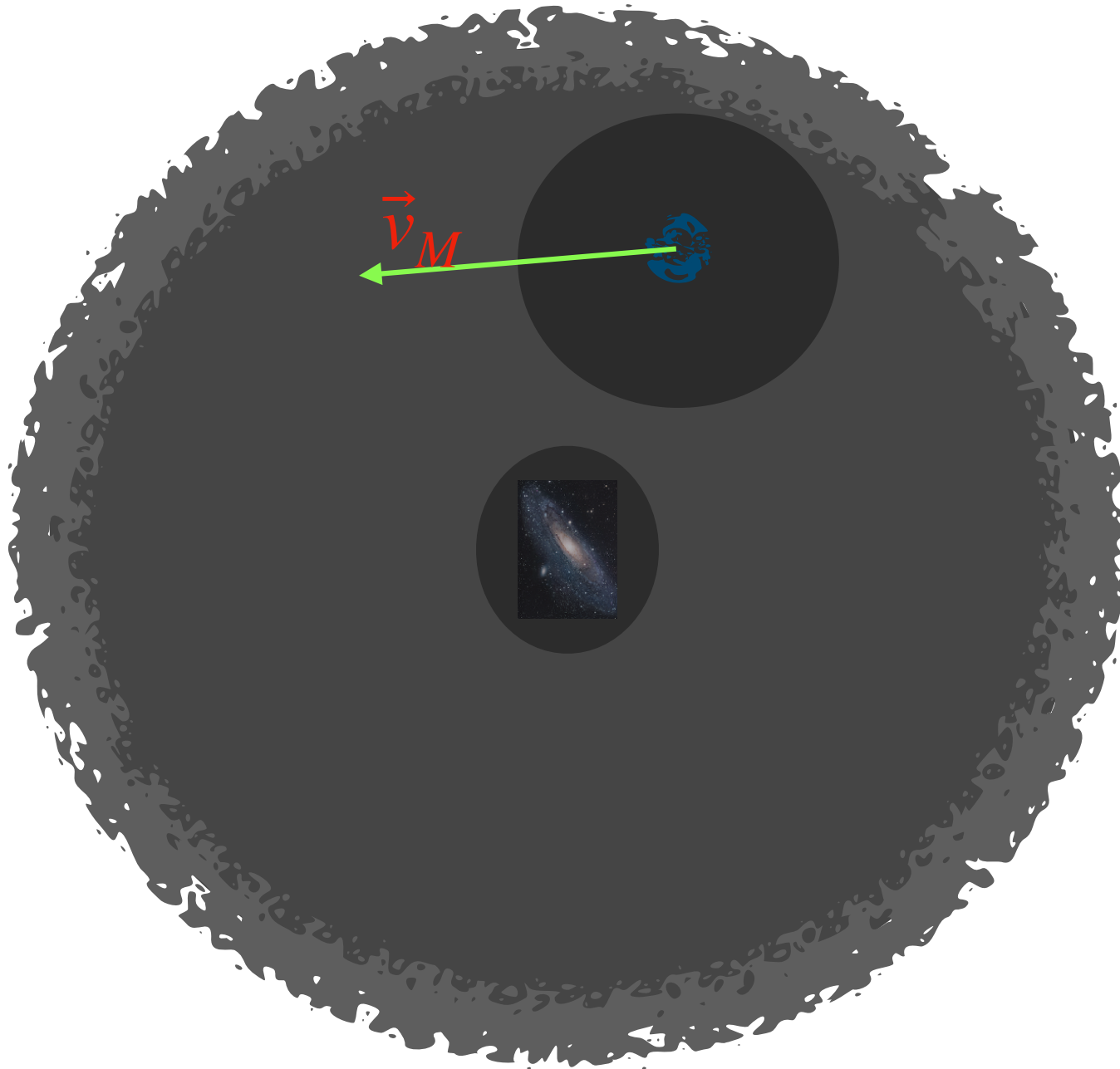
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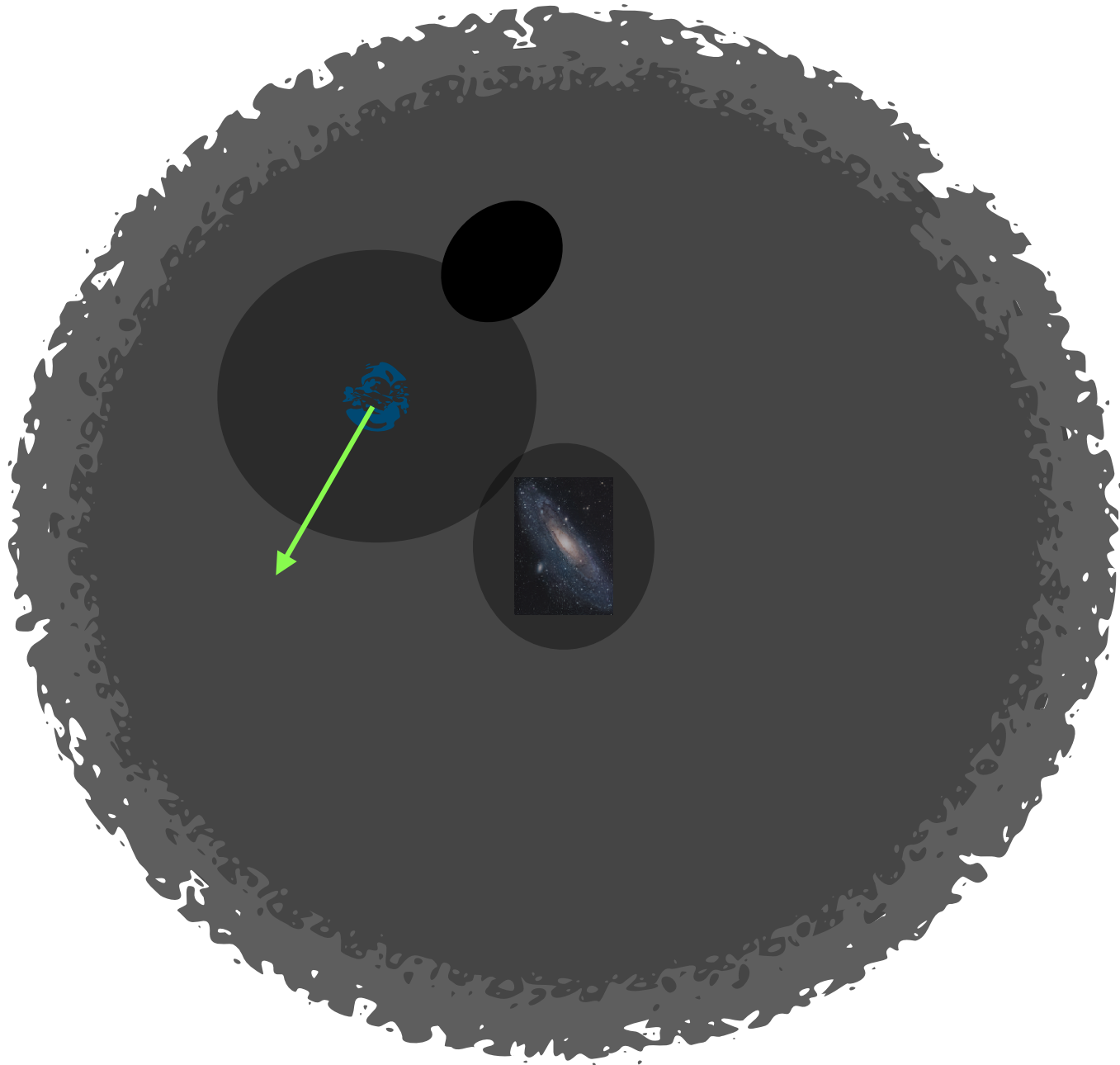
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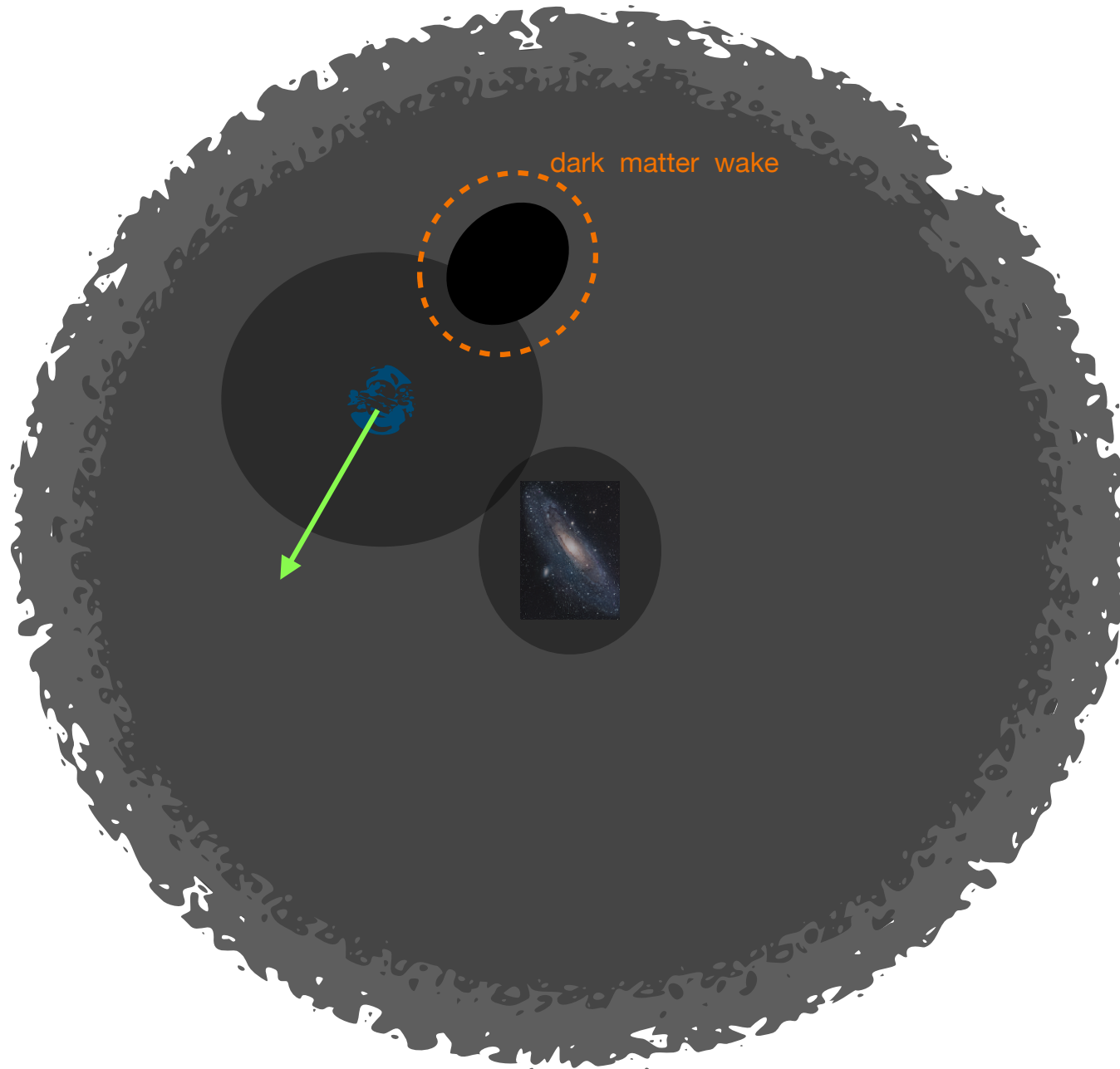
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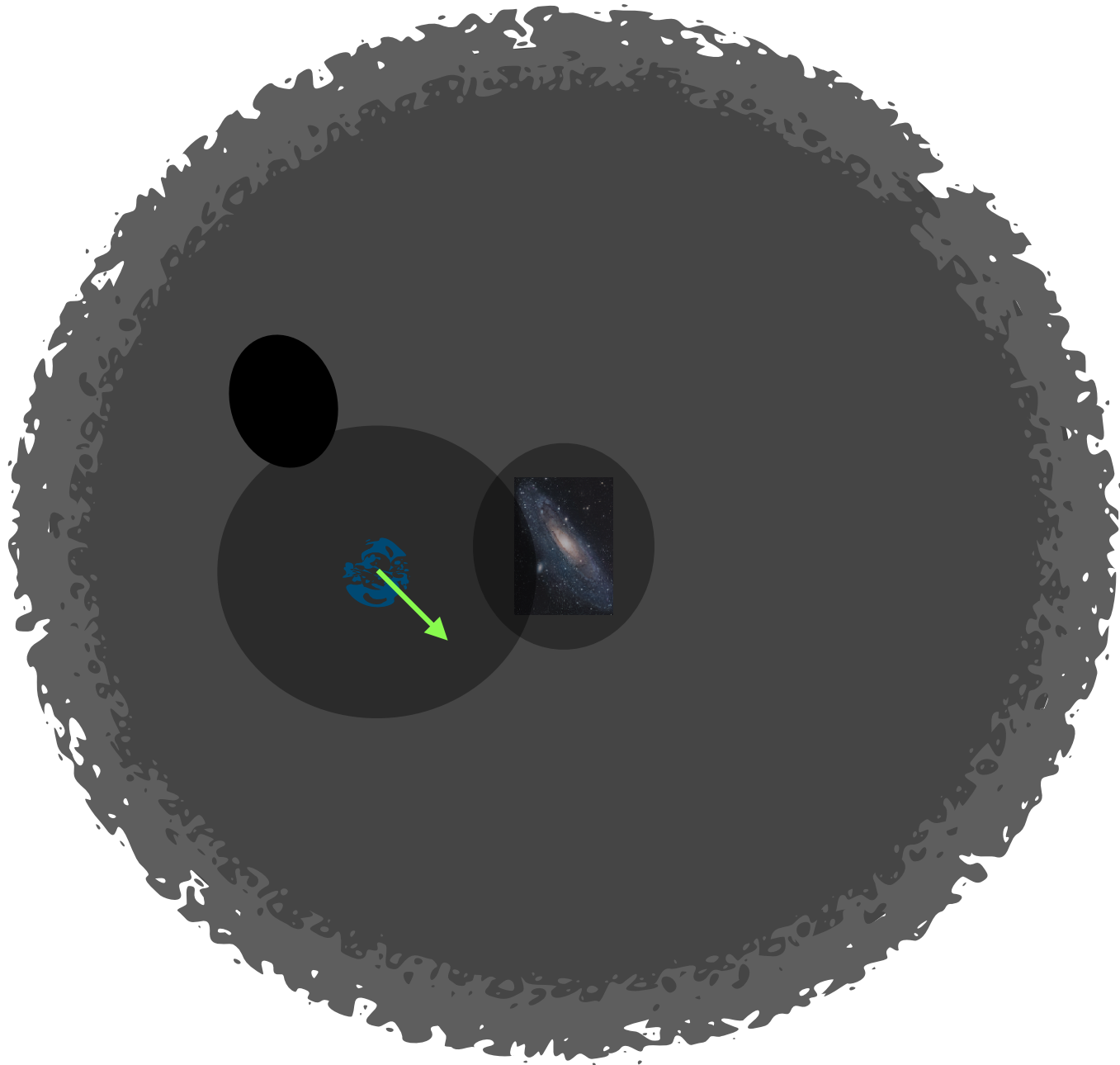
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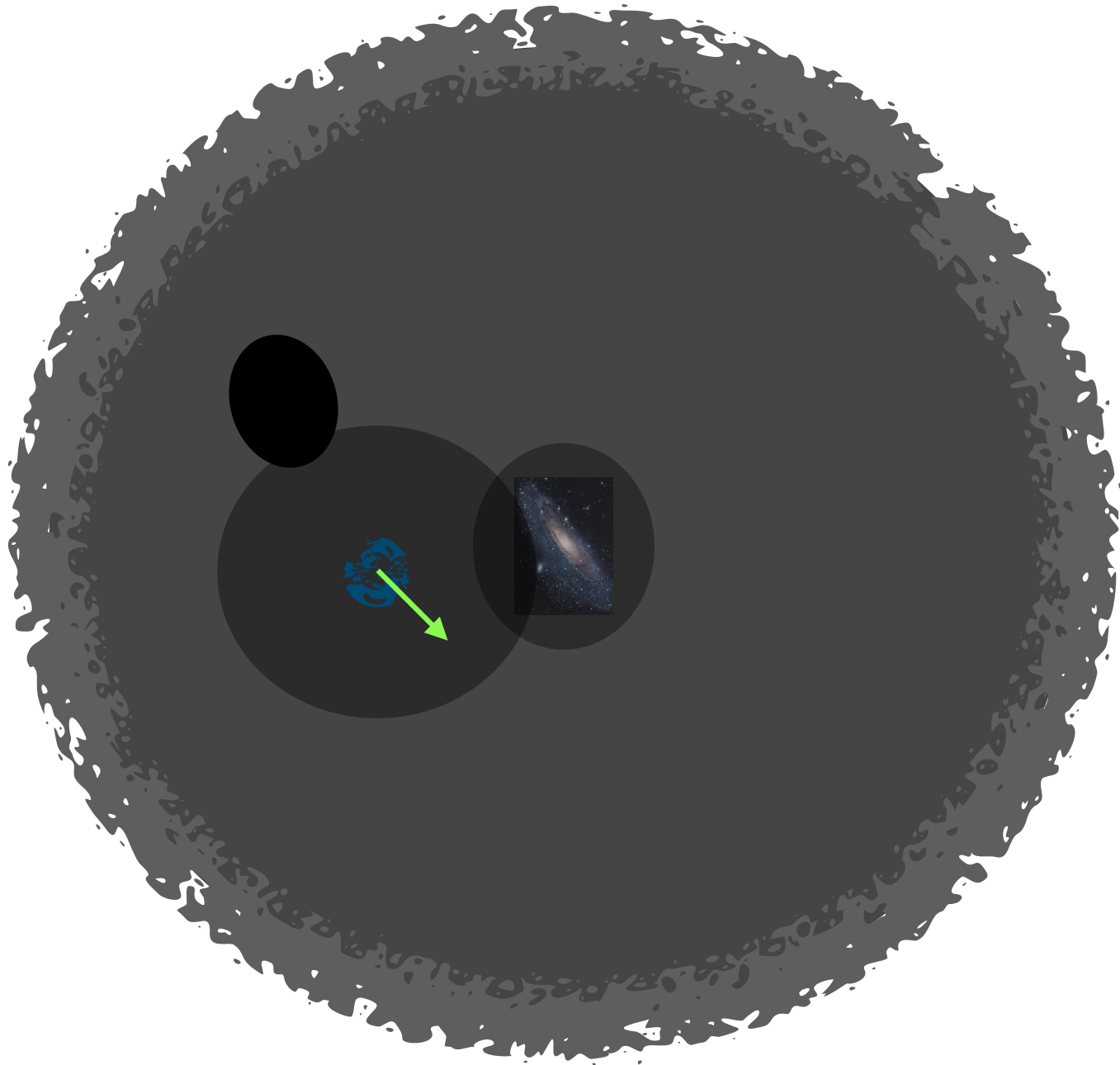
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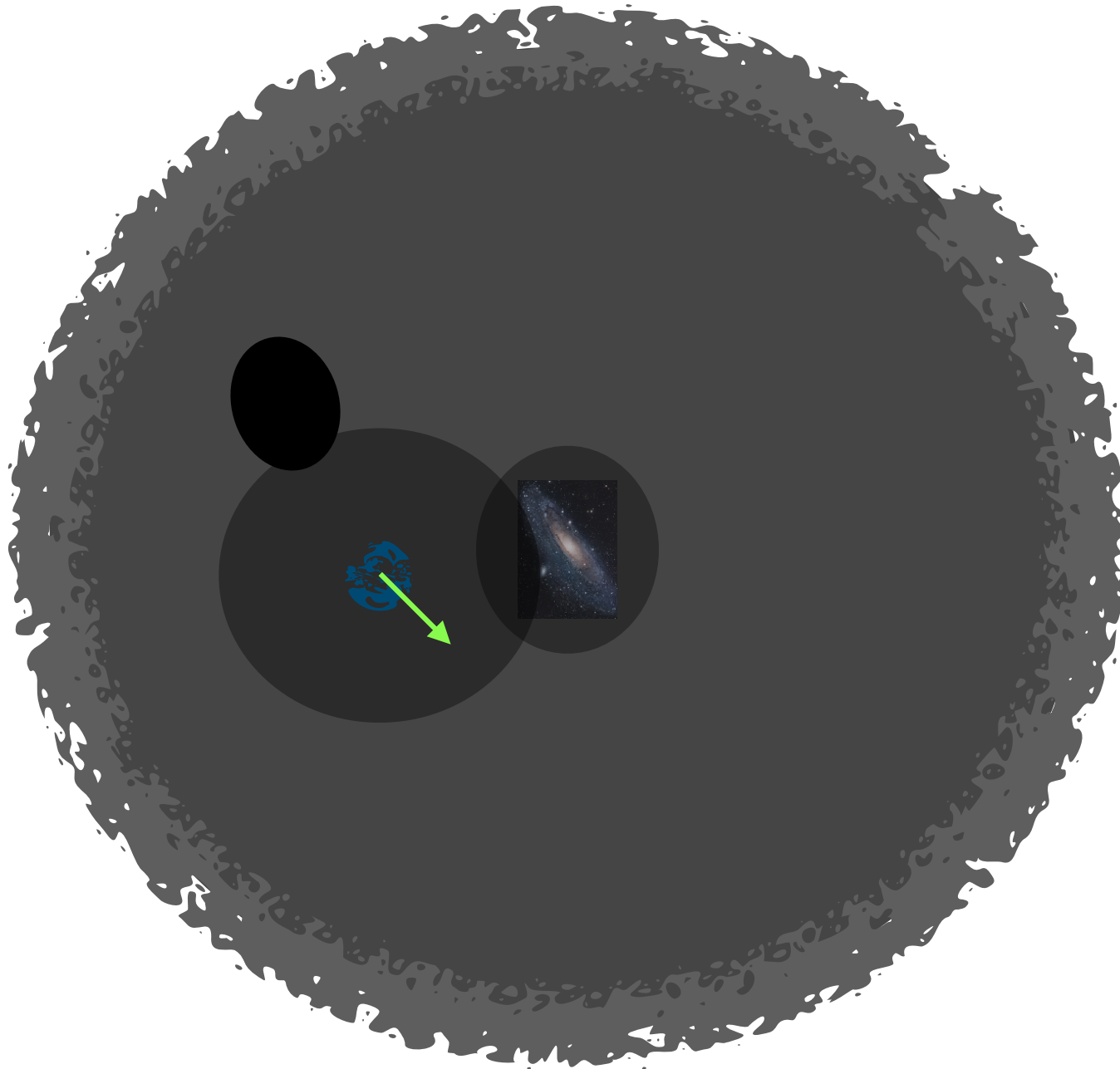
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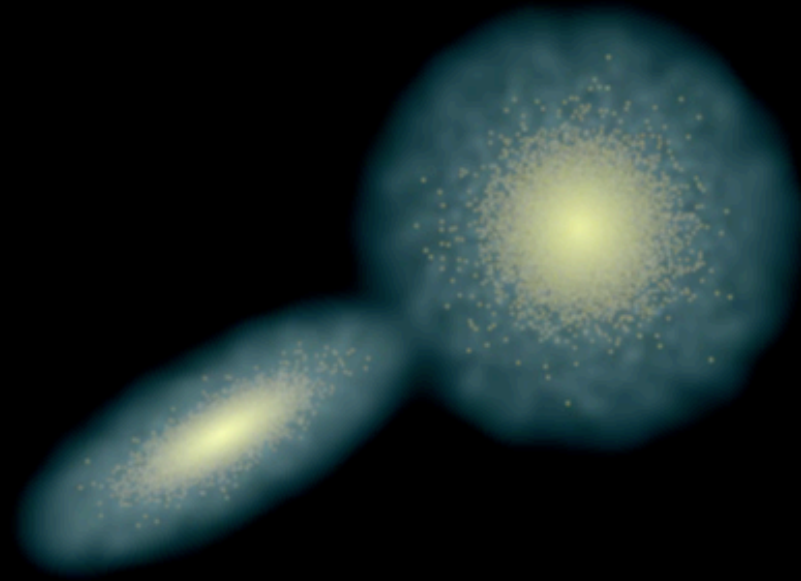
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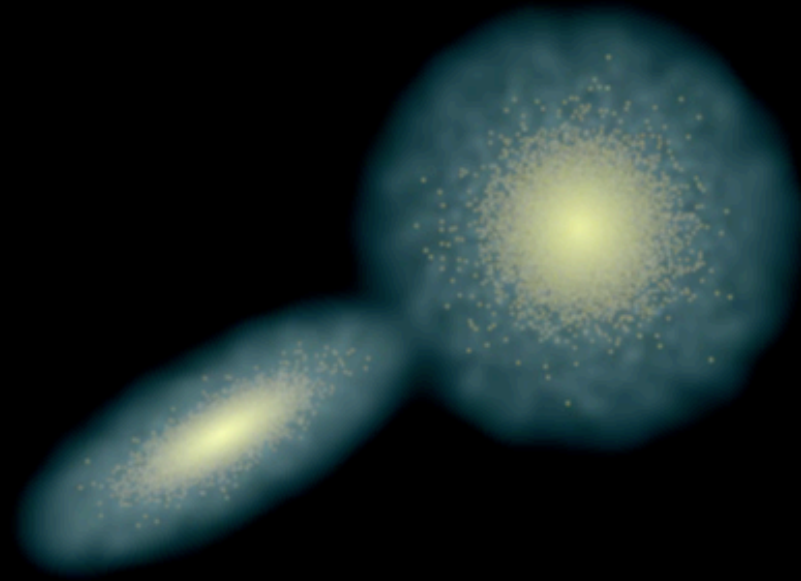


And this is why galaxies merge,  
**but only in the dark matter theory**

# Newtonian plus dark matter calculations of the encounter of two disk galaxies



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*Chandrasekhar dynamical friction*  
is very well understood.

e.g. Binney & Tremaine 1987 - textbook

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Given these properties,  
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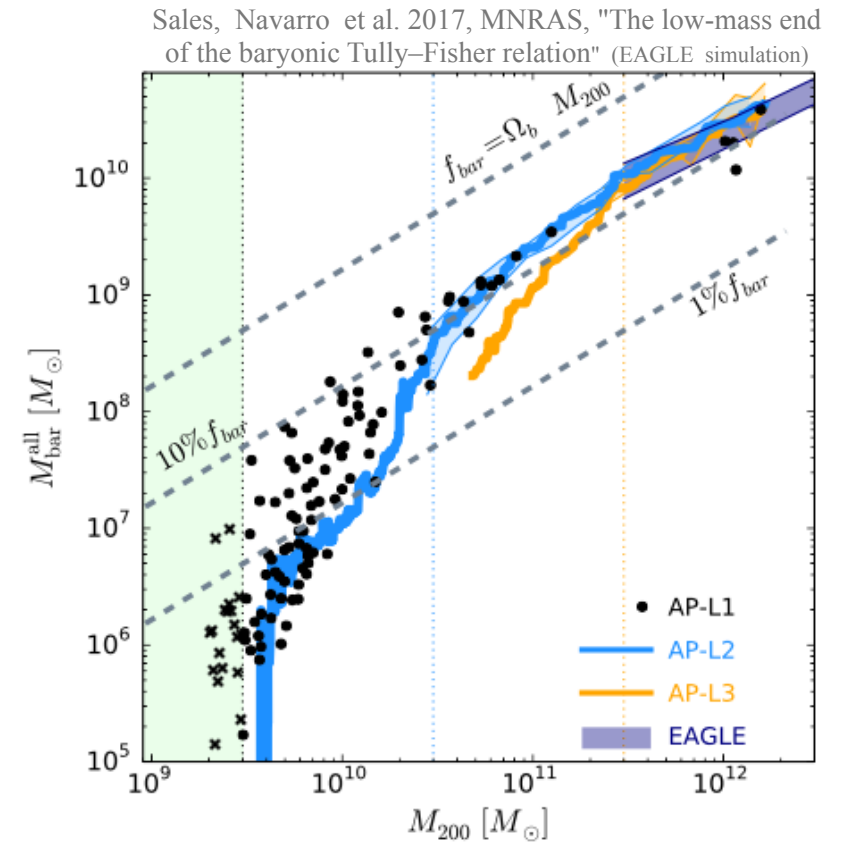
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They must have fallen-in -- so, are there infall solutions ?

# Chandrasekhar dynamical friction :

## Orbits of satellite galaxies



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## Orbits of satellite galaxies

Angus et al. 2011

**Table 2.** Galactocentric distances and velocities of the dSphs. For Fornax, Sculptor and Ursa Minor, our  $V_{x0}$  corresponds to Piatek et al. (2003, 2005, 2006, 2007a)  $V_r$  and our  $V_{y0}$  to their  $V_t$ . For Carina, the proper motion comes directly from Pasetto et al. (2011). Distances come from Mateo (1998).

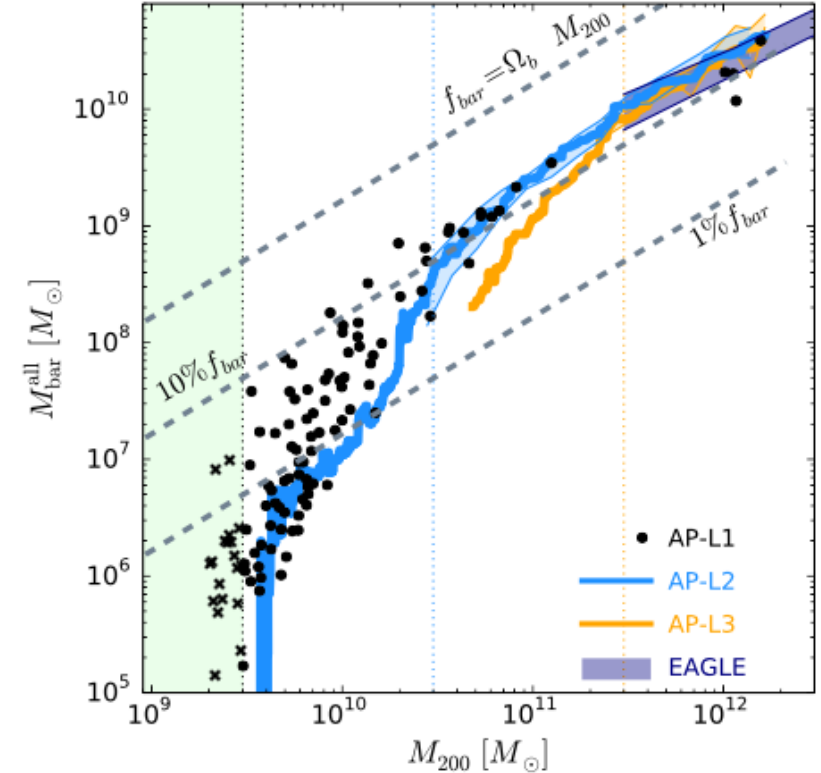
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Fornax	$138 \pm 8$	$-31.8 \pm 1.7$	$196 \pm 29$	$15.5 \times 10^6$
Sculptor	$87 \pm 4$	$79 \pm 6$	$198 \pm 50$	$2.2 \times 10^6$
Ursa Minor	$76 \pm 4$	$-75 \pm 44$	$144 \pm 50$	$0.29 \times 10^6$
Carina	$101 \pm 5$	$113 \pm 52$	$46 \pm 54$	$0.43 \times 10^6$

Note : the inner region of a satellite is affected by tides after significant tidal destruction of its outer parts

(Kazantzidis et al. 2004).

*I.e.* the baryonic content (i.e.  $L_V$ ) is a measure of the DMhalo mass according to LCDM theory.

Sales, Navarro et al. 2017, MNRAS, "The low-mass end of the baryonic Tully–Fisher relation" (EAGLE simulation)



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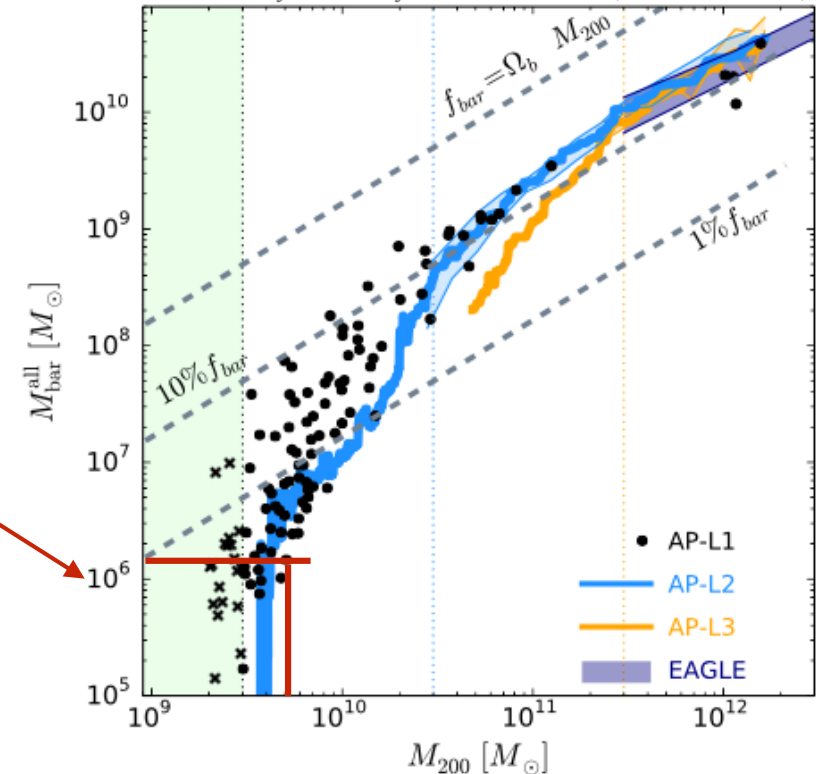
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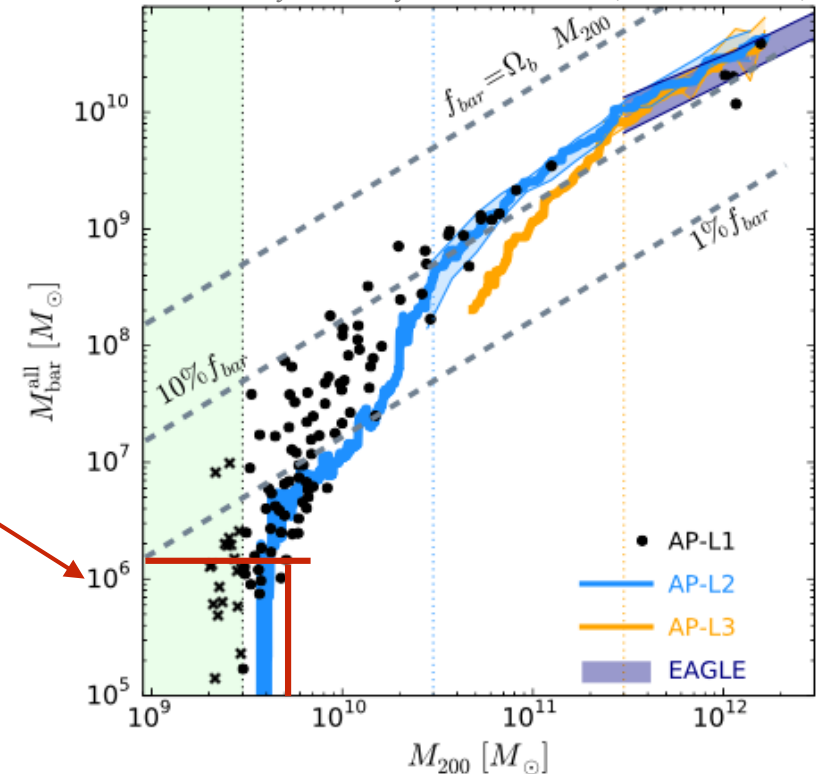
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*I.e.* the baryonic content (i.e.  $L_V$ ) is a measure of the DMhalo mass according to LCDM theory.

observed stellar masses

→  $M_{\text{DMhalo}} < 5 \times 10^9 M_\odot$

Sales, Navarro et al. 2017, MNRAS, "The low-mass end of the baryonic Tully–Fisher relation" (EAGLE simulation)



# Chandrasekhar dynamical friction :

## Orbits of satellite galaxies

Angus et al. 2011

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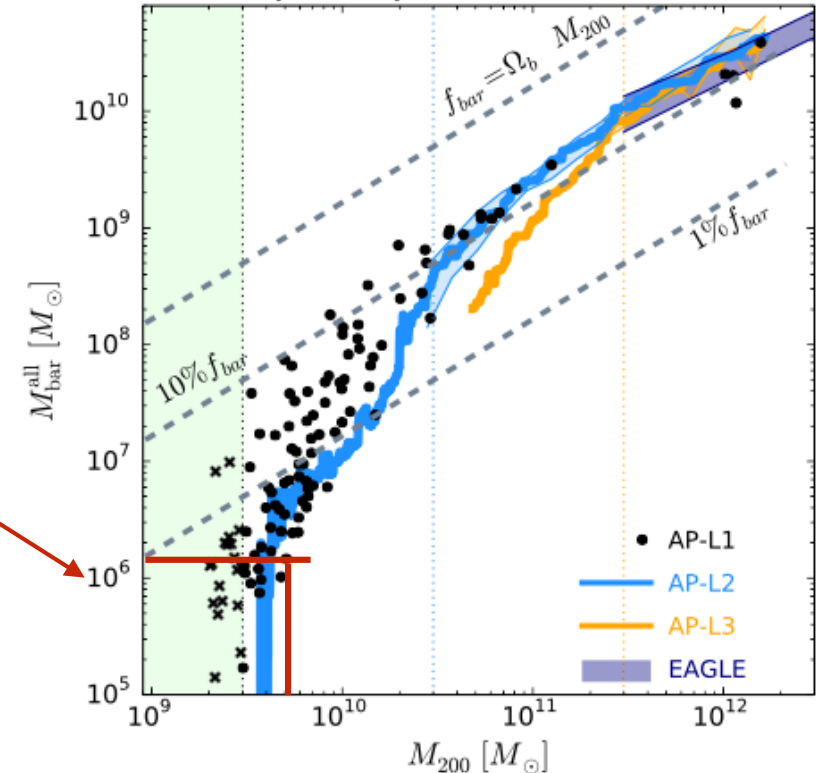
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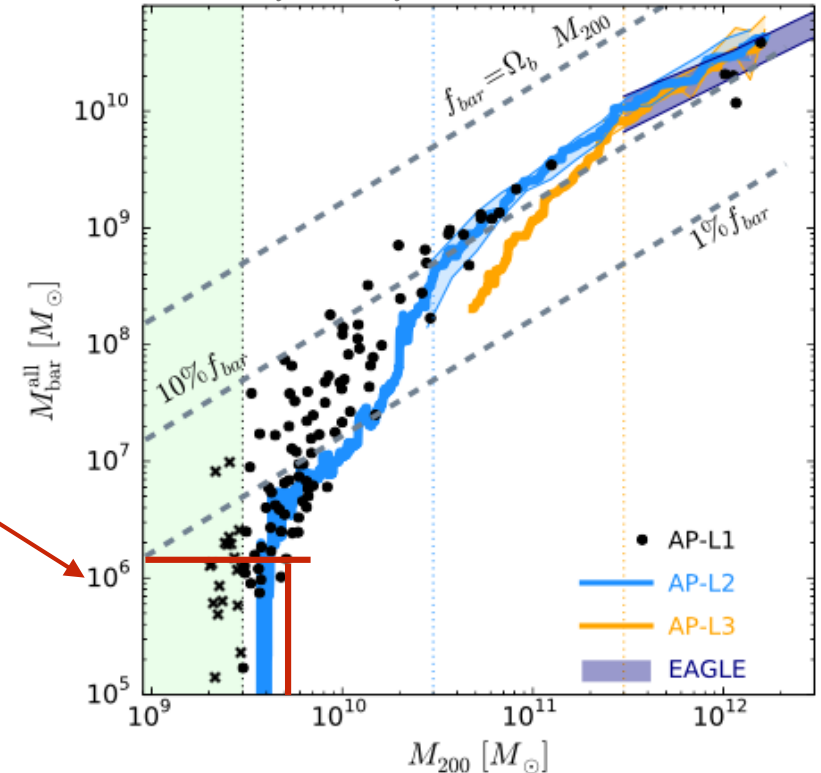
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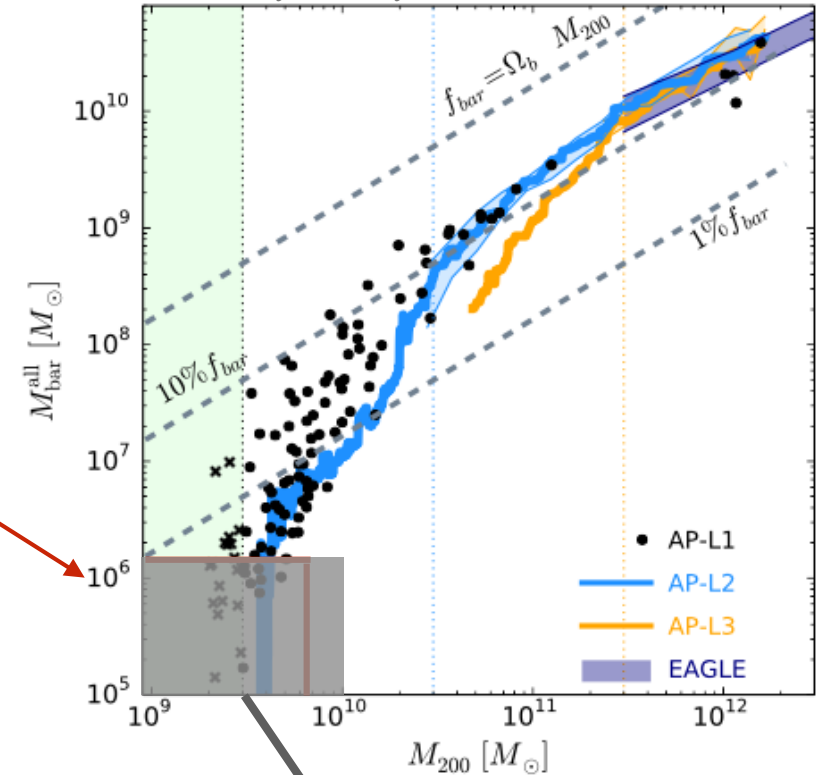
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**excluded by observational data.**

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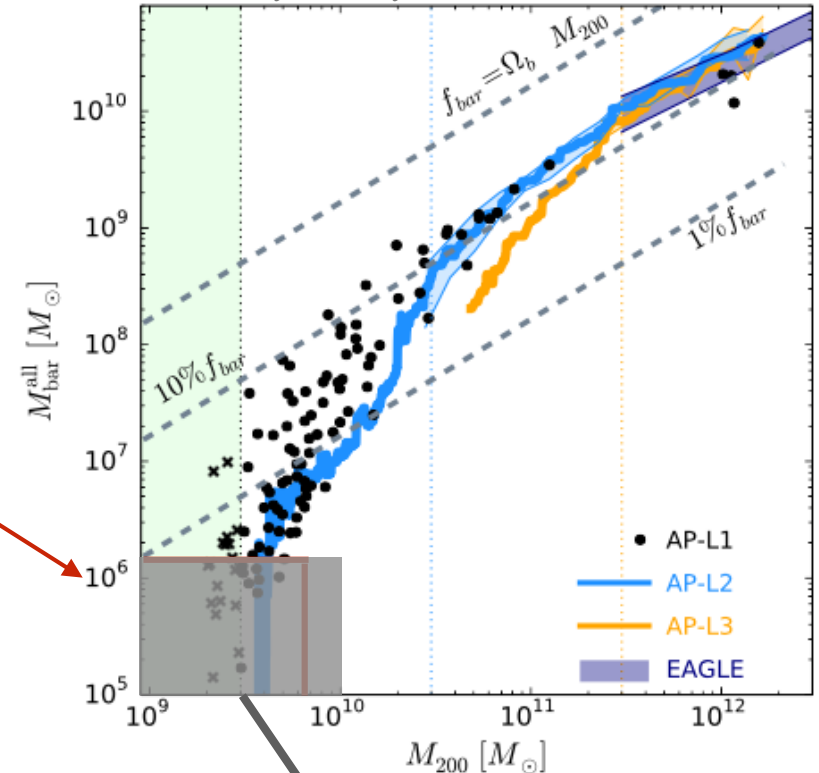
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## Orbits of satellite galaxies

Angus et al. 2011

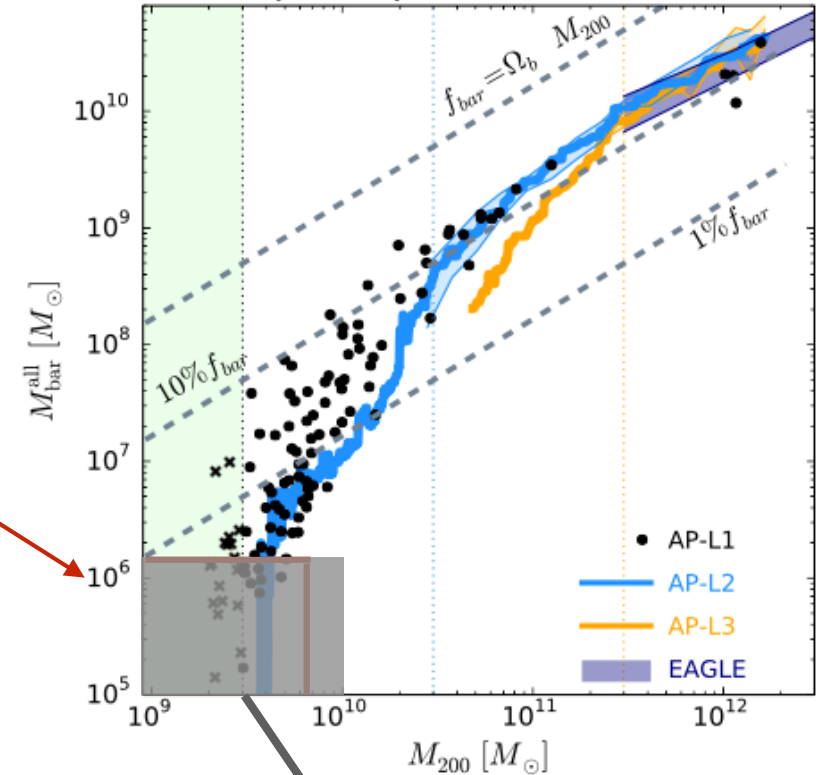
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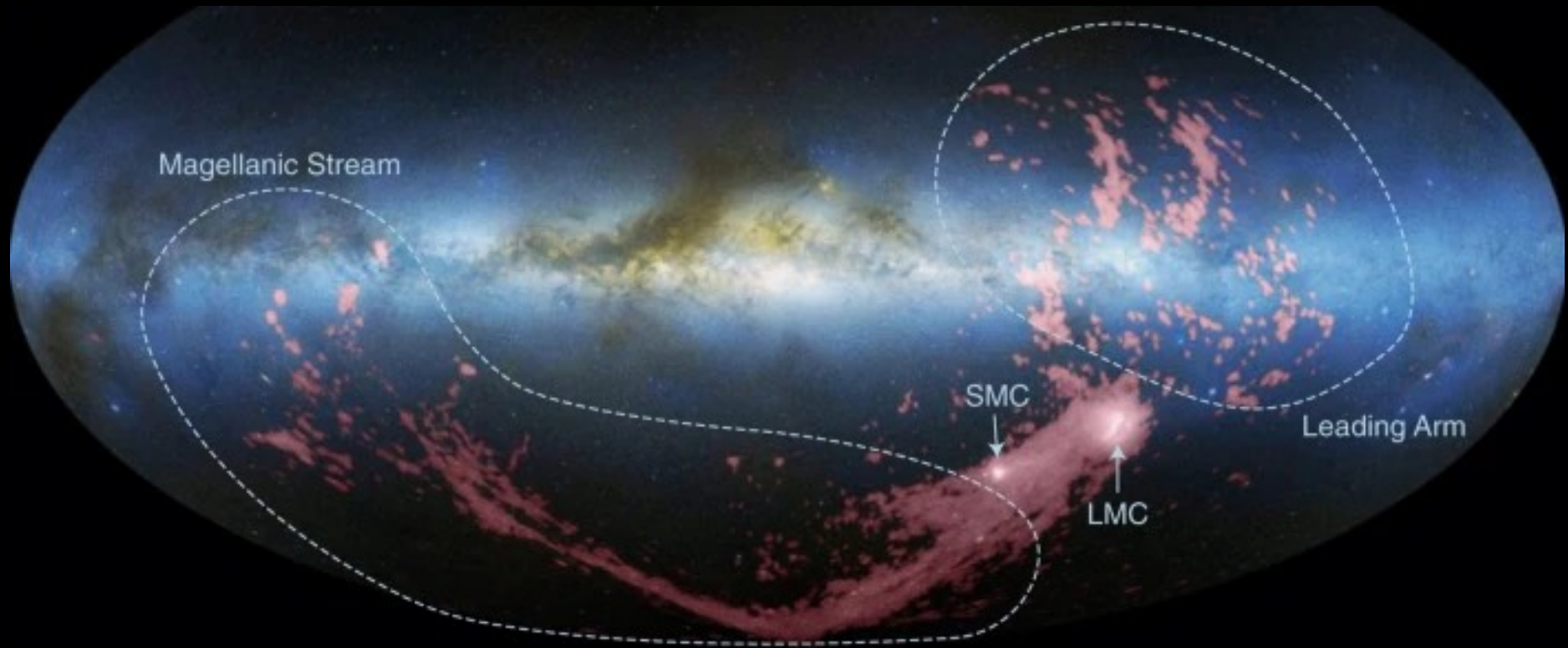
no dark matter halos

Case in point:  
The orbits  
of the  
Large (LMC)  
and  
Small (SMC)  
Magellanic Clouds



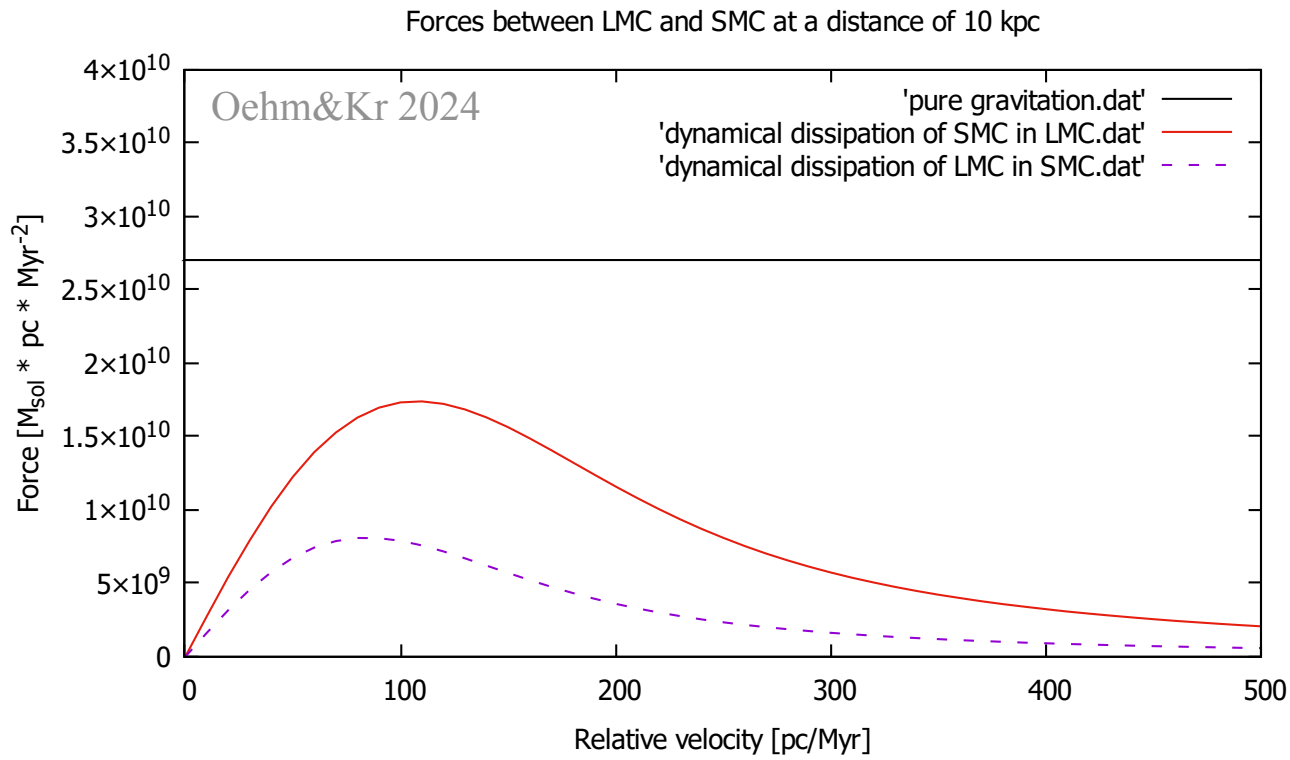
Magellanic clouds  
Magellanic Stream began to form  
about 1-2Gyr ago

e.g. Wang, Hammer...+2022



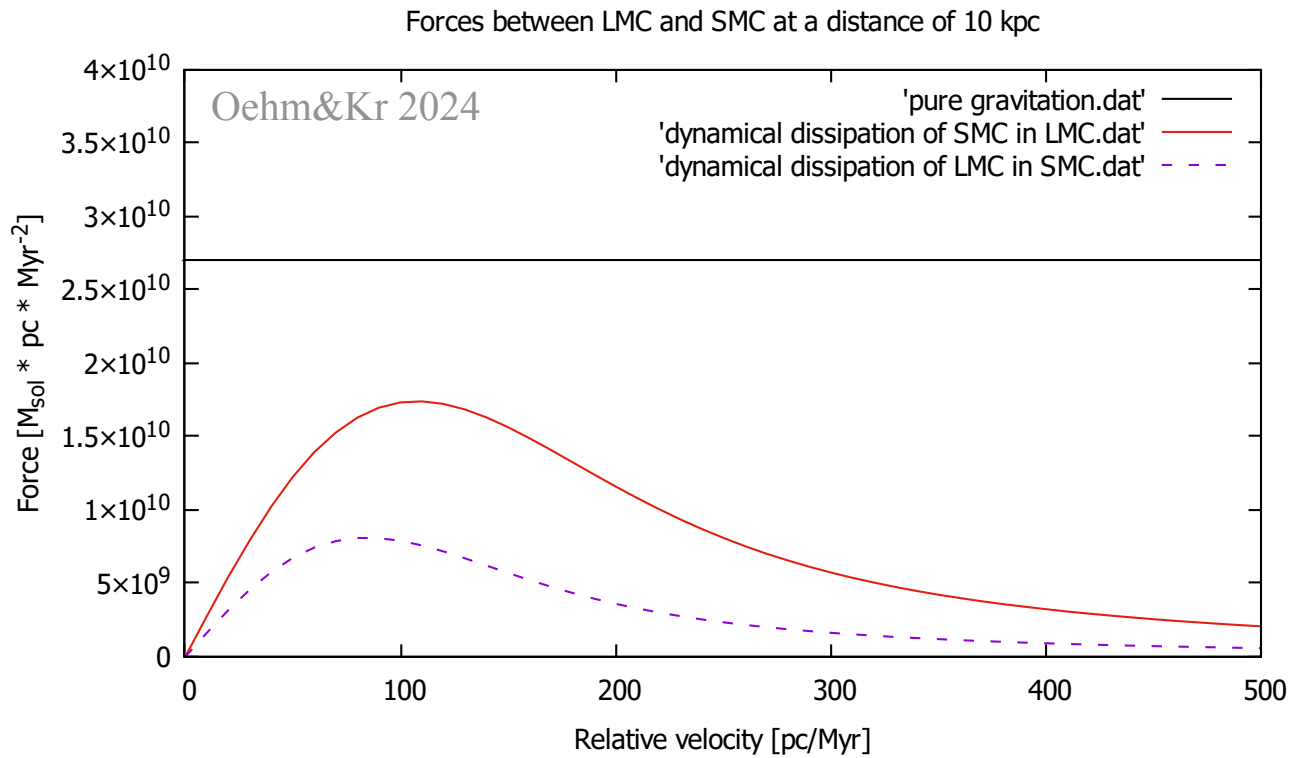
Credit: NASA/D. Nidever

Current distances : LMC-MW = 55kpc  
SMC-LMC = 20kpc



Applied to the LMC and SMC

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Applied to the LMC and SMC

The *frictional deceleration* of the LMC / SMC orbital motion due to Chandrasekhar dynamical friction is comparable to the gravitational *attraction* between the two.

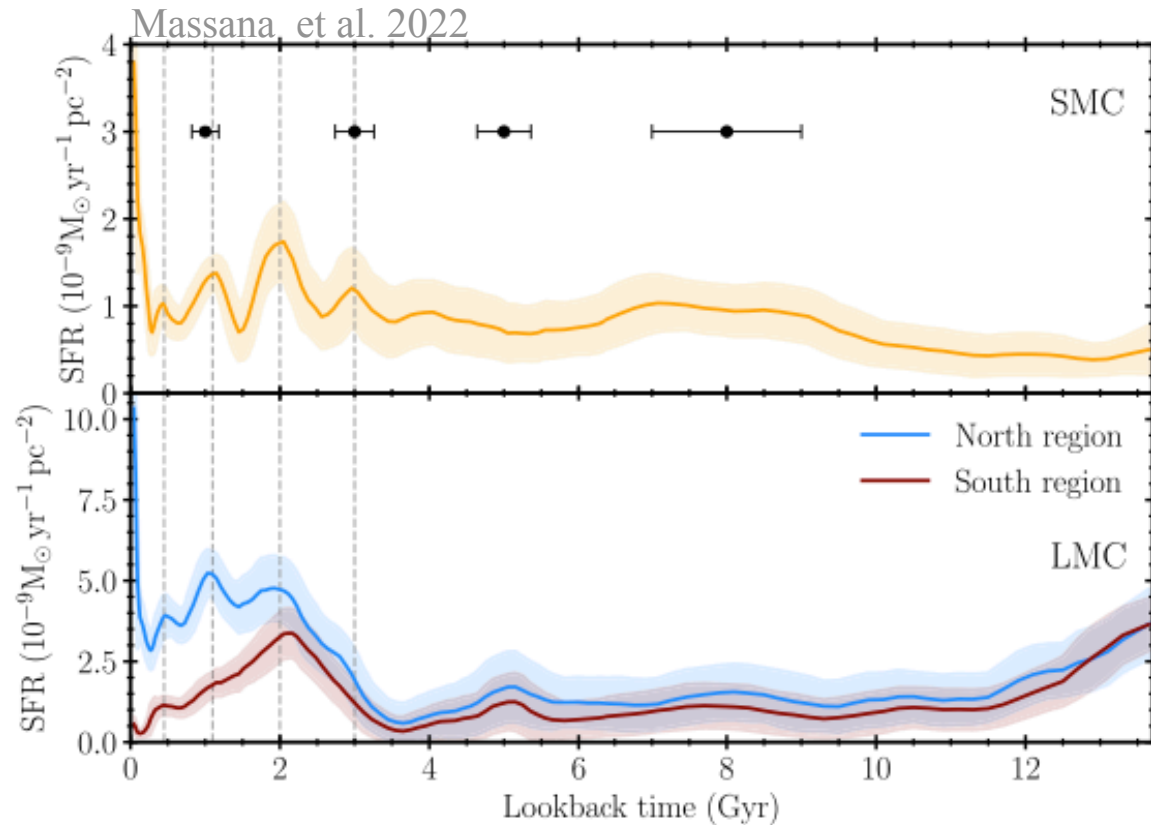


## The synchronized dance of the magellanic clouds' star formation history

P. Massana <sup>1,2</sup>★ T. Ruiz-Lara <sup>3</sup>★ N. E. D. Noël,<sup>1</sup> C. Gallart,<sup>4,5</sup> D. L. Nidever,<sup>6</sup> Y. Choi <sup>7</sup>,  
J. D. Sakowska <sup>1</sup>, G. Besla,<sup>8</sup> K. A. G. Olsen,<sup>9</sup> M. Monelli <sup>4,5</sup>, A. Dorta,<sup>4</sup> G. S. Stringfellow <sup>10</sup>,  
S. Cassisi,<sup>11,12</sup> E. J. Bernard,<sup>13</sup> D. Zaritsky <sup>8</sup>, M.-R. L. Cioni <sup>14</sup>, A. Monachesi <sup>15,16</sup>,  
R. P. van der Marel,<sup>7,17</sup> T. J. L. de Boer<sup>18</sup> and A. R. Walker<sup>19</sup>

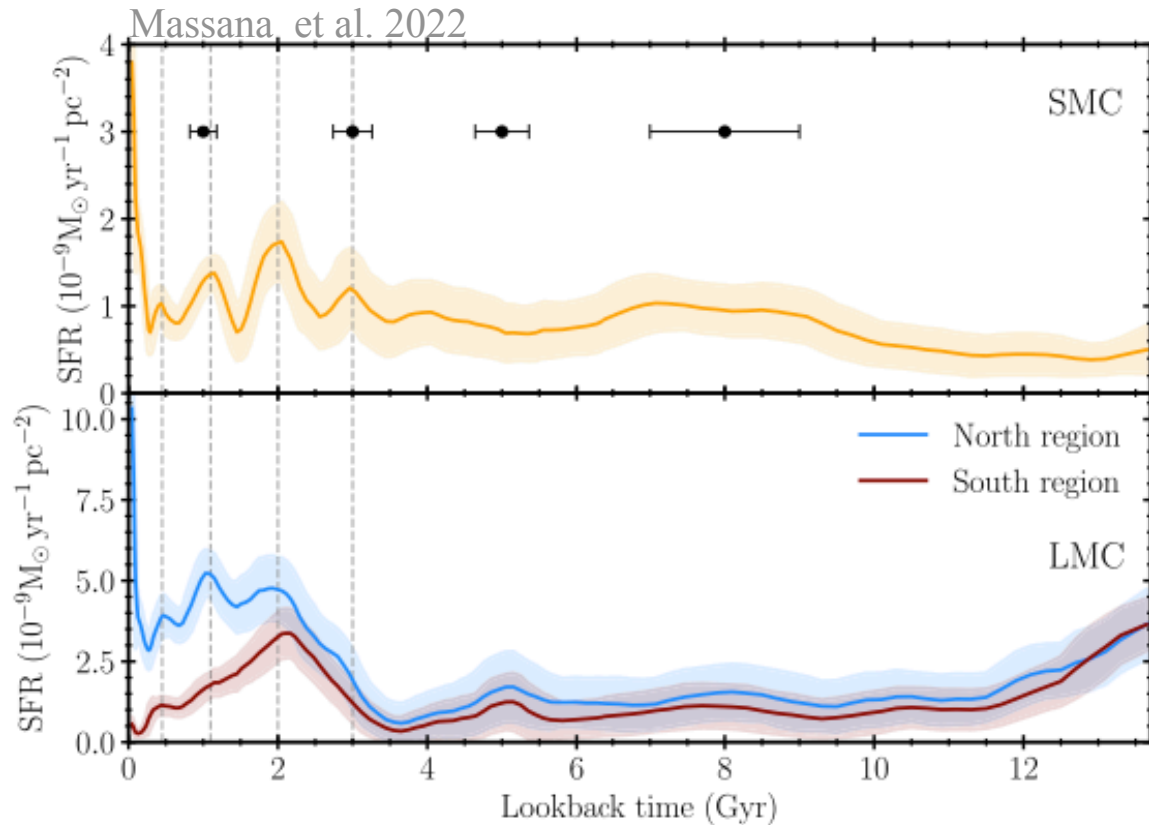
### ABSTRACT

We use the SMASH survey to obtain unprecedented deep photometry reaching down to the oldest main-sequence turn-offs in the colour–magnitude diagrams (CMDs) of the Small Magellanic Cloud (SMC) and quantitatively derive its star formation history (SFH) using CMD fitting techniques. We identify five distinctive peaks of star formation in the last 3.5 Gyr, at  $\sim 3$ ,  $\sim 2$ ,  $\sim 1.1$ ,  $\sim 0.45$  Gyr ago, and one presently. We compare these to the SFH of the Large Magellanic Cloud (LMC), finding unequivocal synchronicity, with both galaxies displaying similar periods of enhanced star formation over the past  $\sim 3.5$  Gyr. The parallelism between their SFHs indicates that tidal interactions between the MCs have recurrently played an important role in their evolution for at least the last  $\sim 3.5$  Gyr, tidally truncating the SMC and shaping the LMC's spiral arm. We show, for the first time, an SMC–LMC correlated SFH at recent times in which enhancements of star formation are localized in the northern spiral arm of the LMC, and globally across the SMC. These novel findings should be used to constrain not only the orbital history of the MCs but also how star formation should be treated in simulations.



The LMC and SMC have peaks in the SFRs at very similar times because of their orbits about each other.

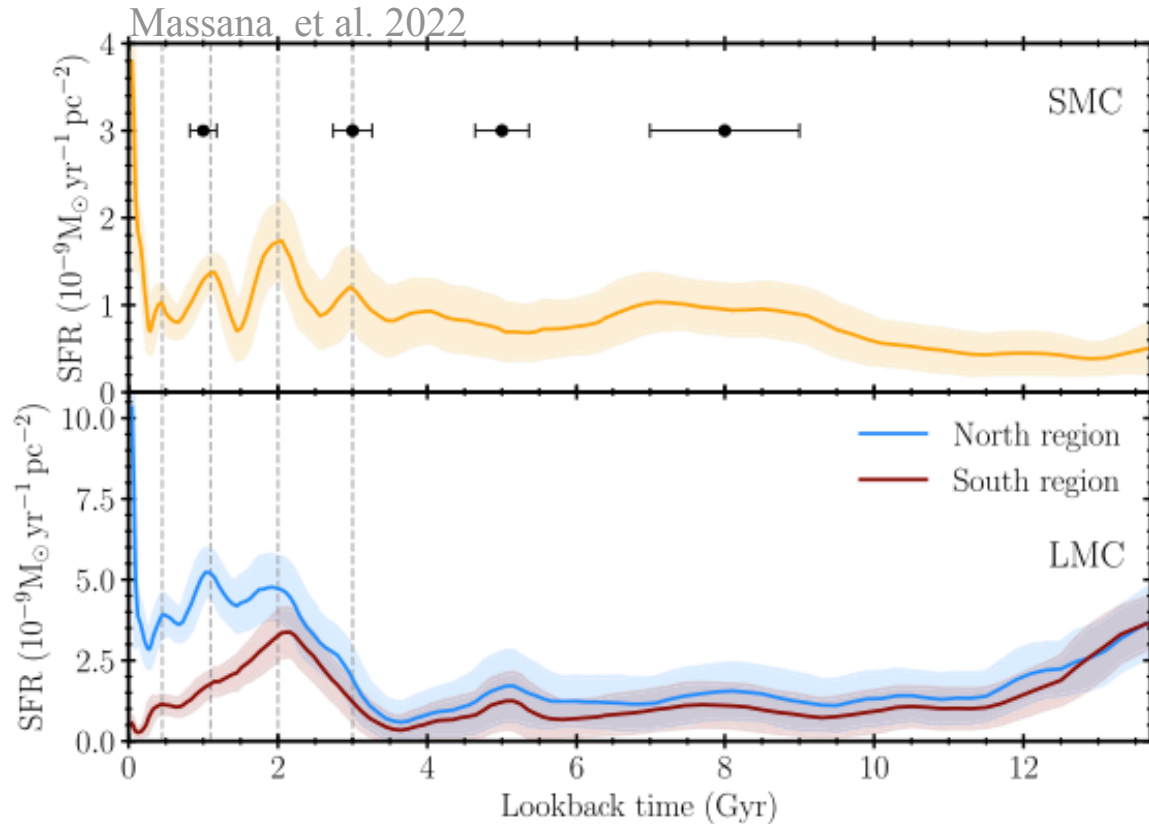
**Figure 2.** Comparison of the global SFRs for the SMC (this work) and the LMC (Ruiz-Lara et al. 2020b). Vertical dashed lines link the peaks at 0.45, 1.1, 2, and 3 Gyr ago in the SMC to those of the LMC. The horizontal bars in the top panel show the width of the SFH enhancement. Uncertainties in the SFHs (shaded regions) were calculated as in Hidalgo et al. (2011) and Rusakov et al. (2021).



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4 over the past 3Gyr !

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Search for solutions using (i) genetic algorithm and (ii) Markov-Chain Monte-Carlo method  
within the  $5\sigma$  uncertainty bounds of velocities  
such that LMC and SMC had an encounter between 1 and 4 Gyr ago with a separation of 20kpc or smaller.

Search for solutions using (i) genetic algorithm and (ii) Markov-Chain Monte-Carlo method within the 5sigma uncertainty bounds of velocities such that LMC and SMC had an encounter between 1 and 4 Gyr ago with a separation of 20kpc or smaller.

**Table 1.** Stellar masses of the galaxies (model (o)), varied by -30% (model (m)) and +30% (model (p)), and the derived DM halo masses according to Section 2.1.

Object	Model	Stellar Mass	DM Halo Mass
		$[M_{\odot}]$	$[M_{\odot}]$
MW	(o)	$5 \times 10^{10}$	$2.41 \times 10^{12}$
	-30% (m)	$3.5 \times 10^{10}$	$1.39 \times 10^{12}$
	+30% (p)	$6.5 \times 10^{10}$	$4.05 \times 10^{12}$
LMC	(o)	$3.2 \times 10^9$	$2.55 \times 10^{11}$
	-30% (m)	$2.24 \times 10^9$	$1.47 \times 10^{11}$
	+30% (p)	$4.16 \times 10^9$	$2.90 \times 10^{11}$
SMC	(o)	$5.3 \times 10^8$	$1.07 \times 10^{11}$
	-30% (m)	$3.71 \times 10^8$	$8.86 \times 10^{10}$
	+30% (p)	$6.89 \times 10^8$	$1.24 \times 10^{11}$

Oehm & Kroupa 2024

**Table 3.** Observational data for LMC and SMC and in parts for the Galactic centre.

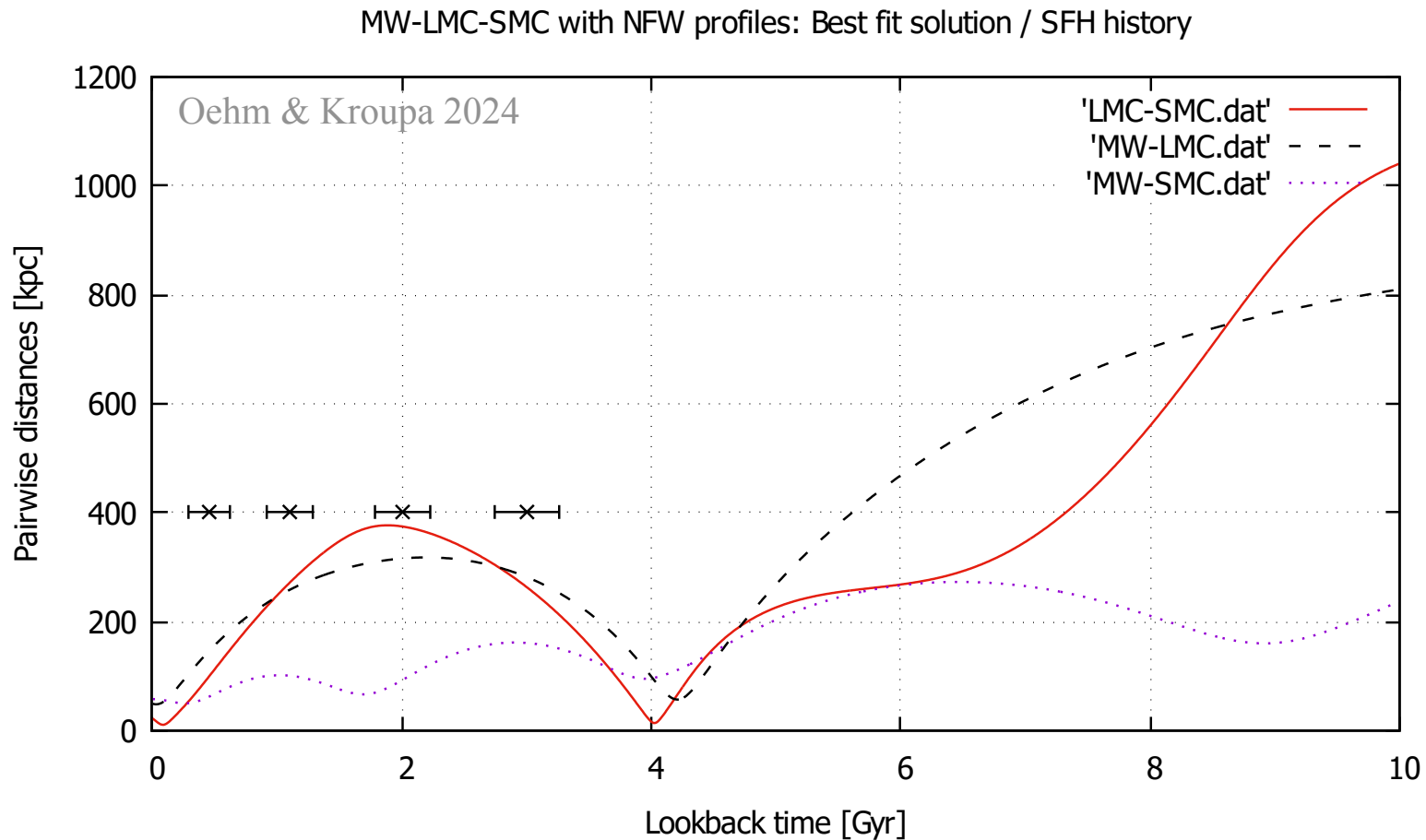
Object	RA	DEC	Heliocentric	Heliocentric
	(EquJ2000)	(EquJ2000)	Distance	Radial Velocity
LMC	80.894°	-69.756°	49.97 kpc	262.2 km/s
SMC	13.187°	-72.829°	60.6 kpc	145.6 km/s
MW	266.405°	-28.936°	8.122 kpc	

**Table 4.** Transverse velocity components for LMC and SMC.

Object	$v_{RA}$	$v_{RA}$	$v_{DEC}$	$v_{DEC}$
	[mas/yr]	[km/s]	[mas/yr]	[km/s]
LMC	$1.872 \pm 0.045$	$443.3 \pm 10.7$	$0.224 \pm 0.054$	$53.0 \pm 12.8$
SMC	$0.820 \pm 0.060$	$235.5 \pm 17.2$	$-1.230 \pm 0.070$	$-353.3 \pm 20.1$

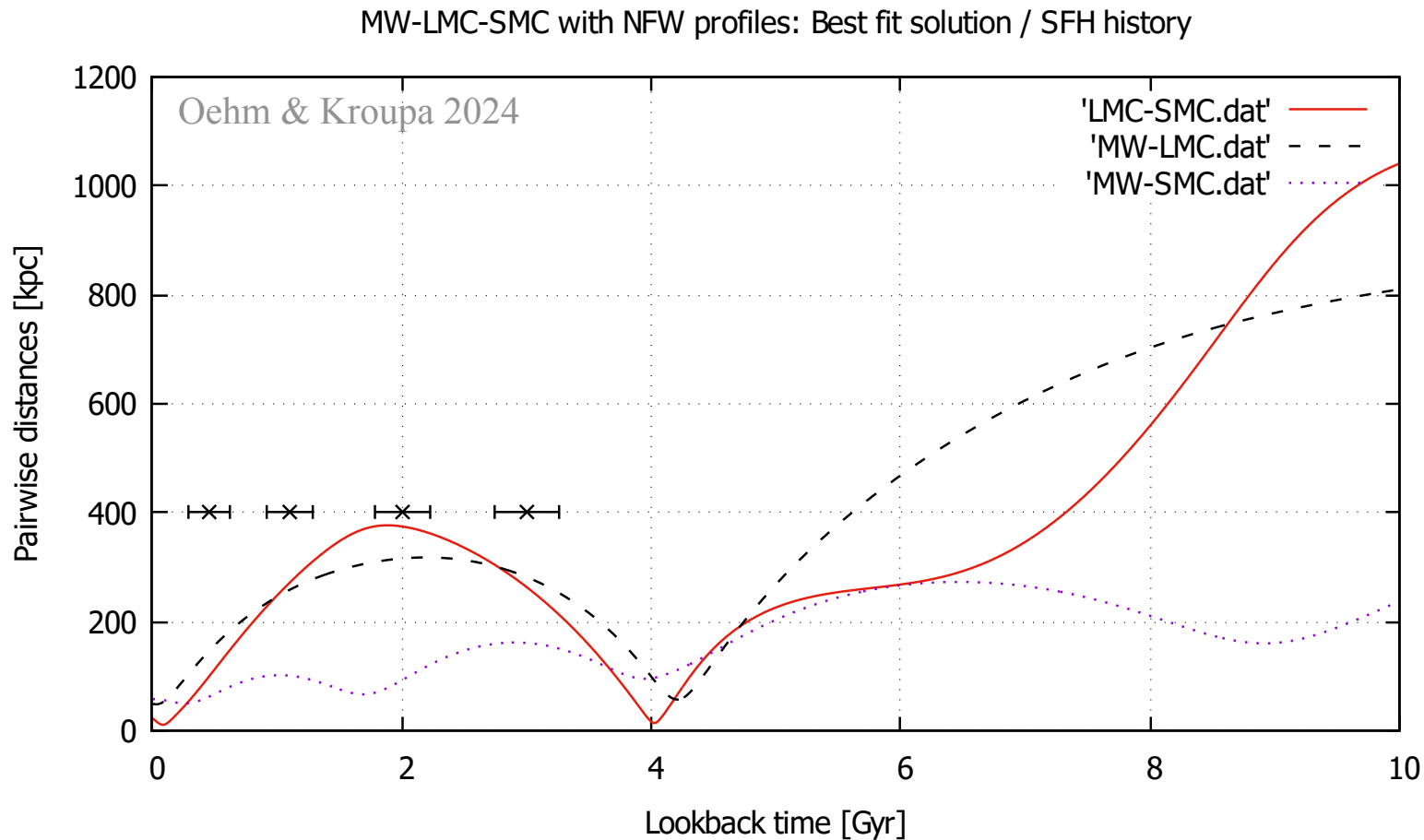
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according to the SMOc and  
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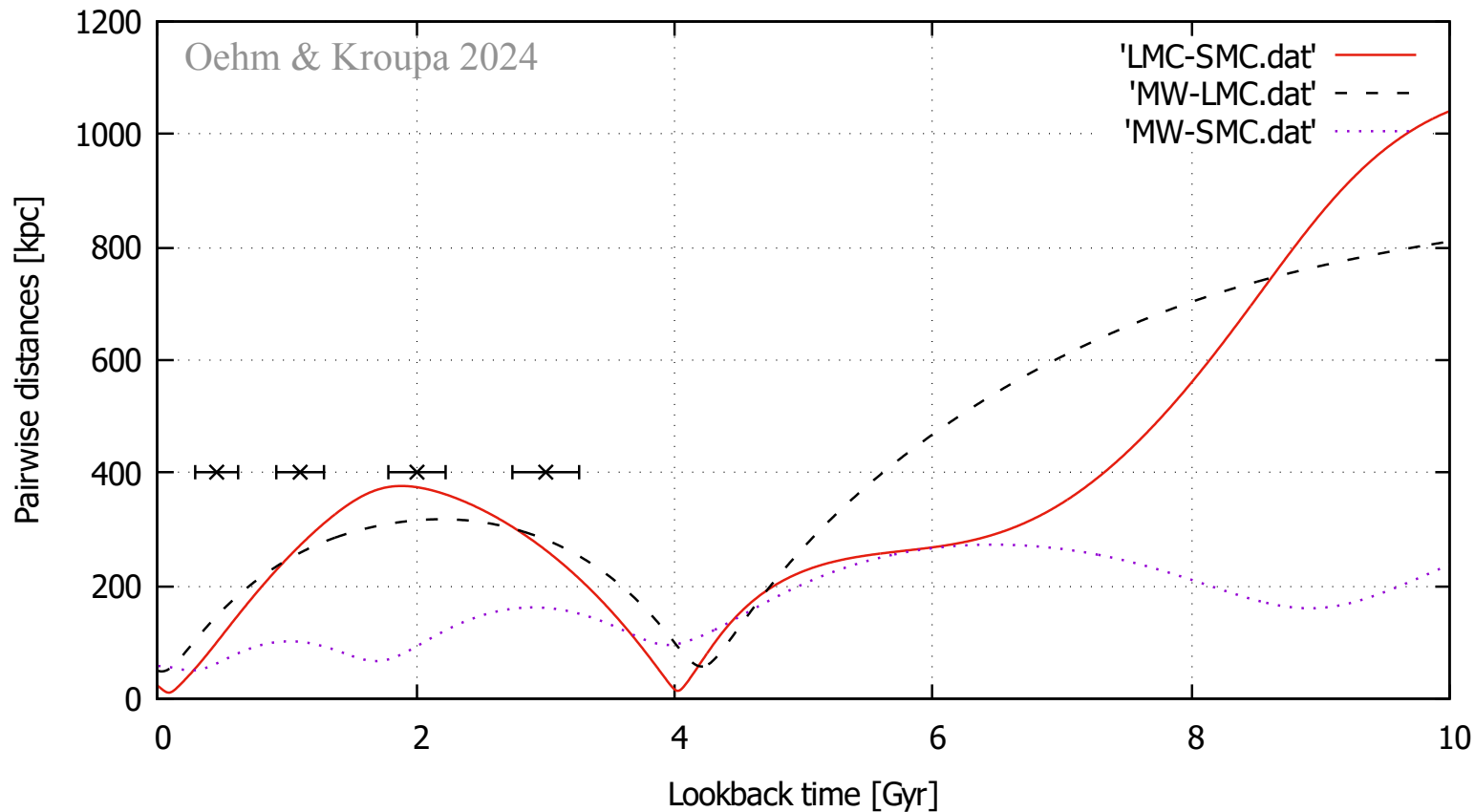
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MW-LMC-SMC with NFW profiles: Best fit solution / SFH history

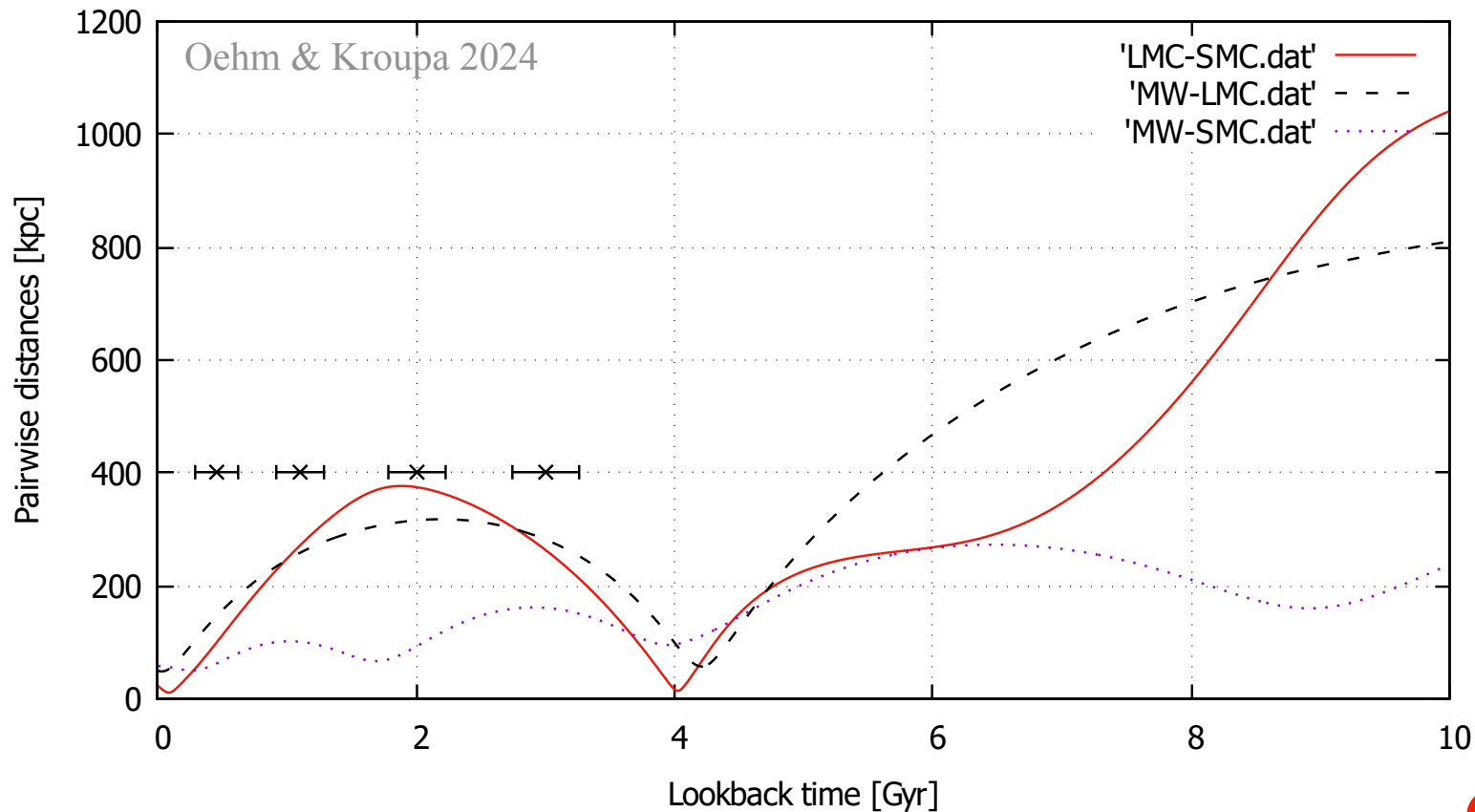


No solution of SMC-LMC orbit that explains the synchronised star-formation history.

A solution of the SMC / LMC / MW system is *not* possible in the SMOc.

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*no* dark matter halos

Testing for the existence  
of

Dark Matter

via

Chandrasekhar  
dynamical friction

With galaxy bars

# Chandrasekhar dynamical friction :

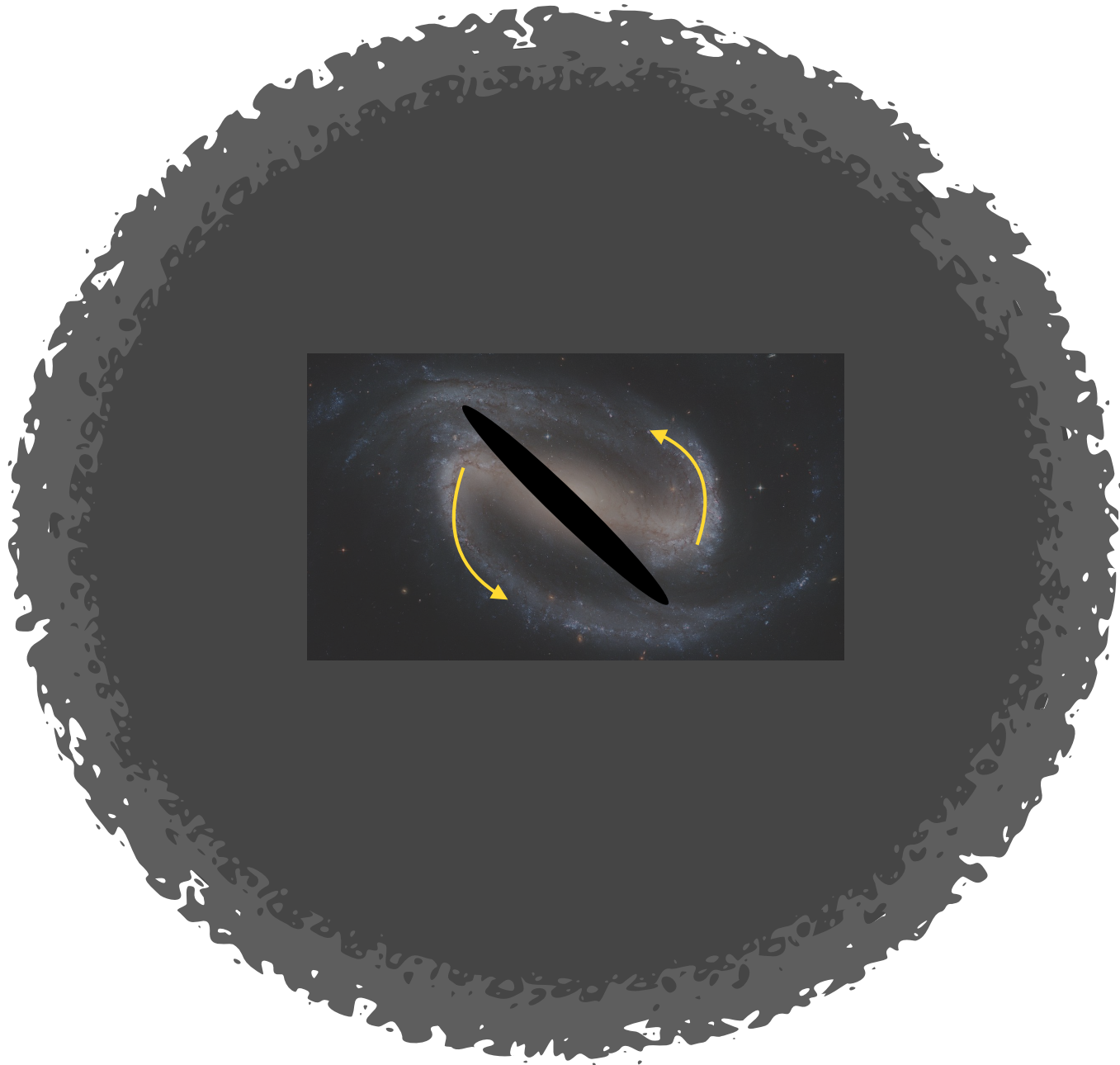
Bars slow down due to dynamical friction on DM halo





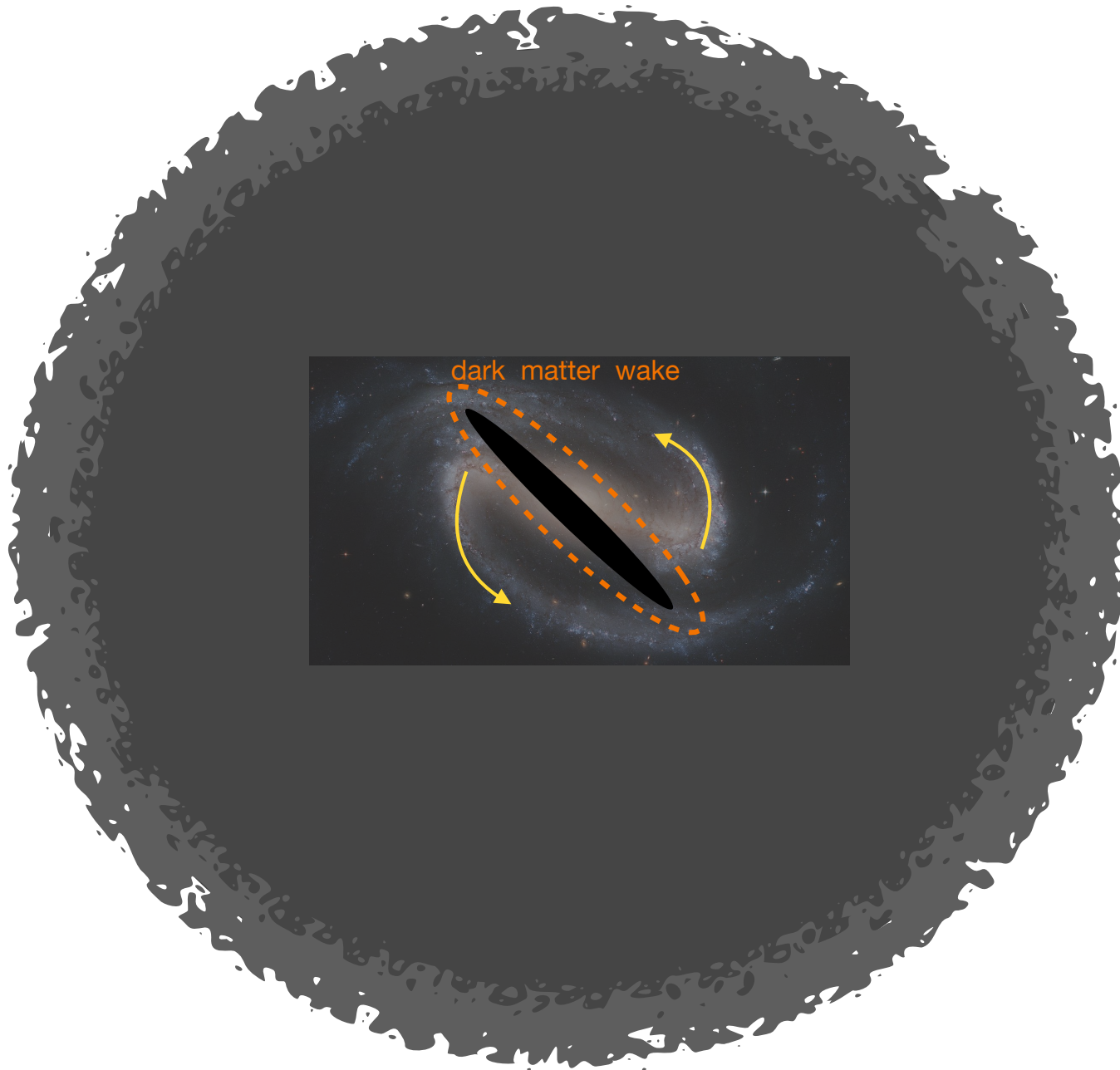
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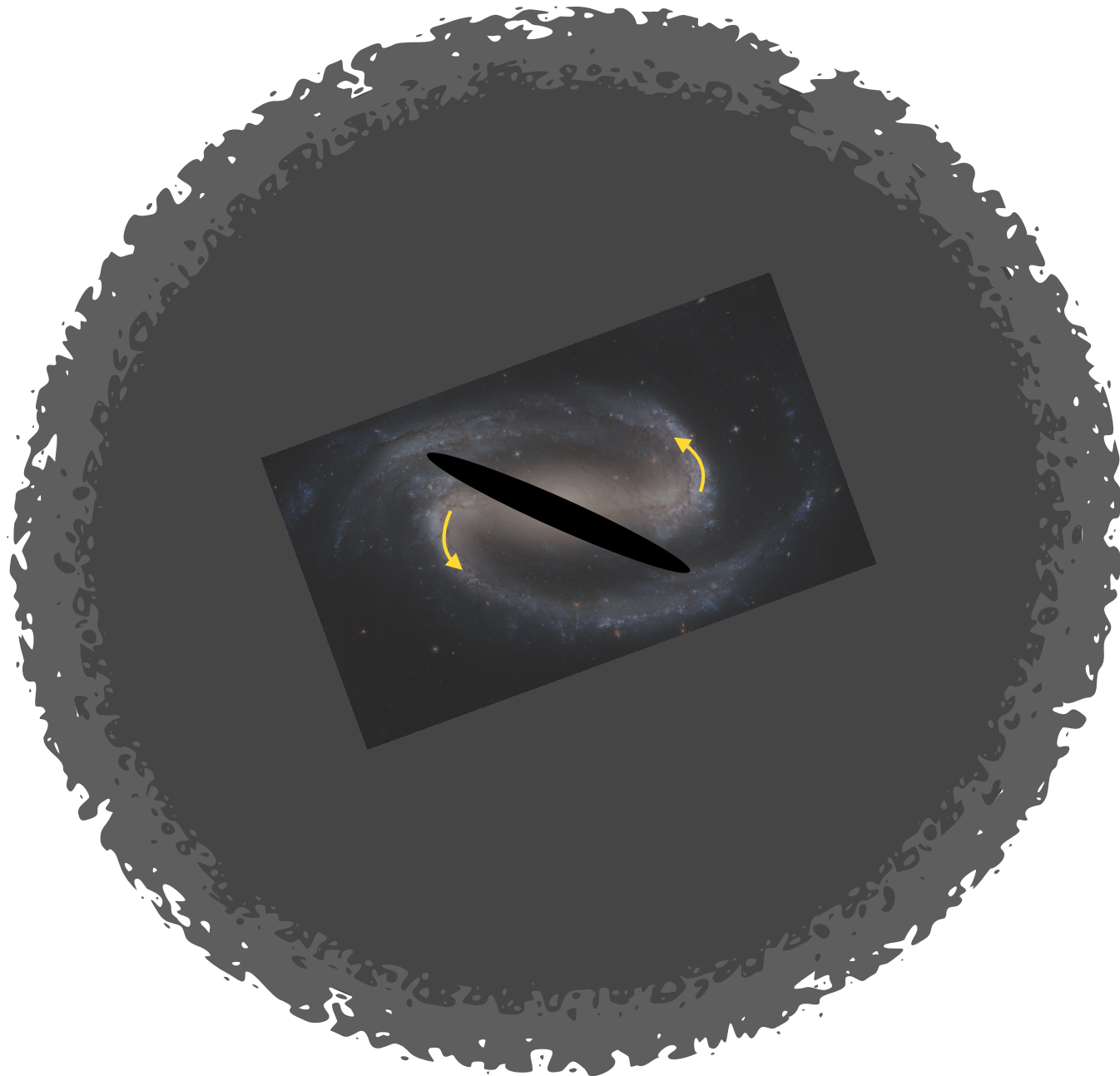
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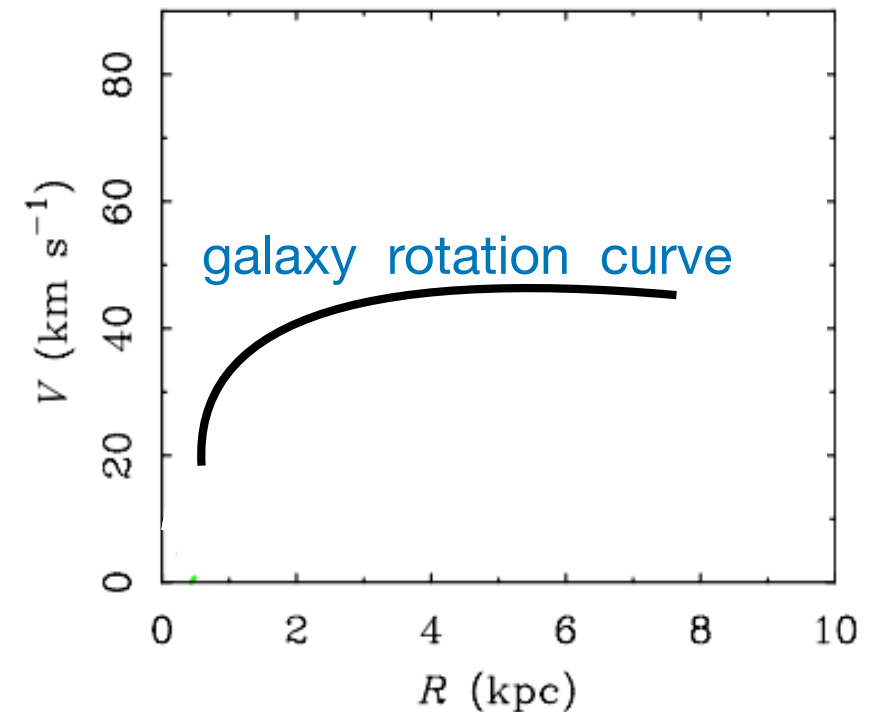
*If* dark matter halos exist,  
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# Chandrasekhar dynamical friction :

Bars slow down due to dynamical friction on DM halo

If dark matter halos exist,  
then bars *must* slow down

Bar rotates like rigid body,  
it's length thus is measure of  
rotation speed.



# Chandrasekhar dynamical friction :

Bars slow down due to dynamical friction on DM halo

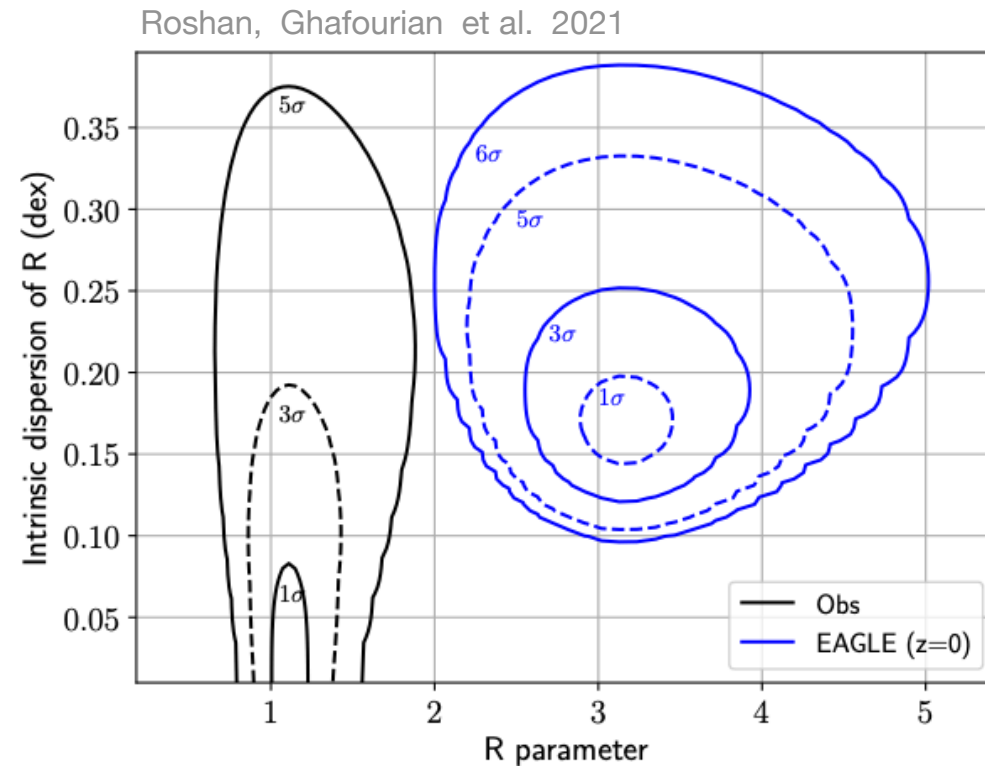
$$\mathcal{R} = \frac{R_{\text{corotation}}}{R_{\text{bar length}}}$$

$\mathcal{R} > 1.4 \Rightarrow$  slow bar

$\mathcal{R} < 1.4 \Rightarrow$  fast bar

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**Figure 19.** The posterior inference on  $\mathcal{R}$  and the intrinsic dispersion of  $\log_{10} \mathcal{R}$ , found by applying Equation 28 to our compilation of observational results (Table 2) and to the EAGLE simulation at  $z = 0$  based on figure 9 of Algorry et al. (2017). Although the calculations are done in the space of  $\log_{10} \mathcal{R}$ , we change the  $x$ -axis to a linear scale when plotting so the results are more intuitive (i.e. we plot  $10^{\overline{\mathcal{R}}}$ ). The black (blue) contours correspond to  $1\sigma$ ,  $3\sigma$ , and  $5\sigma$  outliers from the observed (EAGLE) posterior. Due to the significant mismatch, the  $6\sigma$  contour is also shown for the EAGLE simulation.

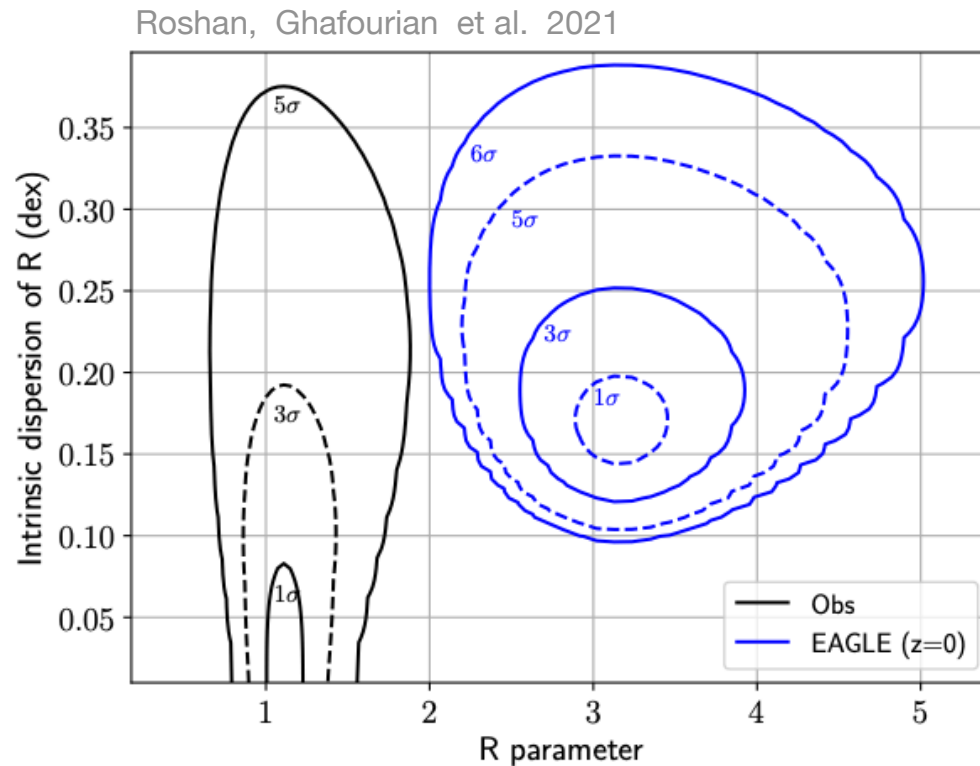
# Chandrasekhar dynamical friction :

Bars slow down due to dynamical friction on DM halo

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$\mathcal{R} > 1.4 \Rightarrow$  slow bar

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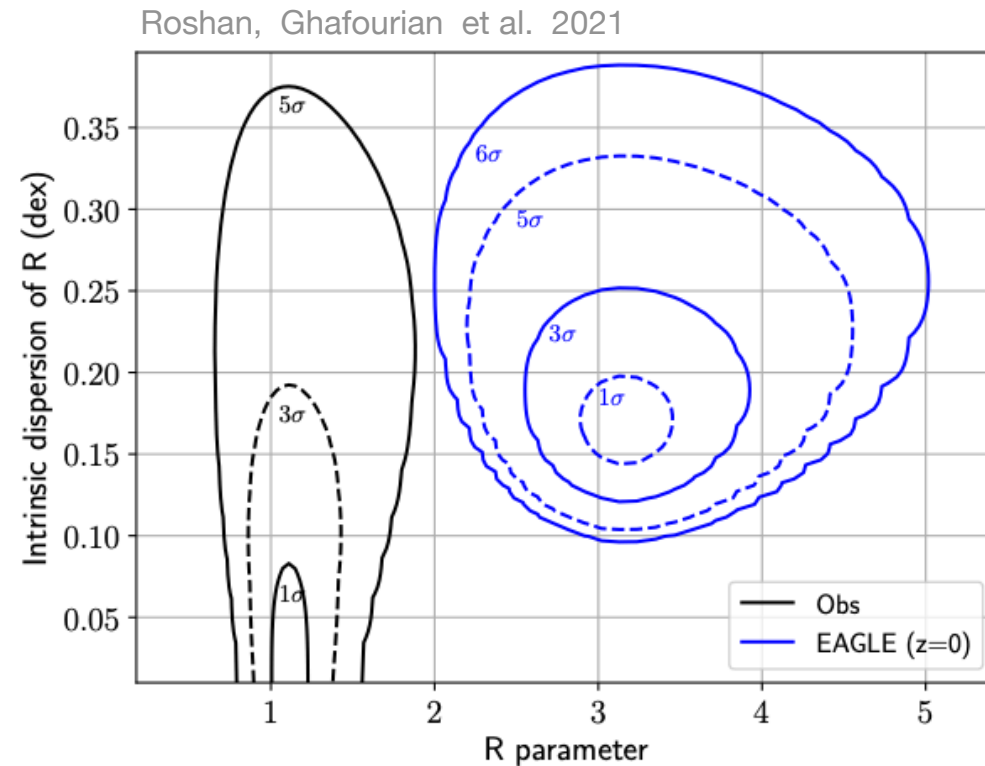


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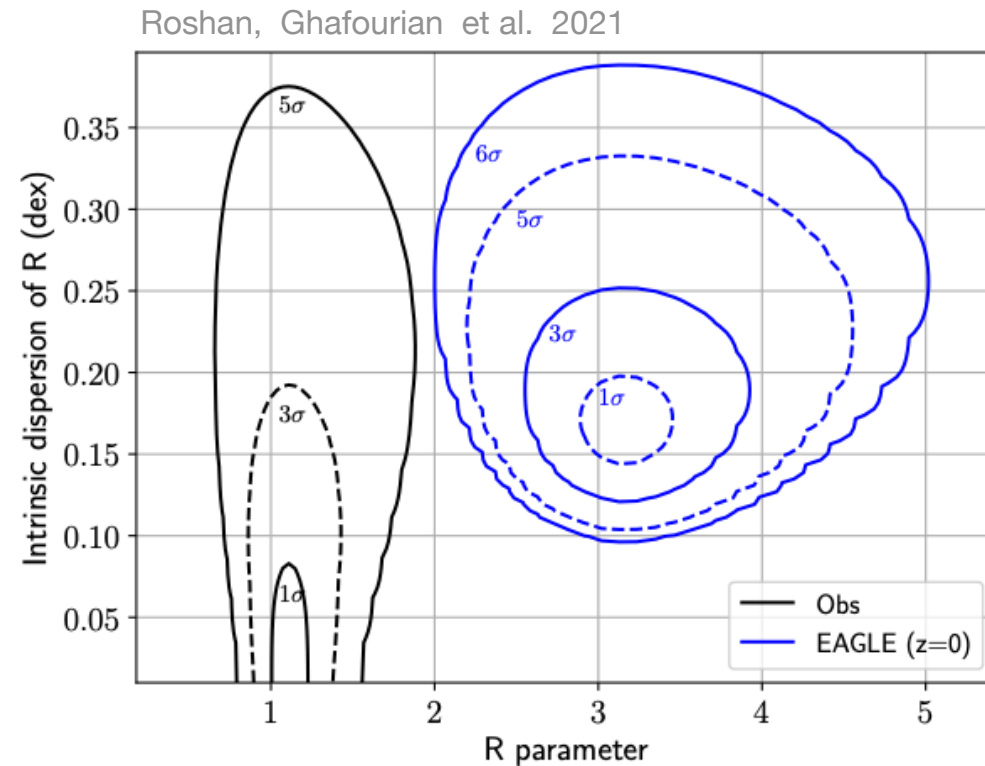
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8 sigma tension

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no significant dark matter halo in nature

Thus, other applications of  
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The bars of galaxies are too long



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Roshan, Ghafourian et al. 2021





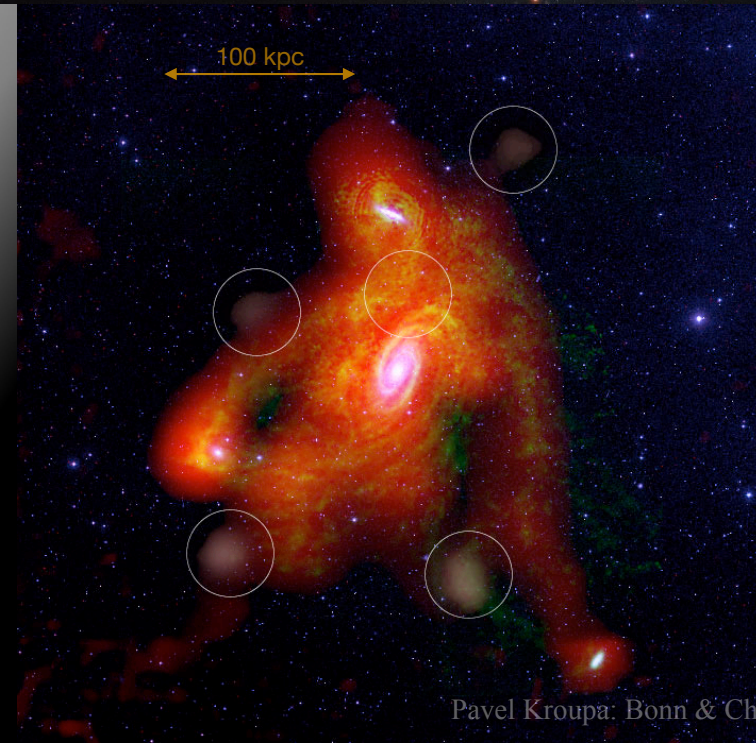
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The observed configuration of  
the M81 group of galaxies  
*cannot exist* in the SMOc

Yun 1999  
Thomson, Laine & Turnbull 1999  
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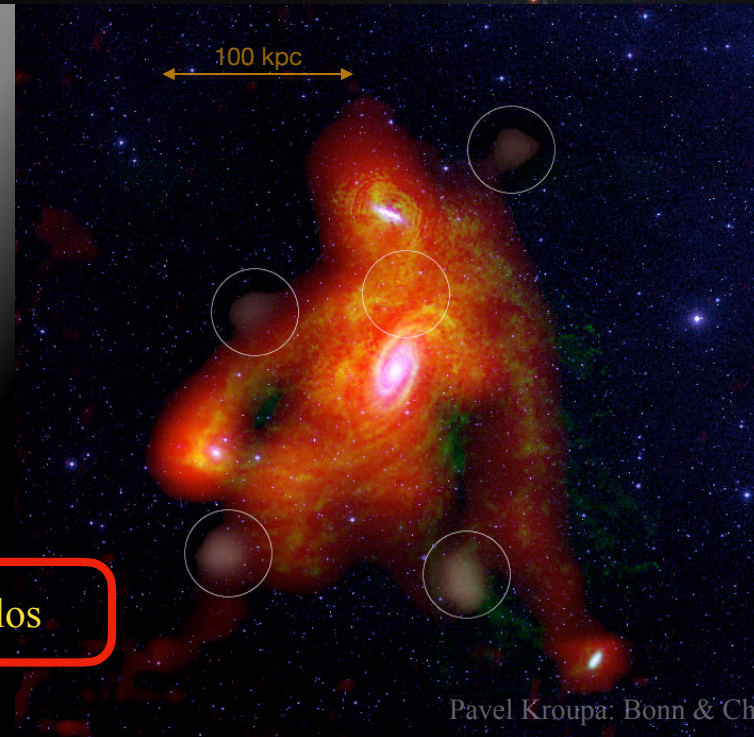
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no dark matter halos

# Chandrasekhar dynamical friction :

All tests performed demonstrate

with  $\gg 5$  sigma confidence

that dark matter halos  
made of particles  
of any mass  
are ruled out.

Other tests,  
**not** based  
on  
Chandrasekhar dynamical  
friction

If there is no C/W dark matter,

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no ?

$$\dot{M}_{\text{cluster}} < 0$$

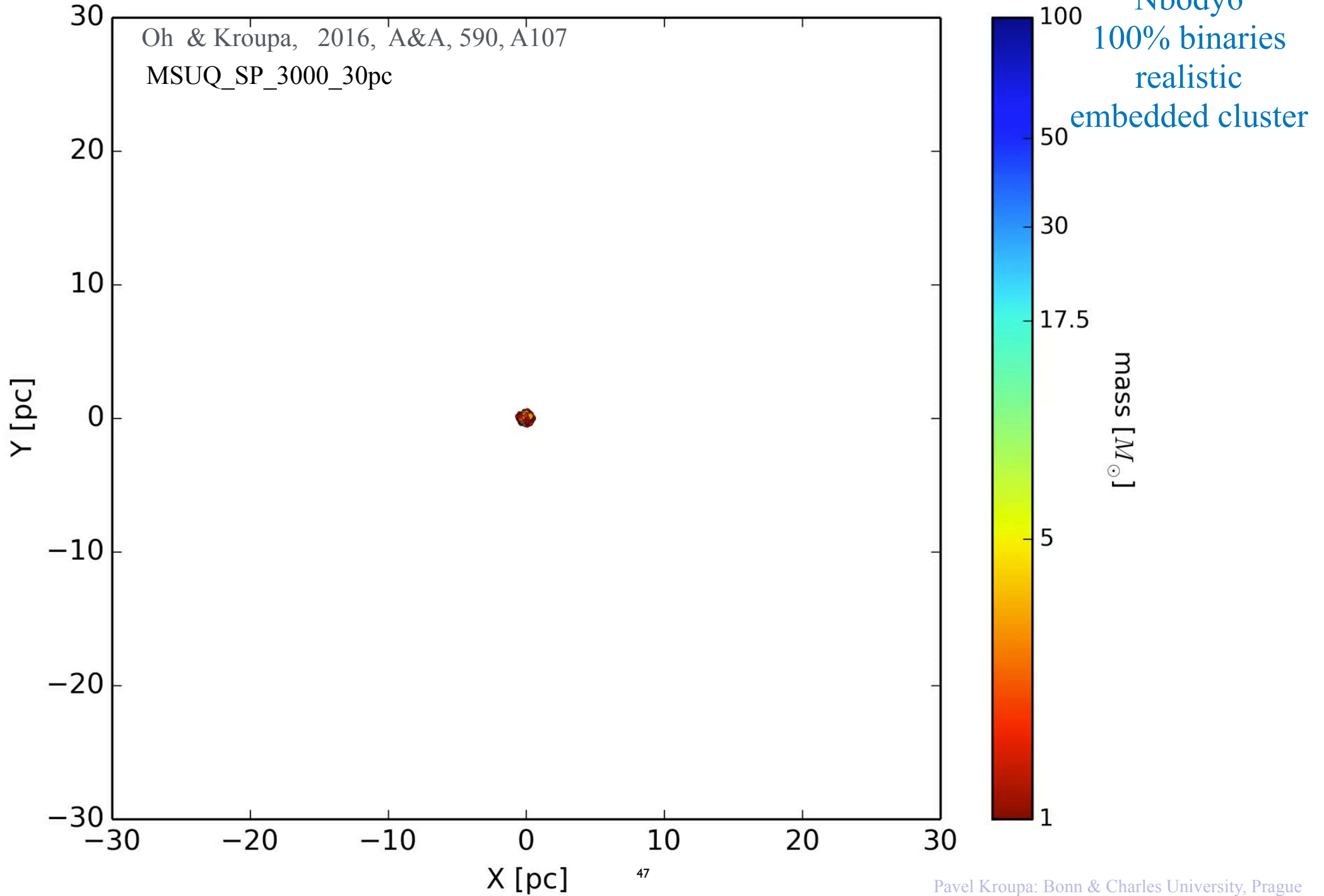
Open star clusters  
as tests of  
gravitational theory

# Open star clusters as tests of gravitational theory

How do star clusters loose their stars ?

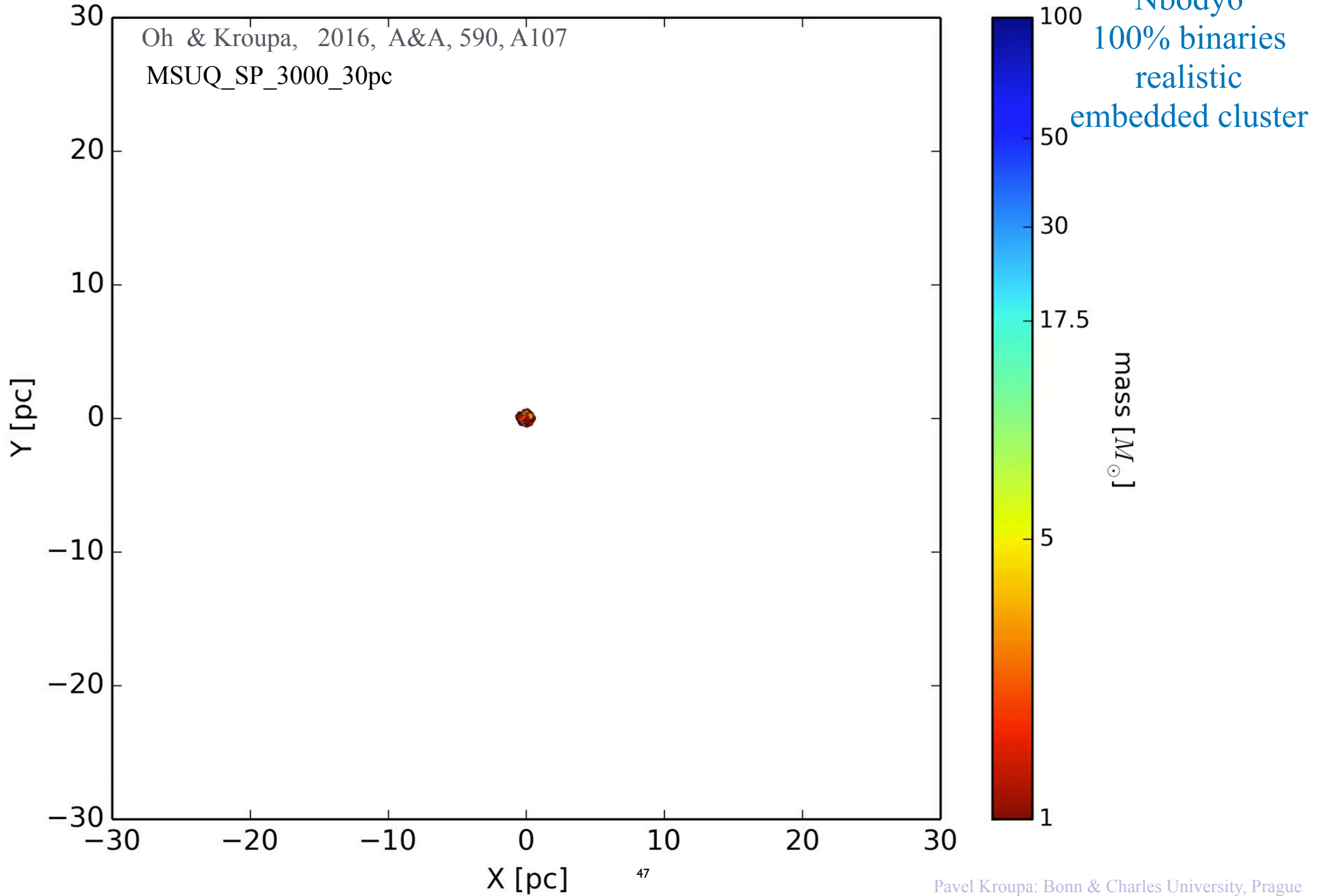
# Ejection

0.000 Myr



# Ejection

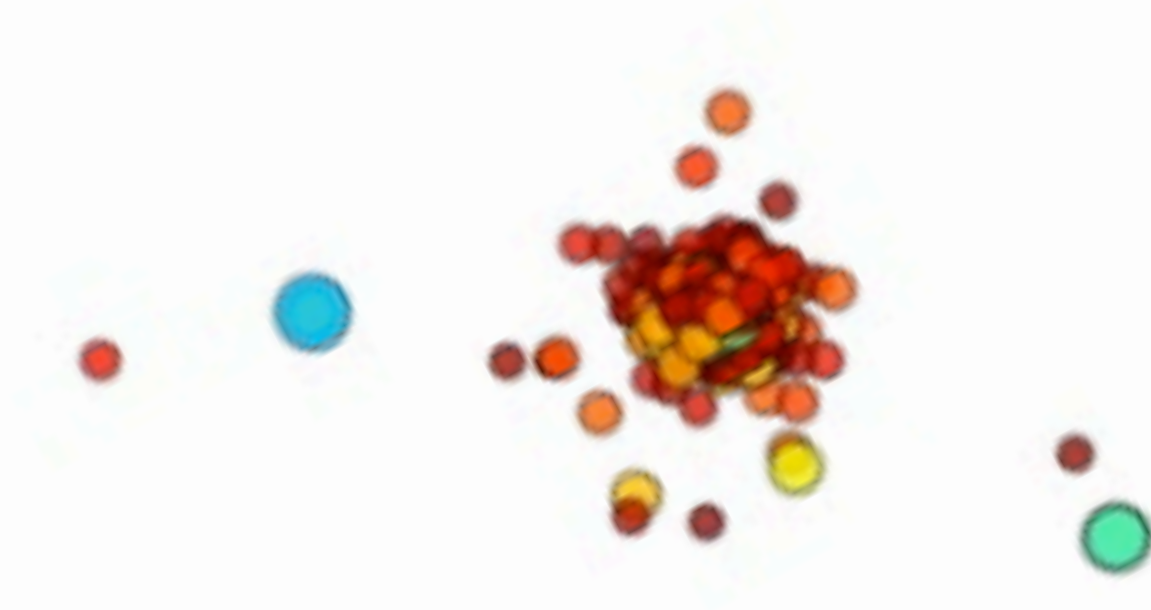
0.000 Myr



# *Ejection*

Oh & Kroupa, 2016, A&A, 590, A107

MSUQ\_SP\_3000\_30pc Nbody models



# Monoceros R2 cluster

(Carpenter et al. 1997, AJ 114, 198)



# *Evaporation*

*Assume*, for simplicity : the cluster consists of single stars of equal mass  $m$ .



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At a given radius  $r$  in the cluster the stars have, approximately, a *Maxwell-Boltzmann* distribution of speeds :

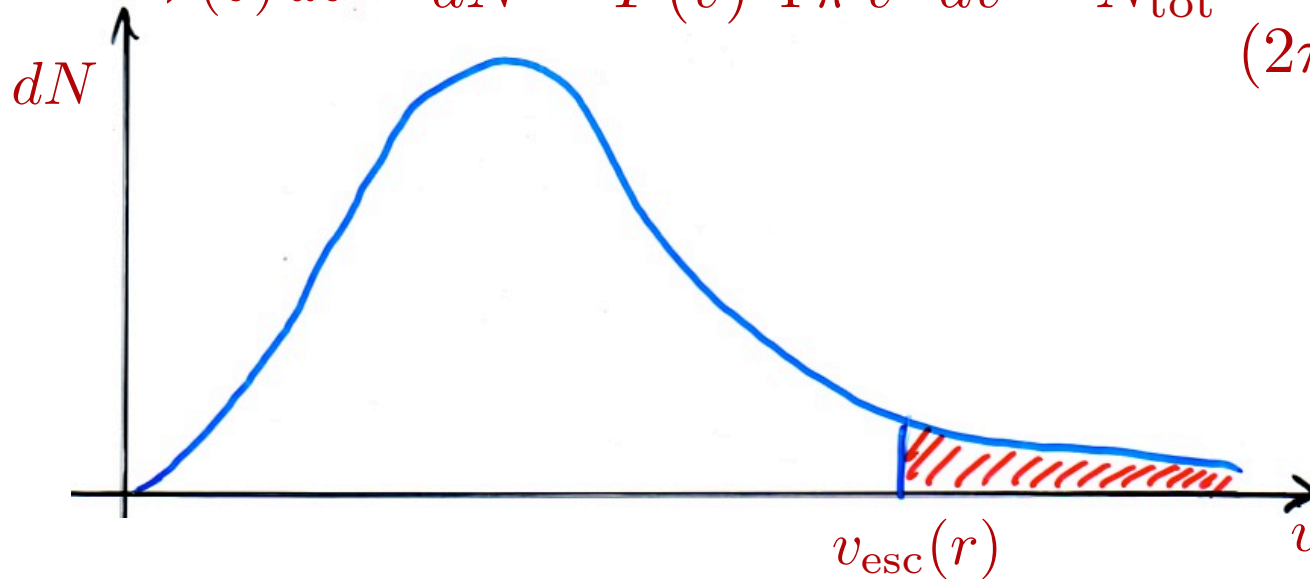
$$\mathcal{V}(v) dv = dN = F(v) 4\pi v^2 dv = N_{\text{tot}} \frac{1}{(2\pi\sigma^2)^{\frac{3}{2}}} e^{-\frac{v^2}{2\sigma^2}} 4\pi v^2 dv$$

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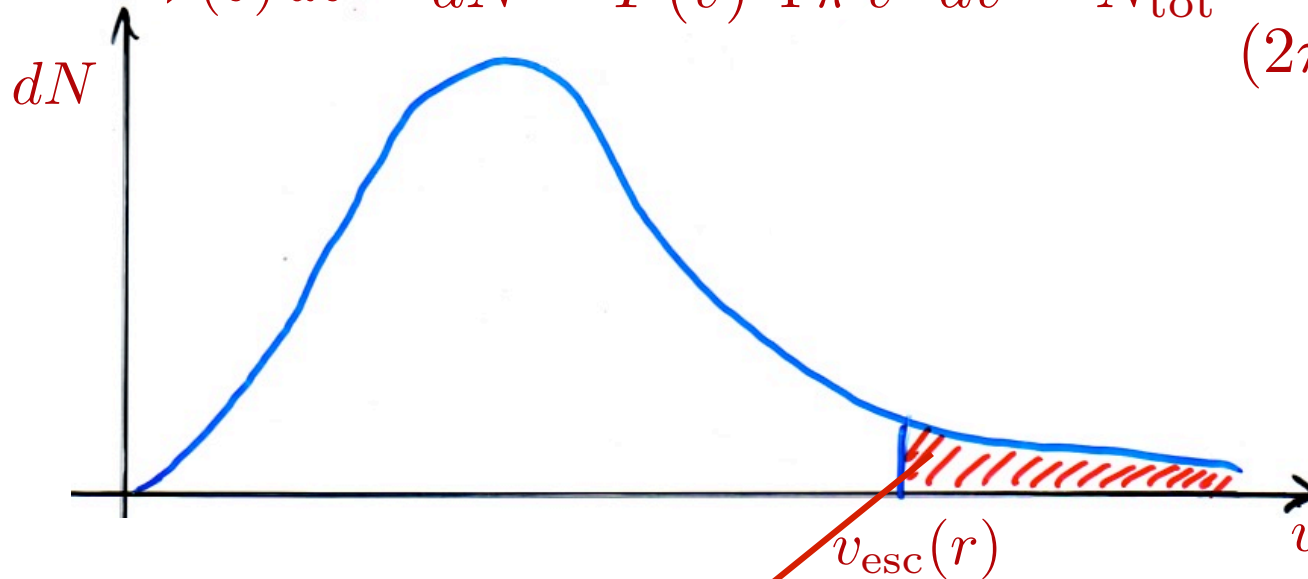


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$$\frac{dM_{\text{cl}}}{dt}(t) = m \frac{dN}{dt}(t)$$

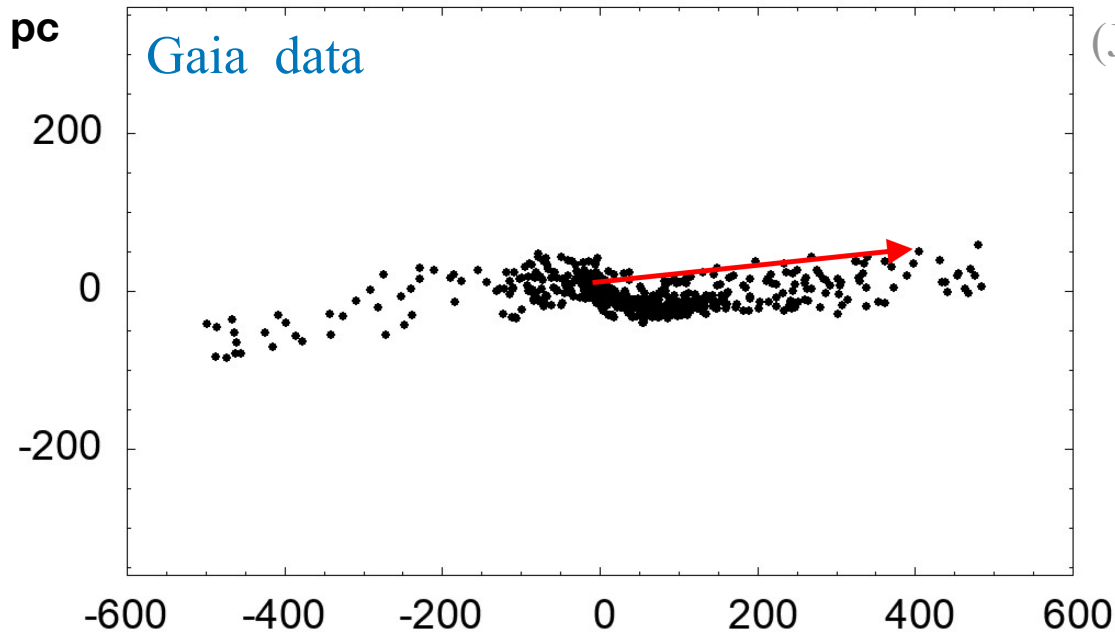
Evaporated stars  
leave their  
open clusters  
through  
tidal tails

New method developed by Tereza Jerabkova in 2021  
allowing *the tidal tails of open clusters* to be mapped  
to their tips.

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The Jerabkova Compact Convergent Point (CCP) method.

(Jerabkova et al. 2021)

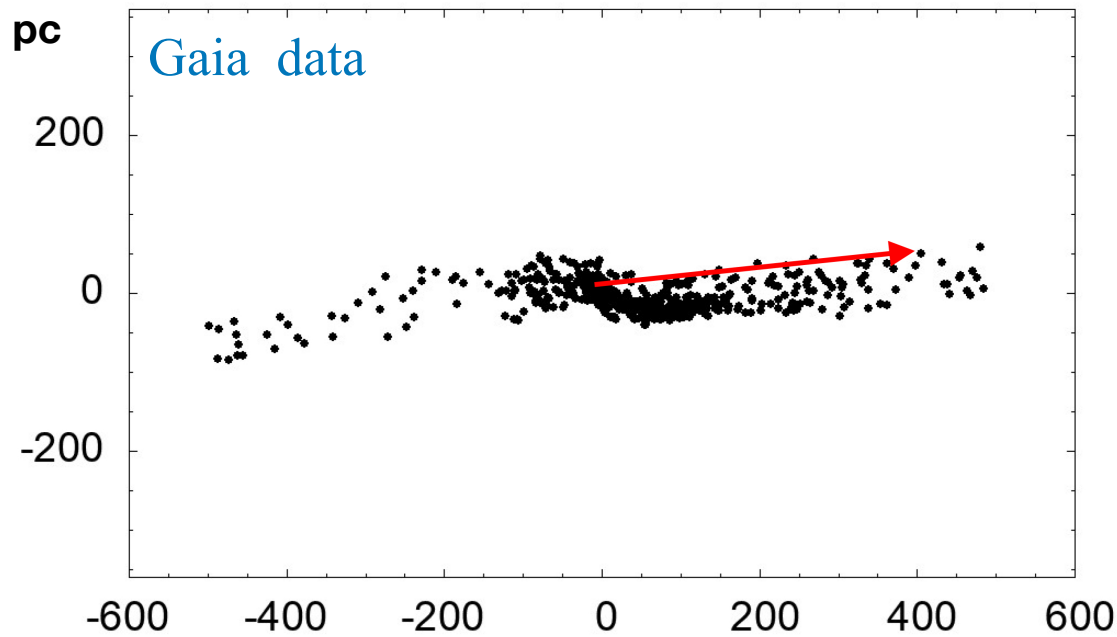


(Jerabkova et al. 2021)

# Hyades

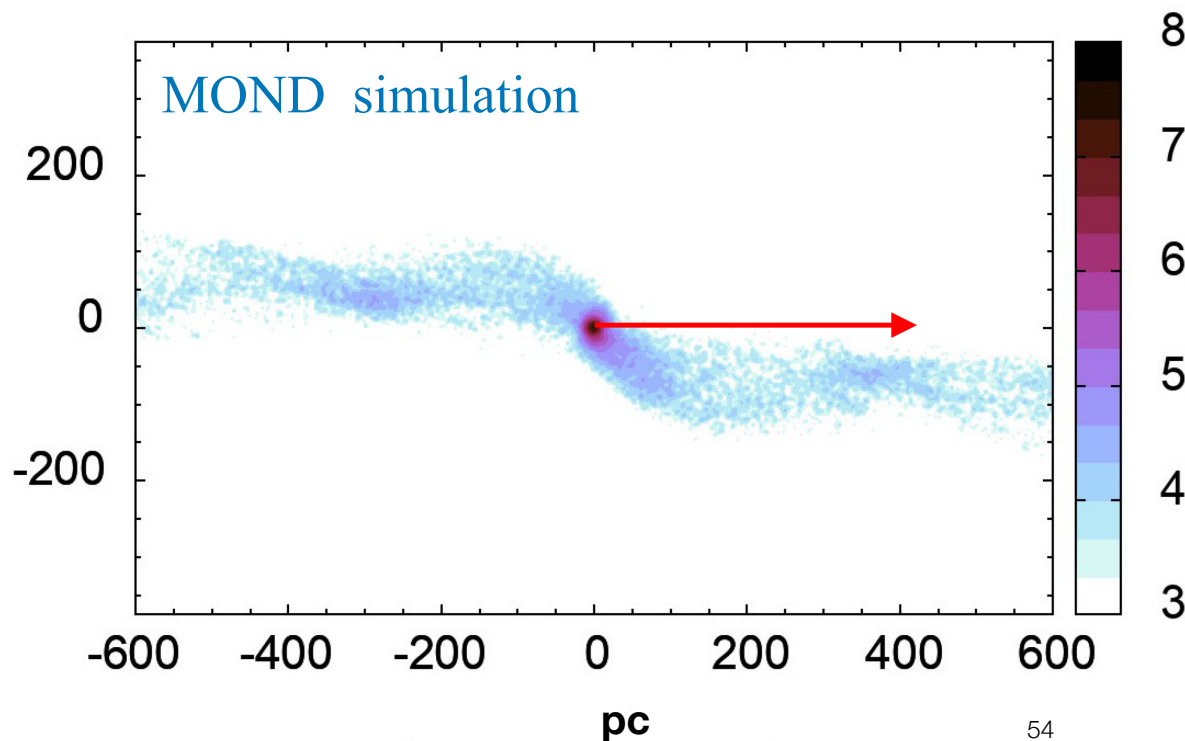
(Kroupa, Jerabkova et al. 2022)

The asymmetry in  
number of stars  
between leading and trailing tail  
is a **6.5sigma** deviation  
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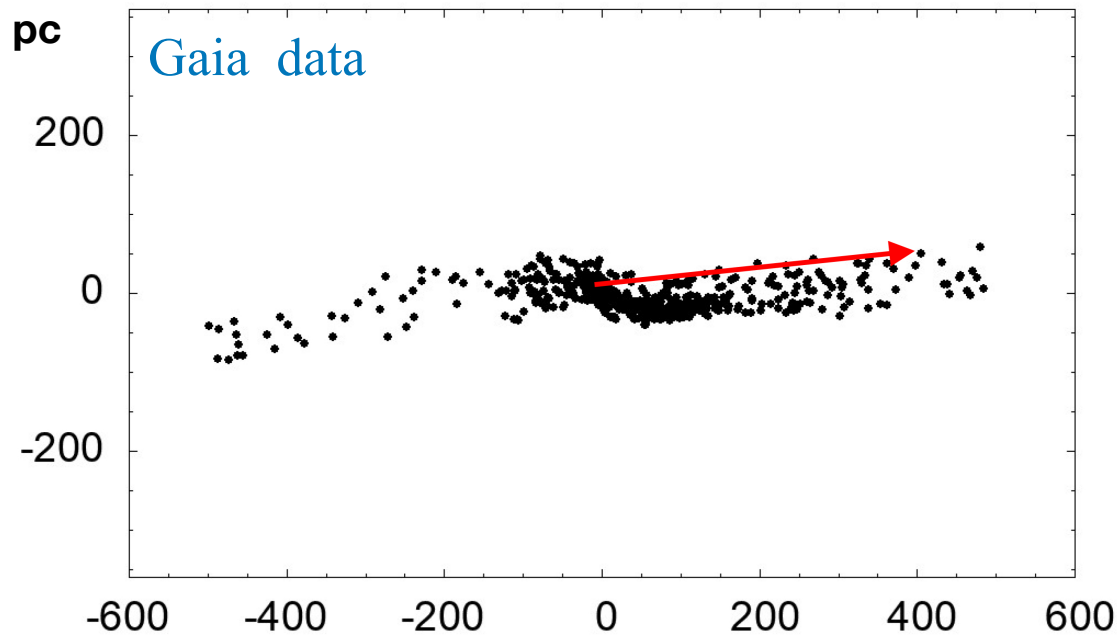
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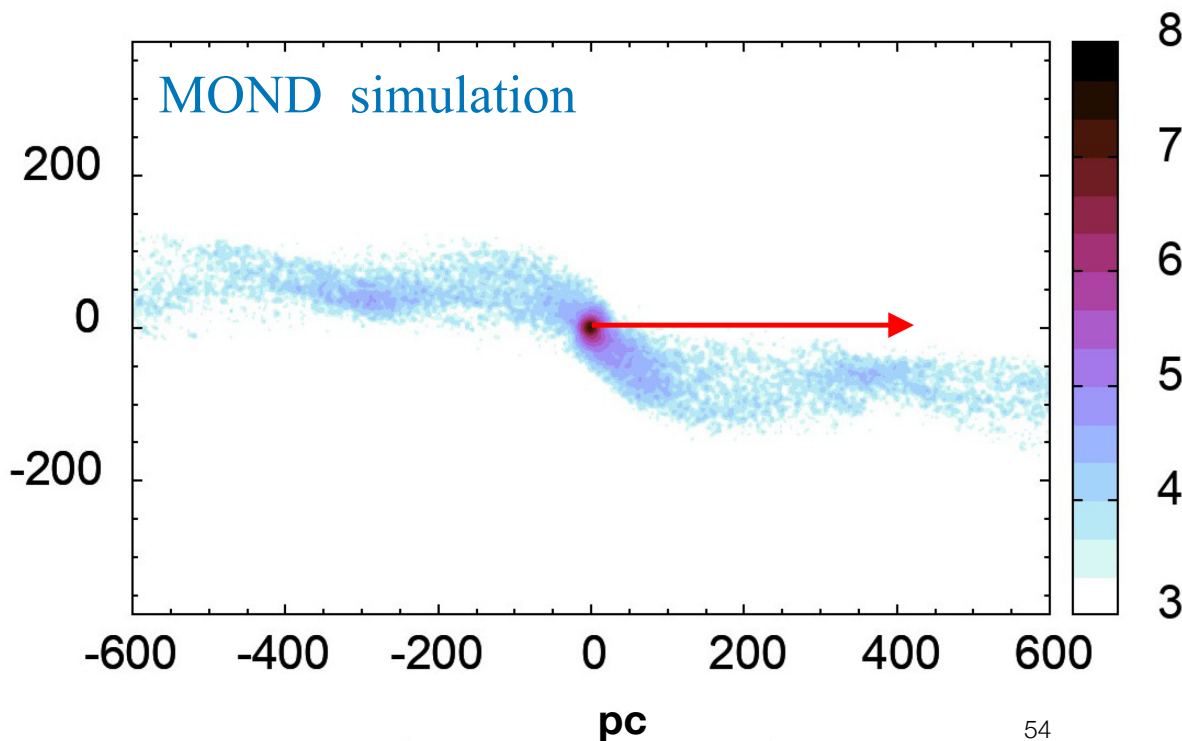
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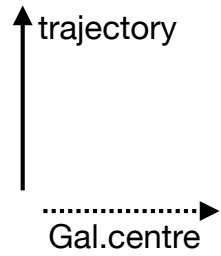
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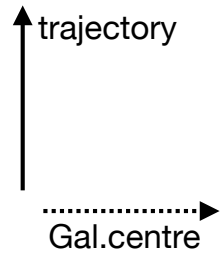
# Evaporation in Newtonian and Milgromian gravitation



(Kroupa, Jerabkova et al. 2022)

open star cluster

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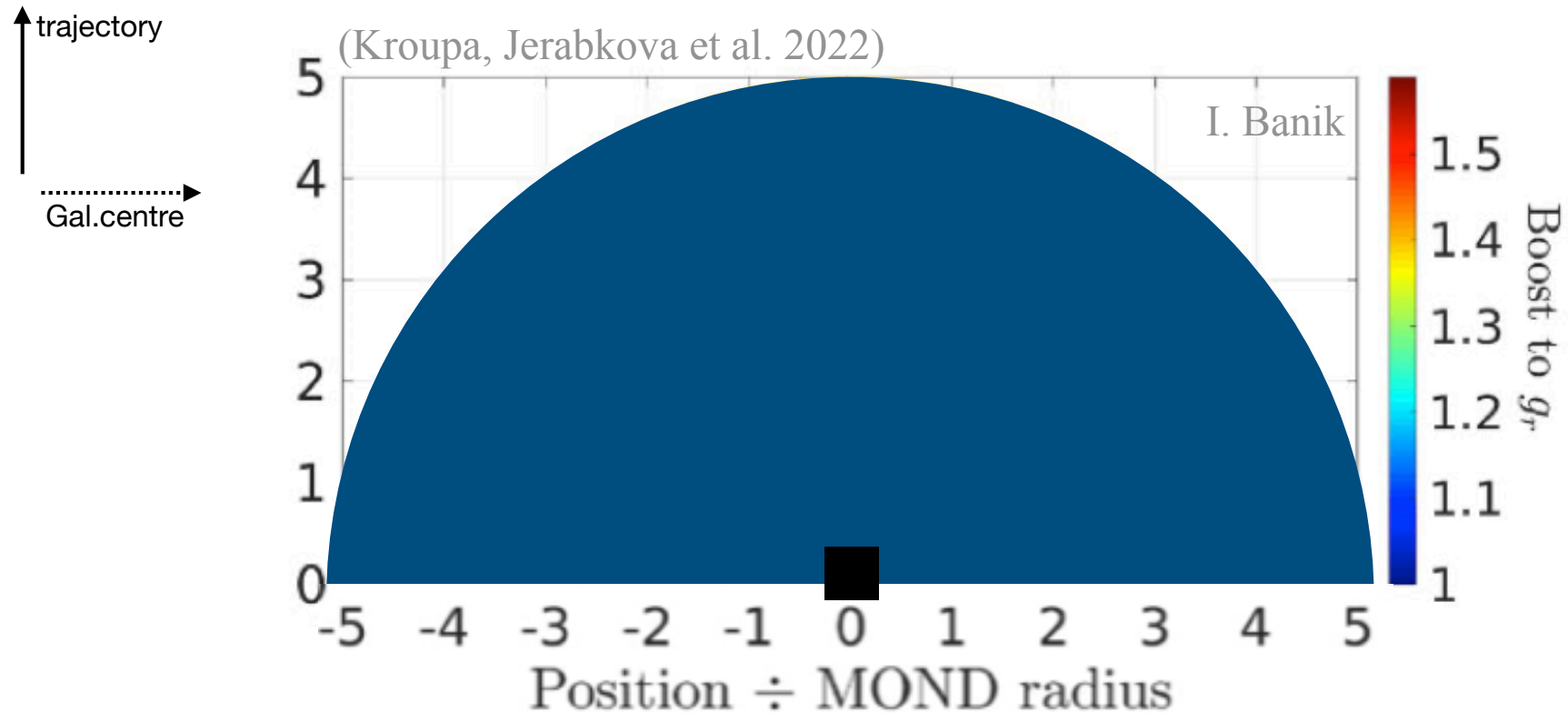
(Kroupa, Jerabkova et al. 2022)

■  
open star cluster

MOND radius :

$$r_M = \left( \frac{G M_{oc}}{a_0} \right)^{\frac{1}{2}}$$

# Newtonian case

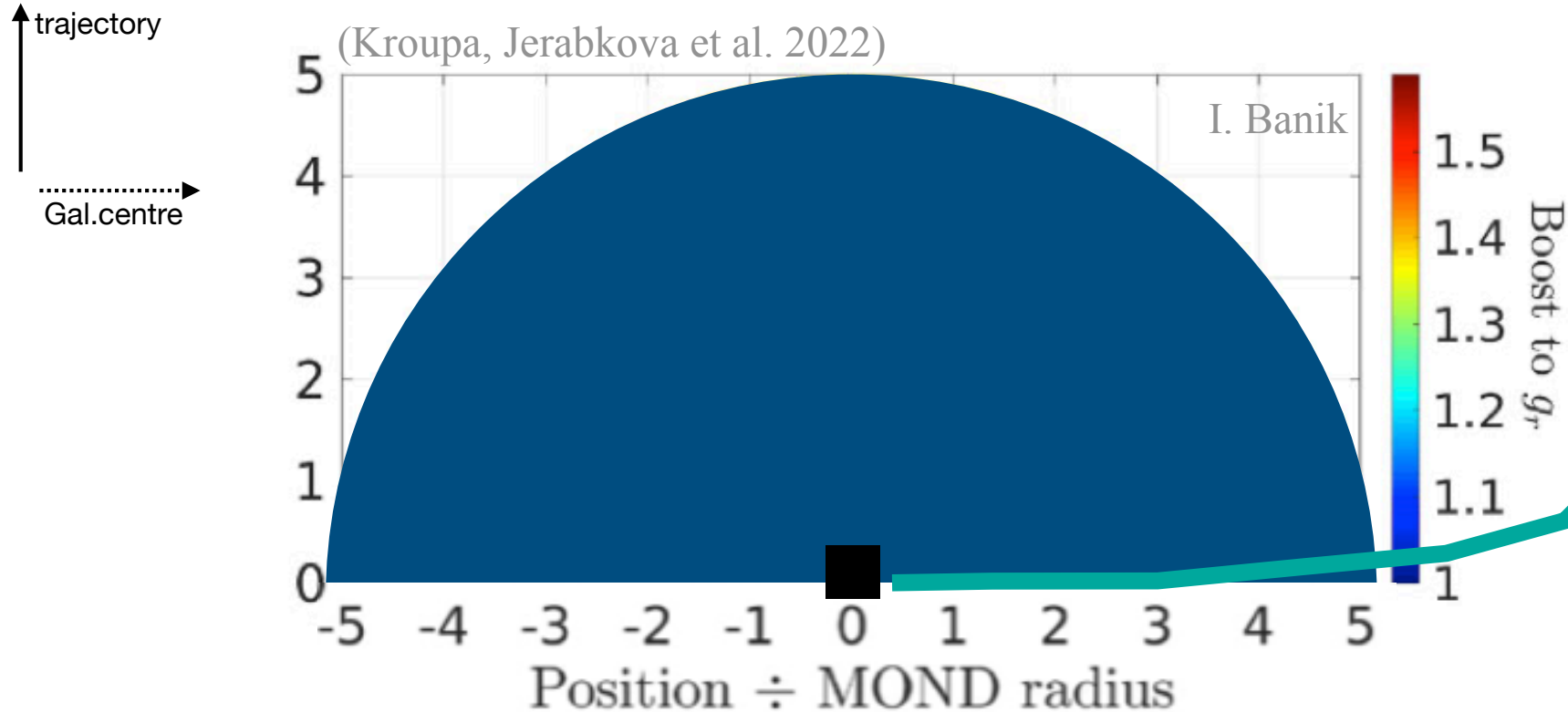


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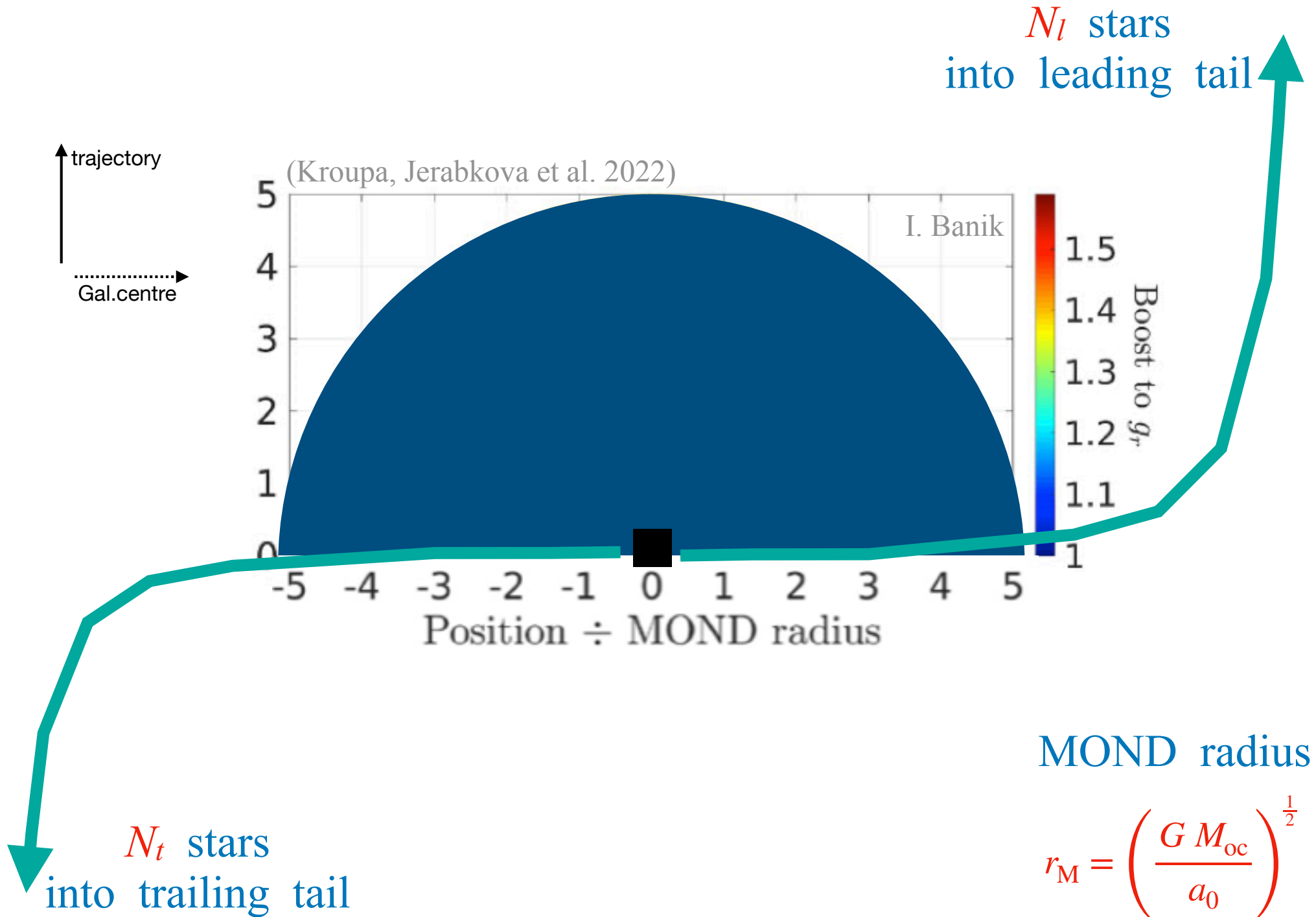
$N_l$  stars  
into leading tail



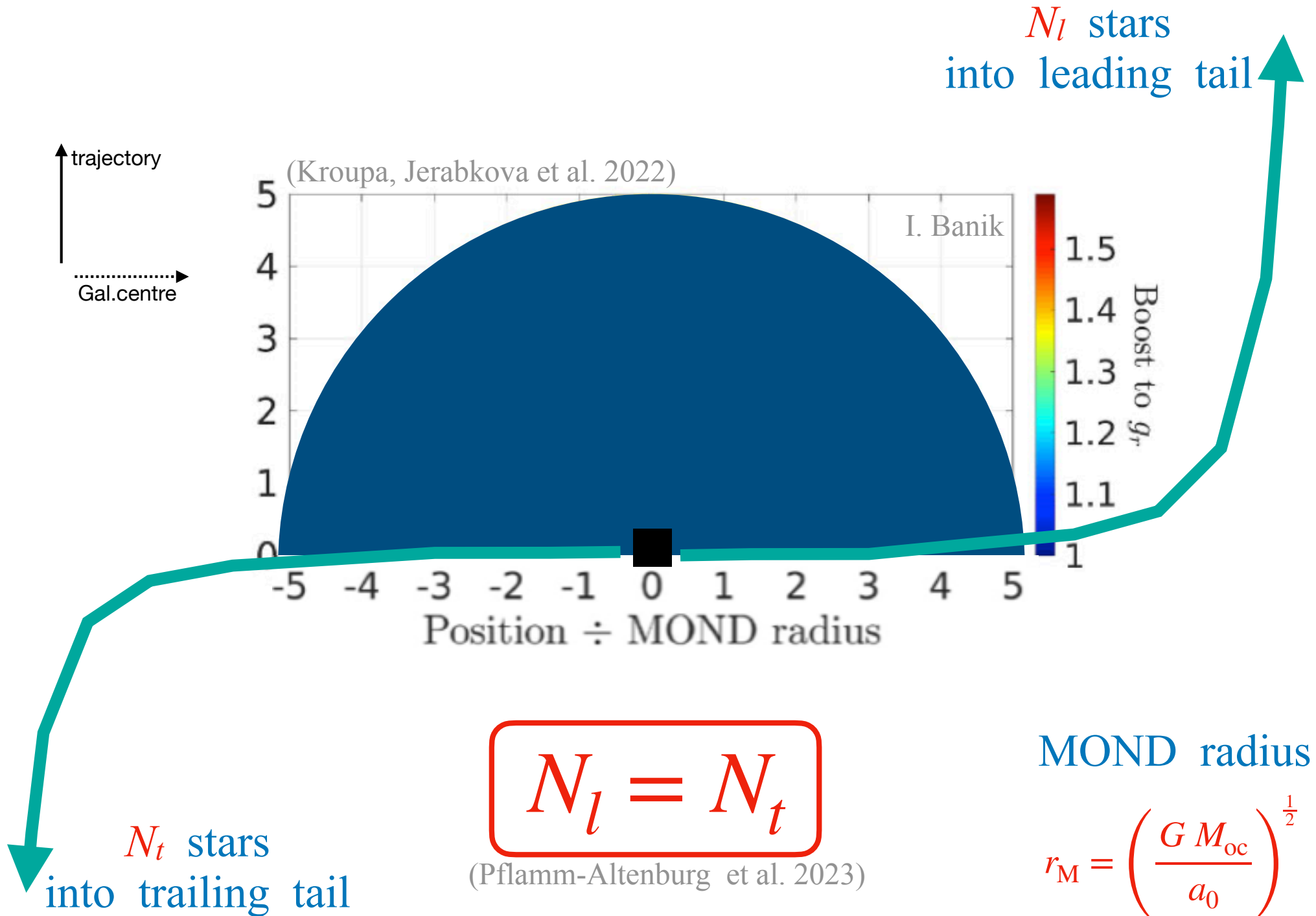
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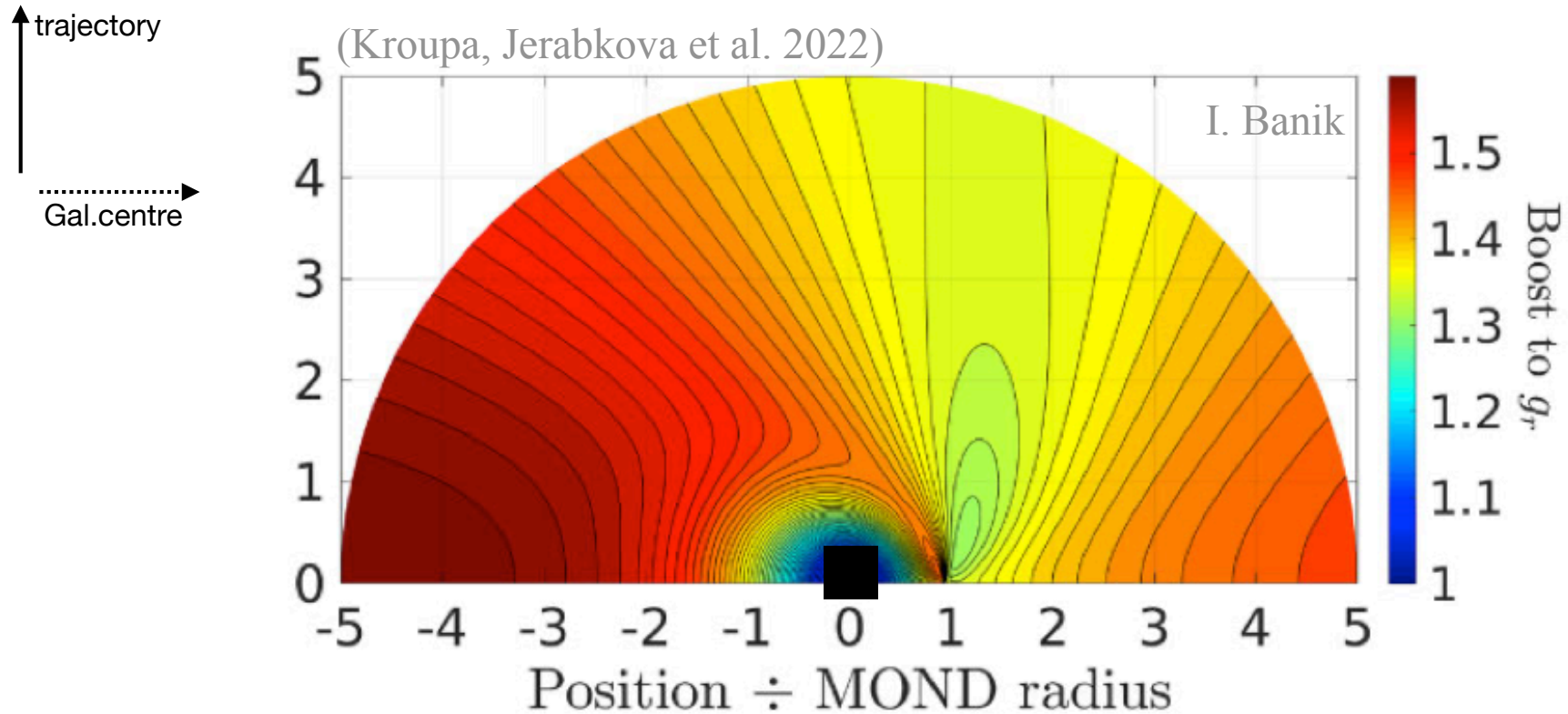


# Newtonian case



# MOND predictions

*of new phenomena*



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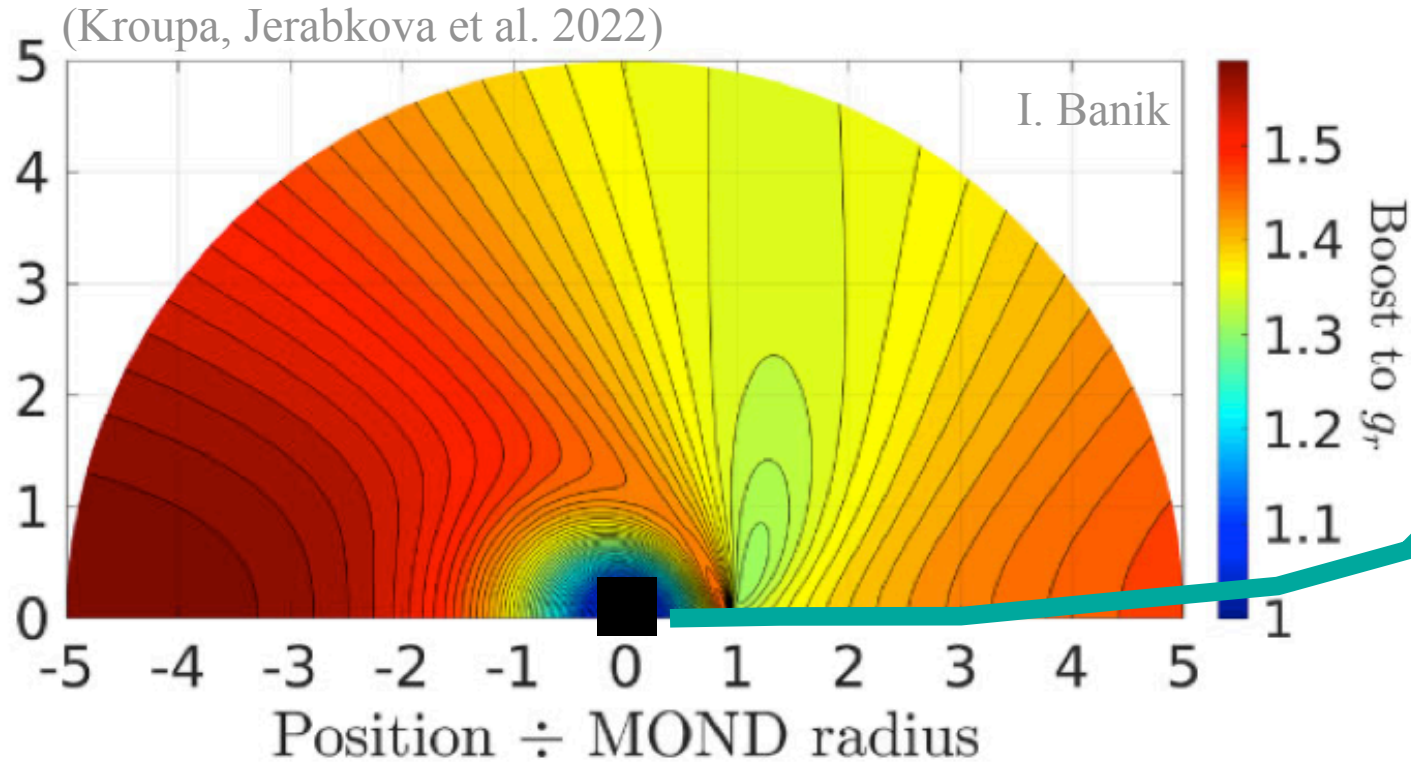


# MOND predictions

of new phenomena

$N_l$  stars  
into leading tail

↑ trajectory  
→ Gal. centre



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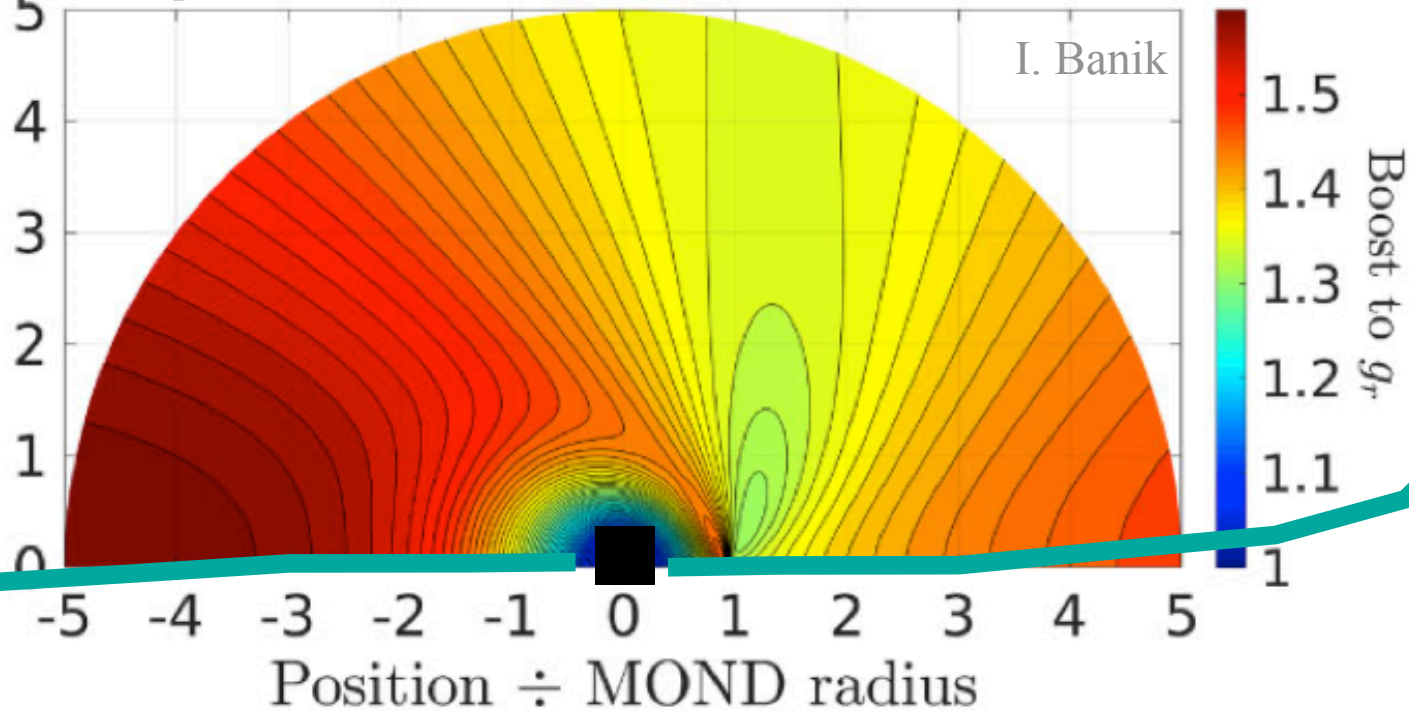
$N_l$  stars  
into leading tail

trajectory

Gal. centre

(Kroupa, Jerabkova et al. 2022)

I. Banik



$N_t$  stars  
into trailing tail

MOND radius :

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# MOND predictions

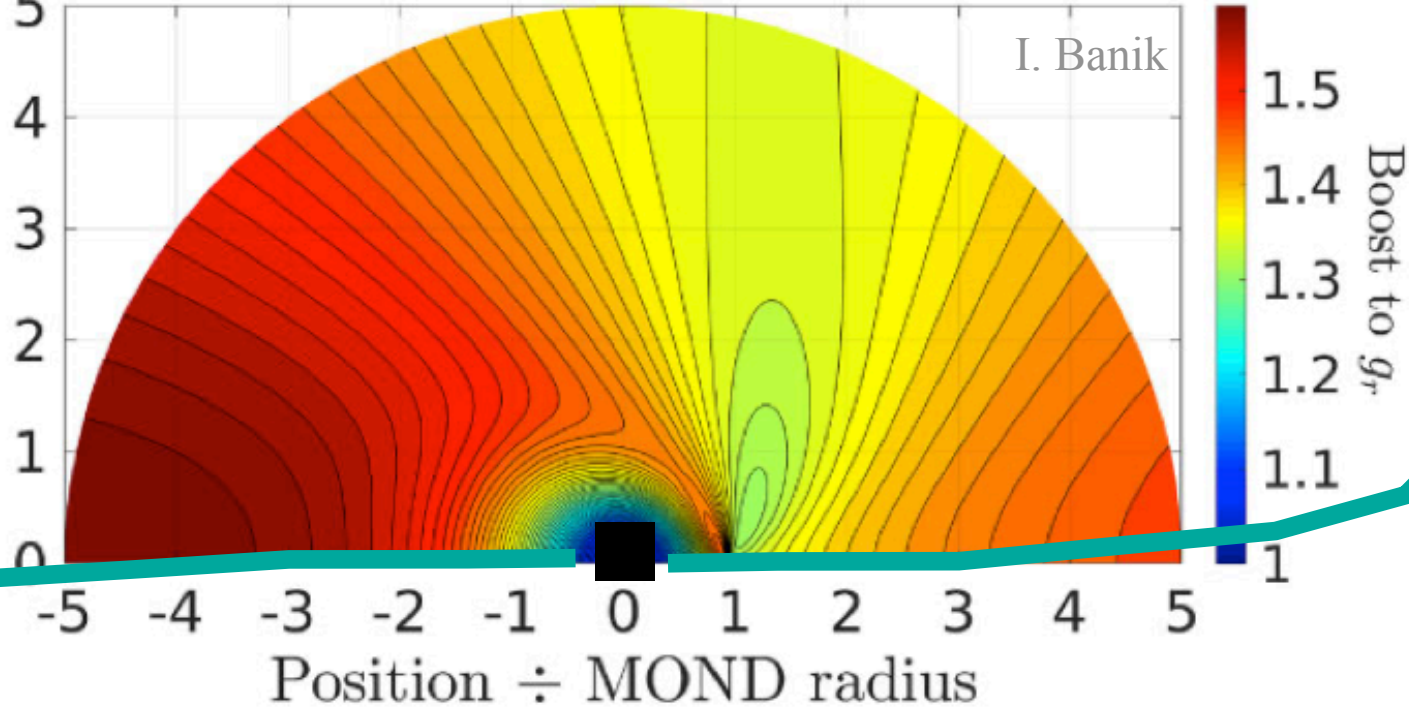
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Gal. centre

(Kroupa, Jerabkova et al. 2022)



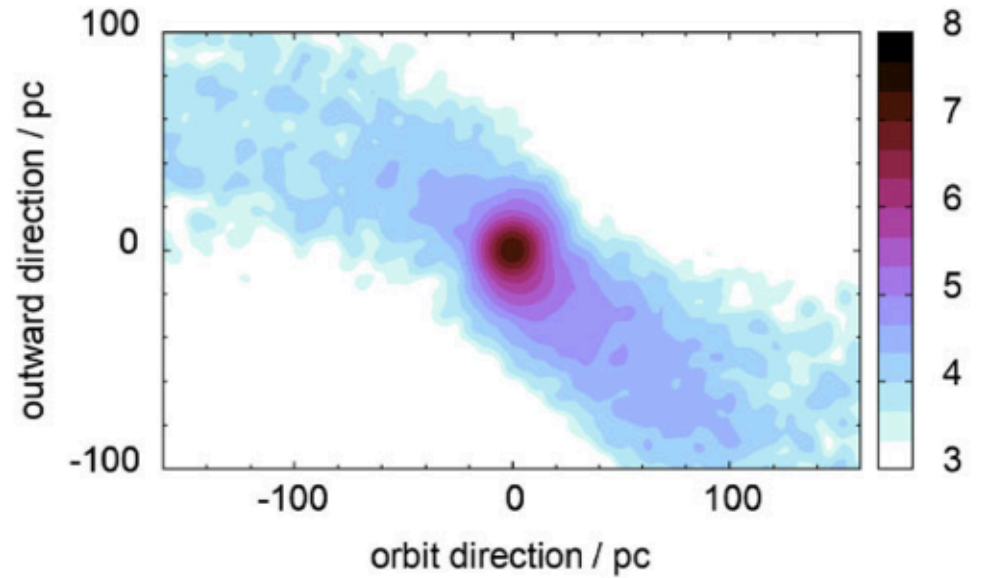
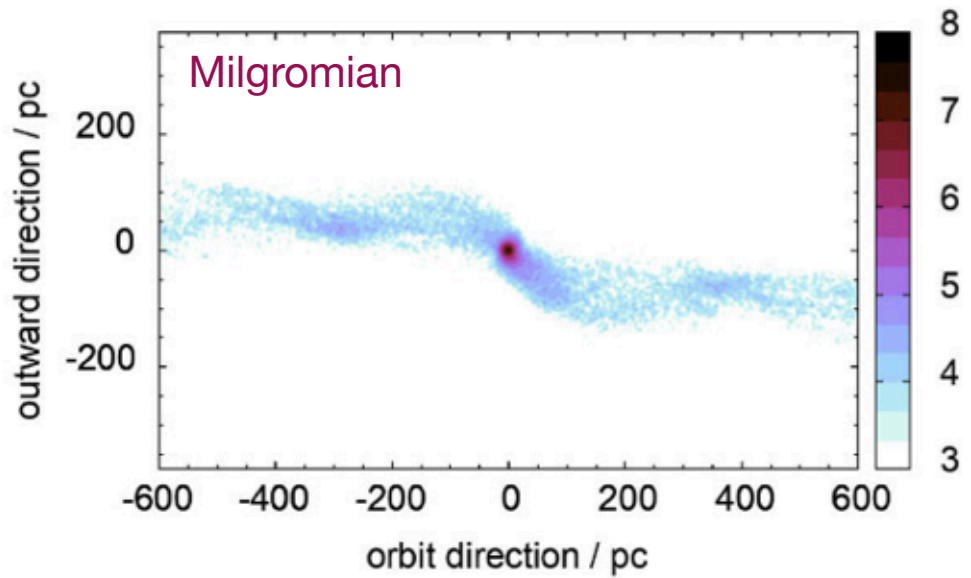
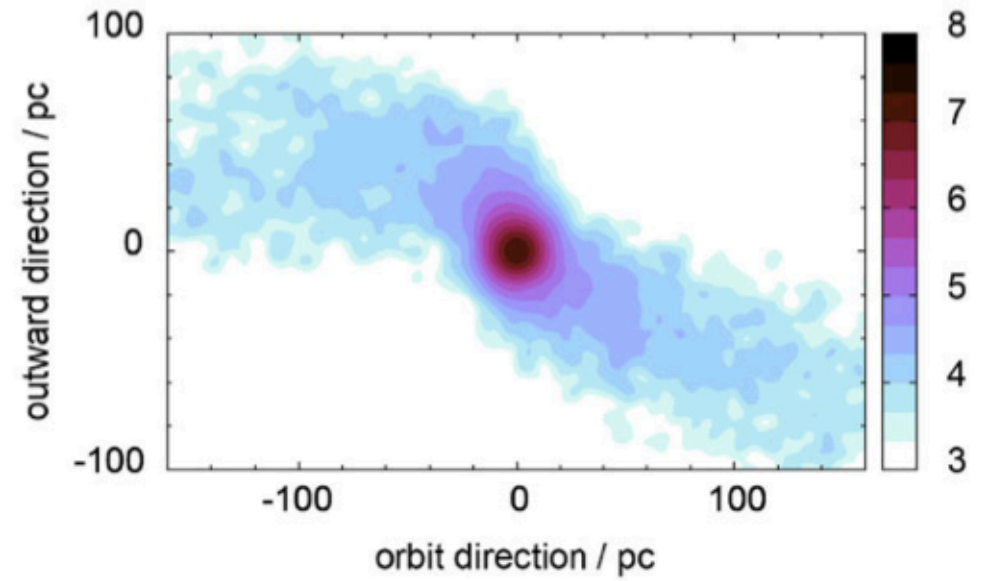
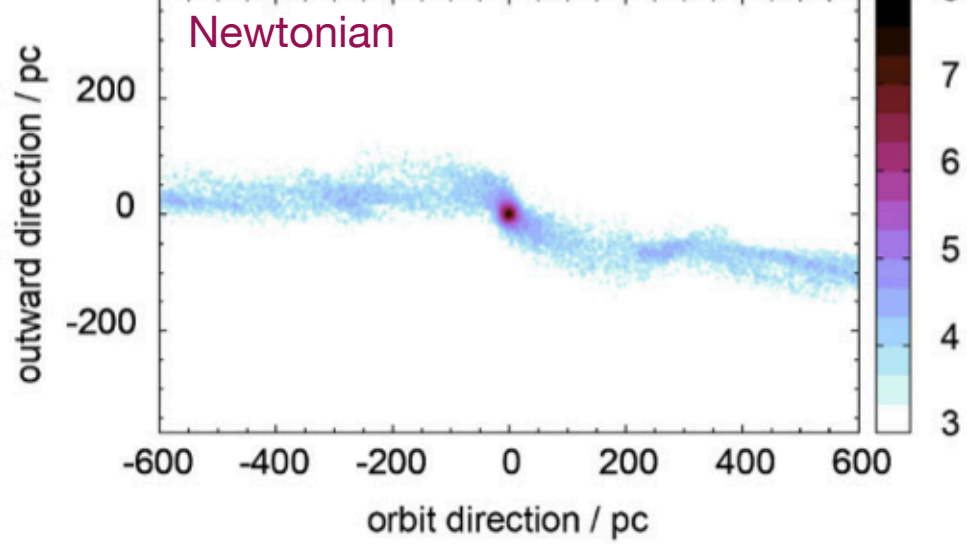
$$N_l > N_t$$

MOND radius :

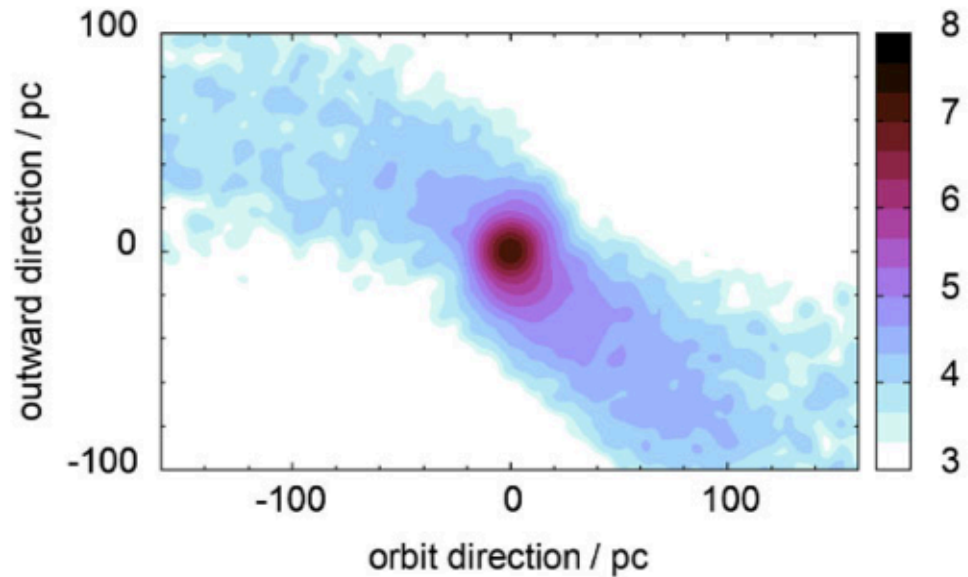
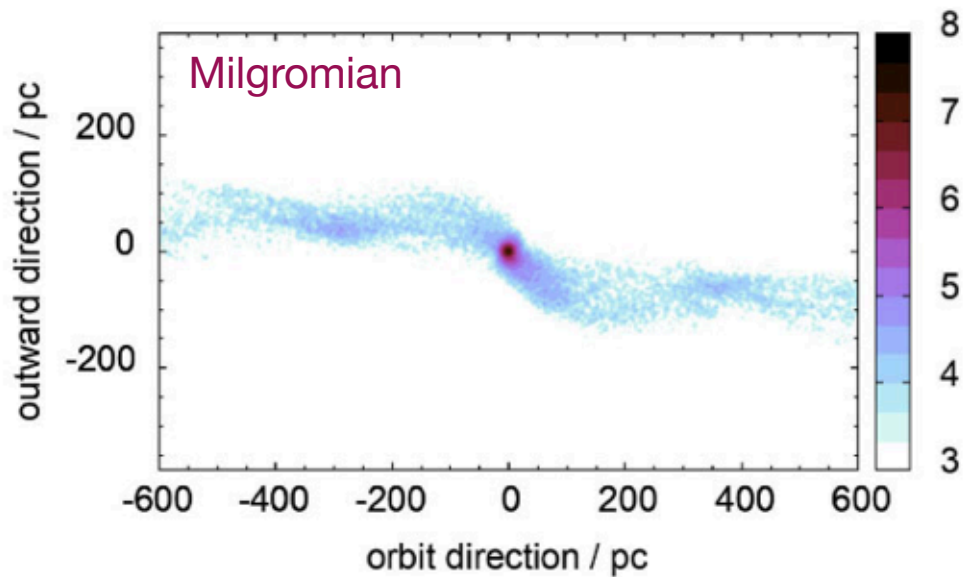
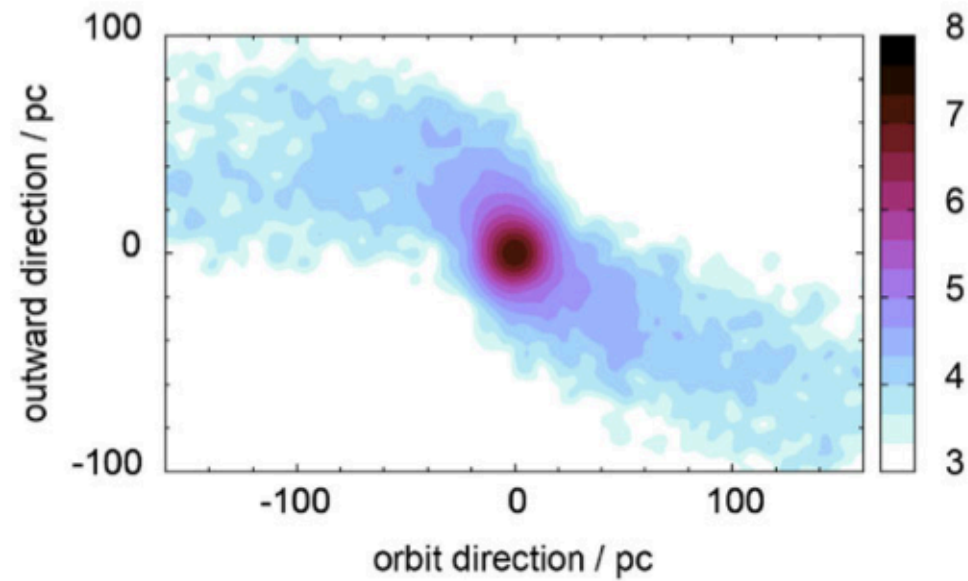
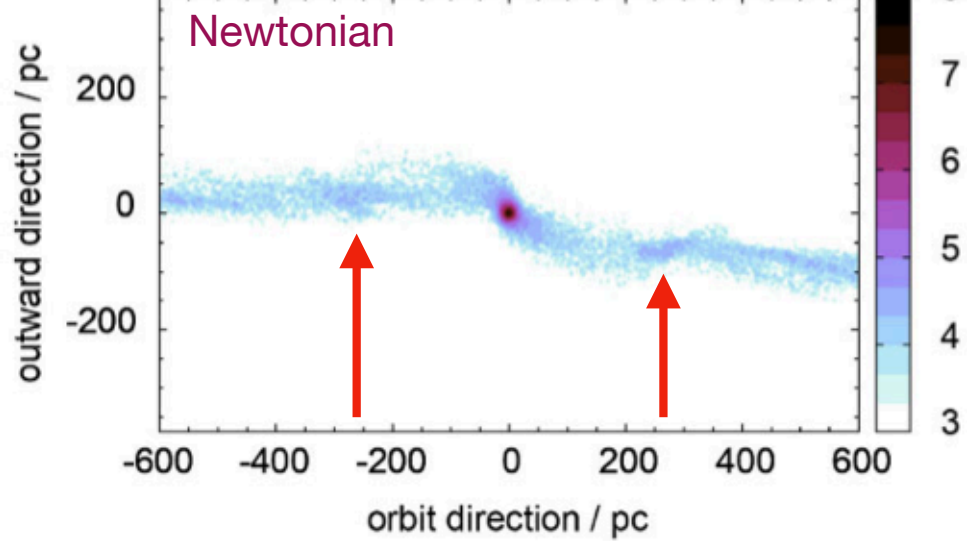
$$r_M = \left( \frac{G M_{oc}}{a_0} \right)^{\frac{1}{2}}$$

$N_t$  stars  
into trailing tail

(Kroupa, Jerabkova et al. 2022)

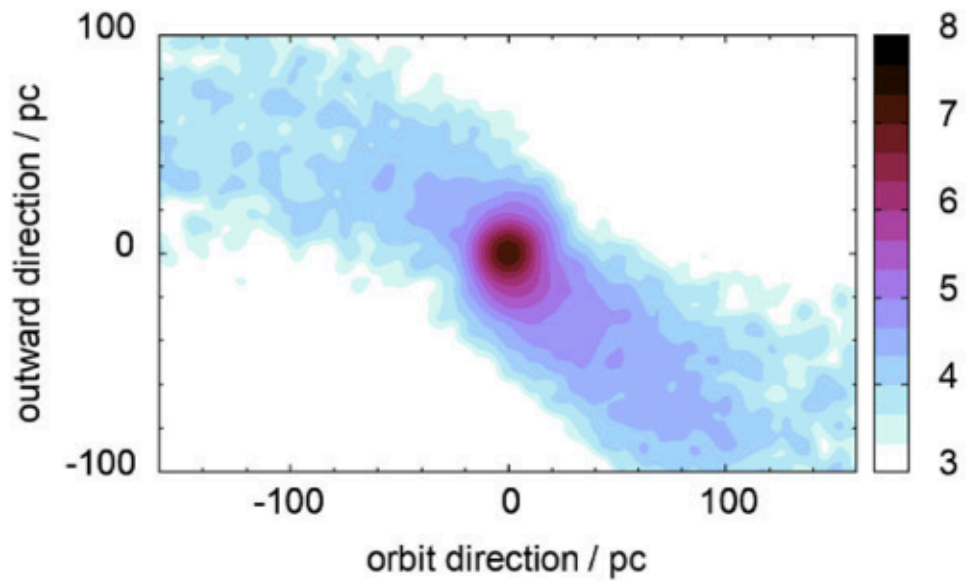
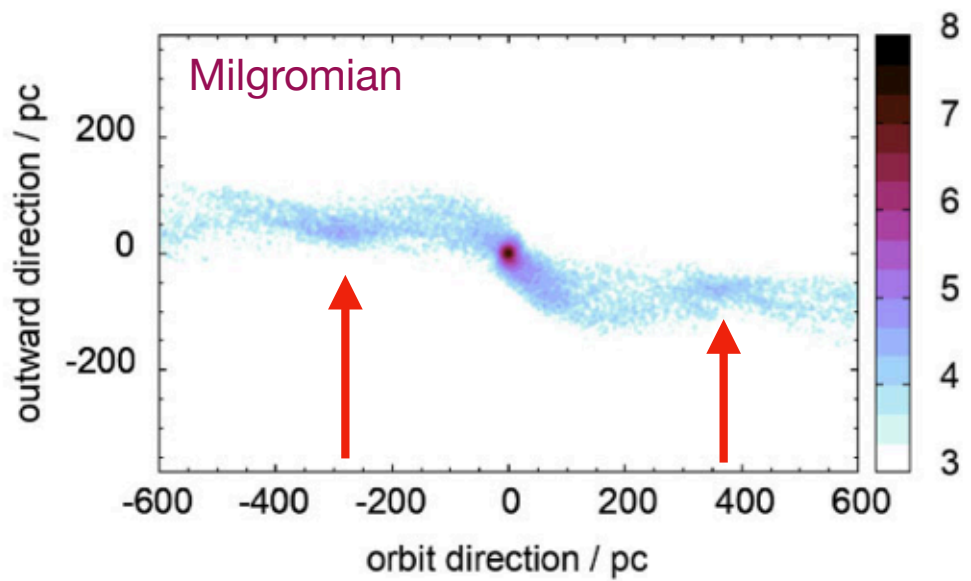
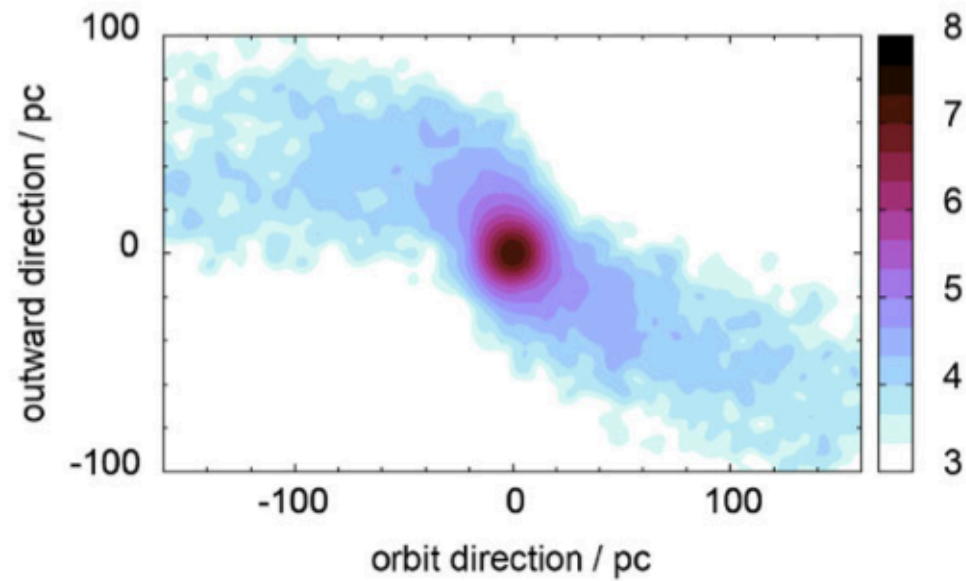
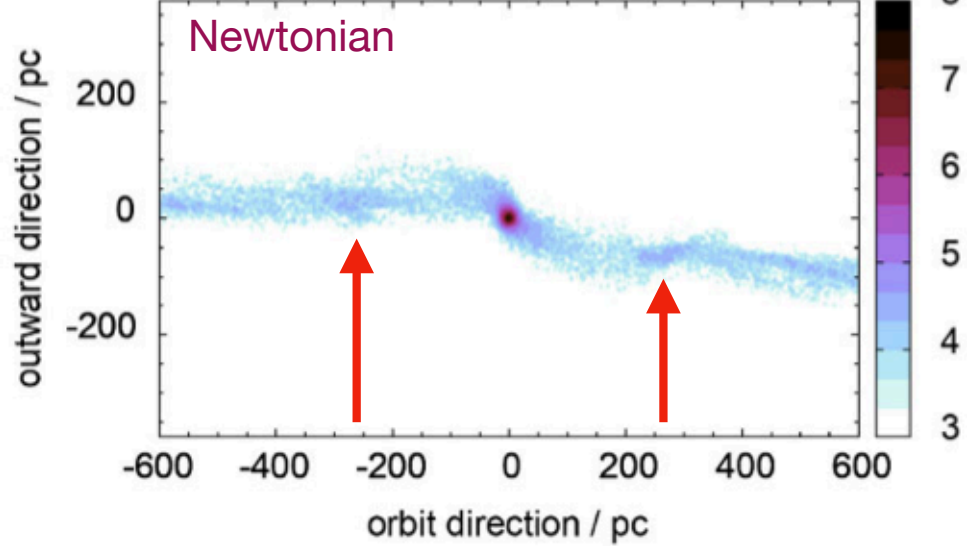


(Kroupa, Jerabkova et al. 2022)

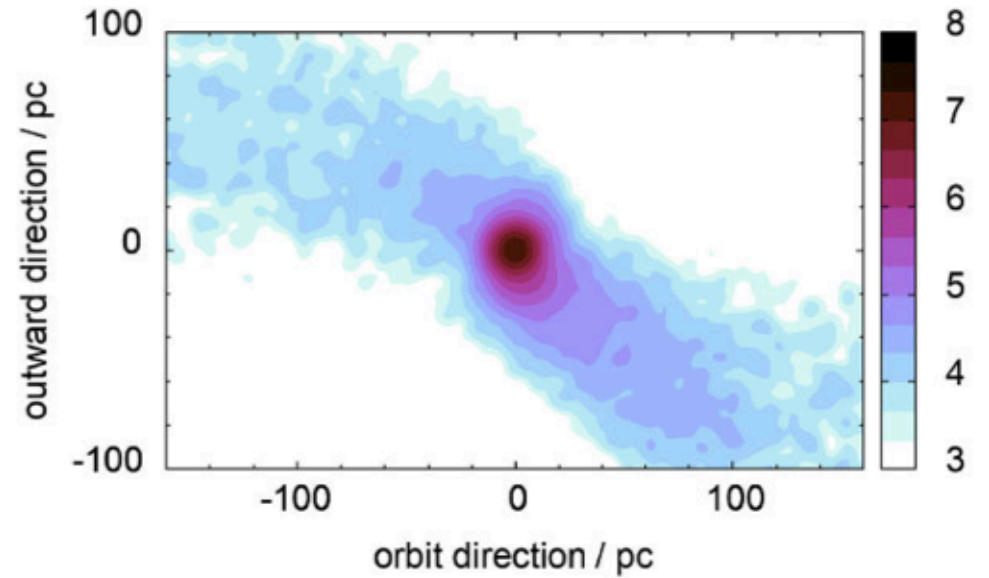
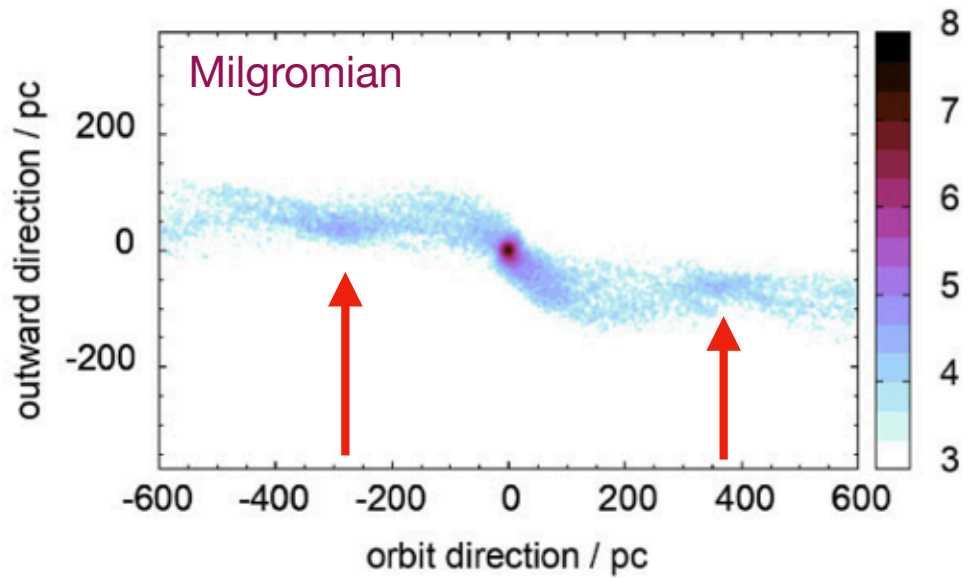
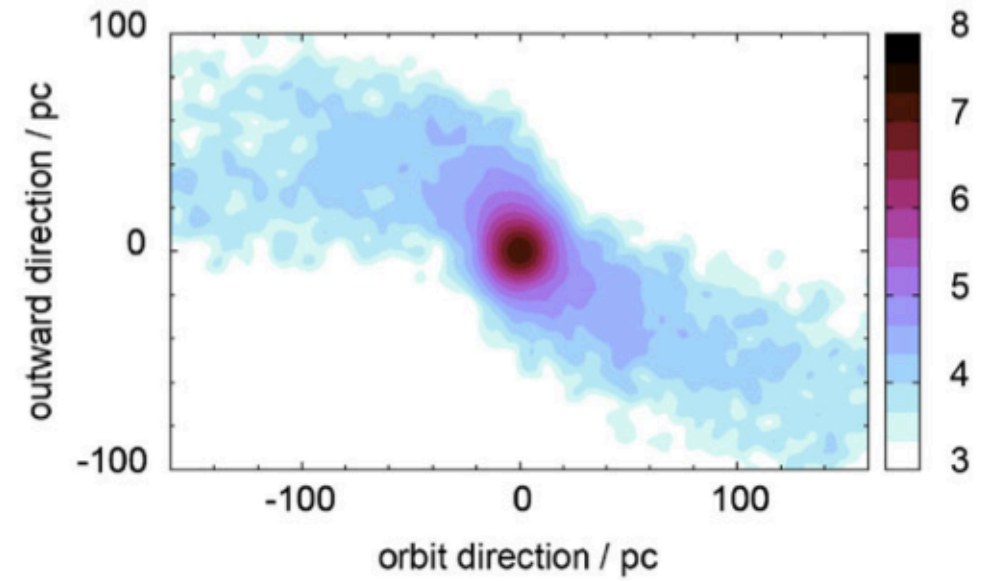
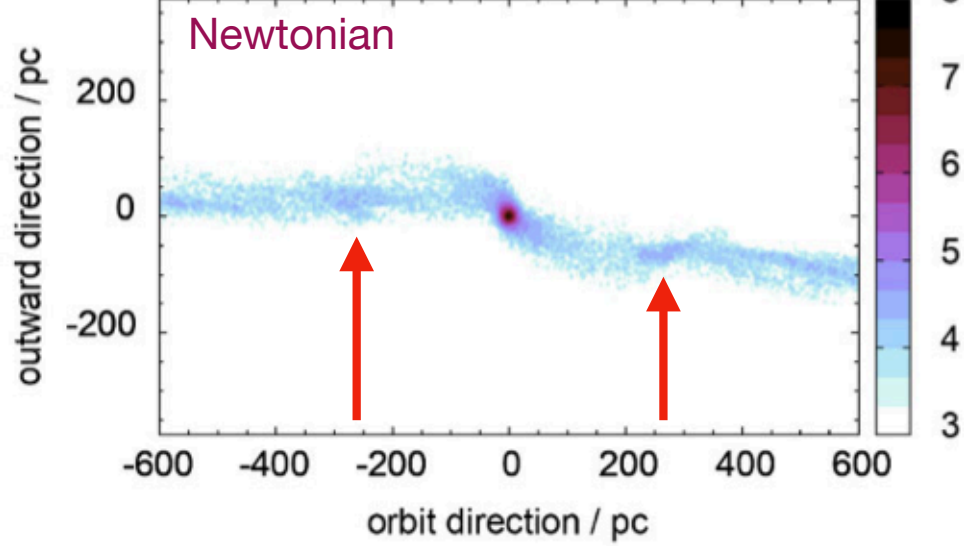




(Kroupa, Jerabkova et al. 2022)



(Kroupa, Jerabkova et al. 2022)



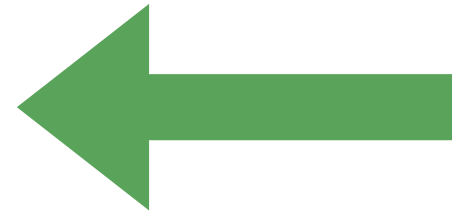
Leading Kuepper-overdensity further from cluster in Milgromian case

Above applied the new CCP method  
to extract the extended tidal tails.

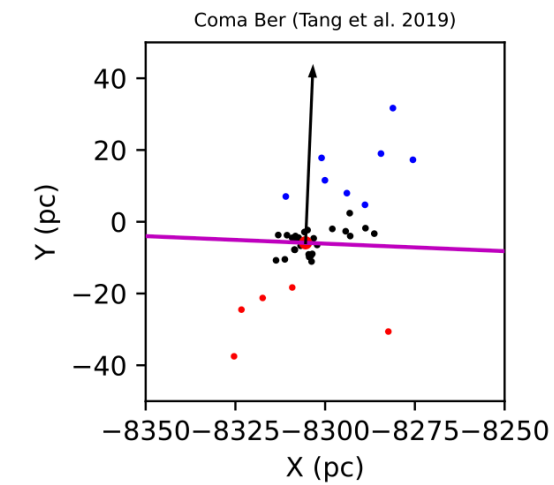
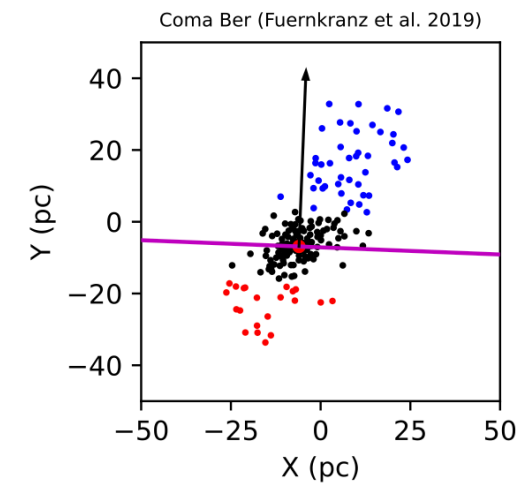
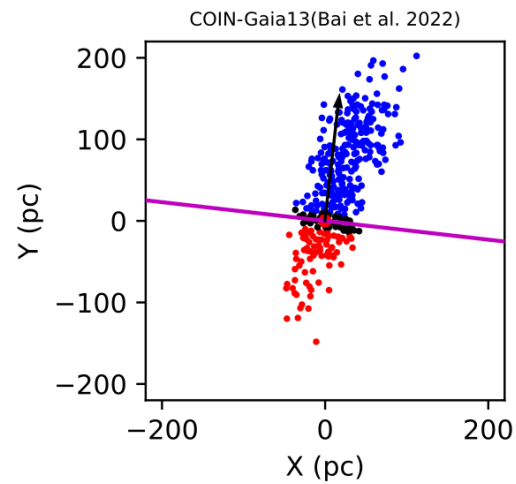
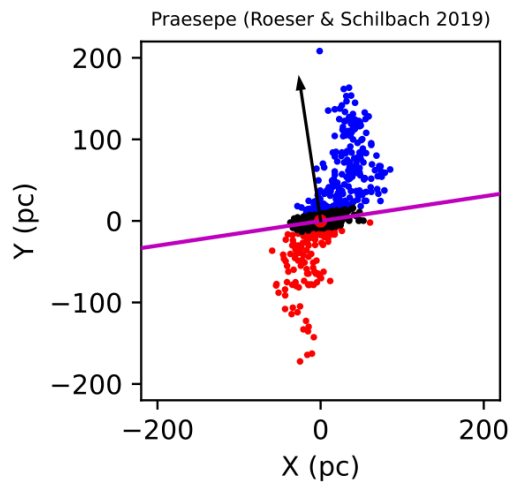
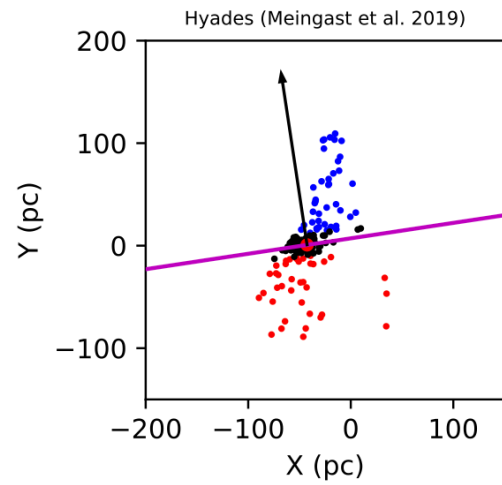
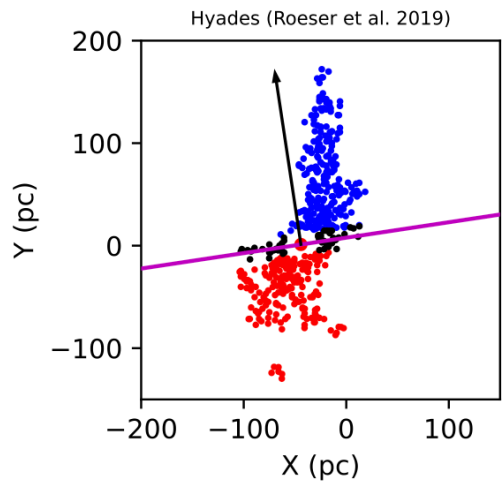


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Four nearby open star clusters analysed  
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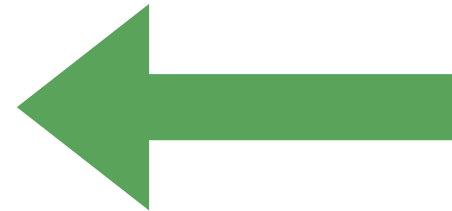


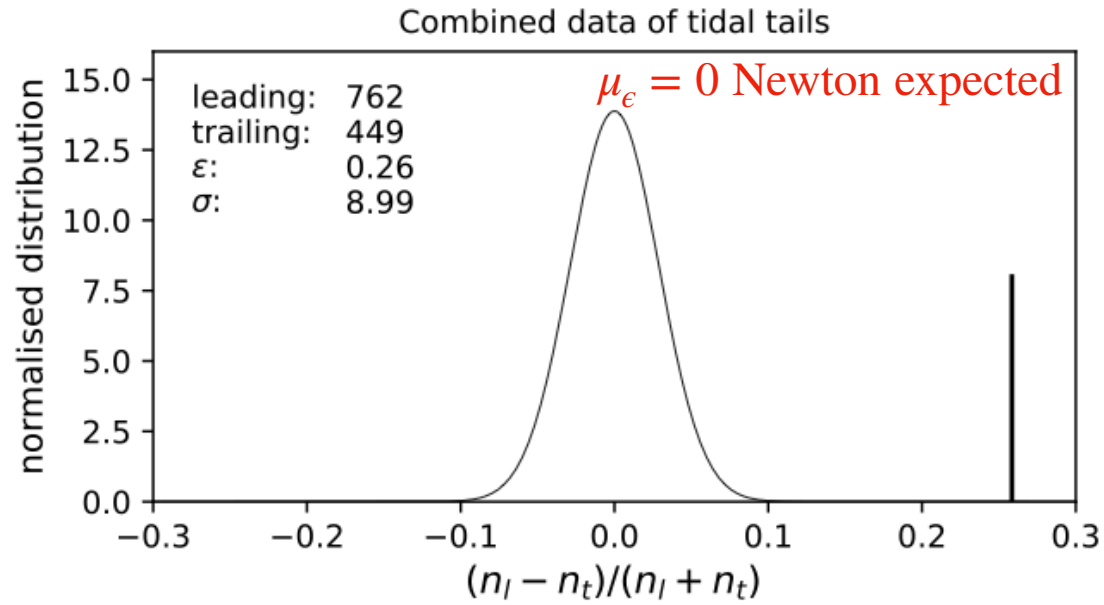
# (Kroupa, Pflamm-Altenburg et al. 2024)



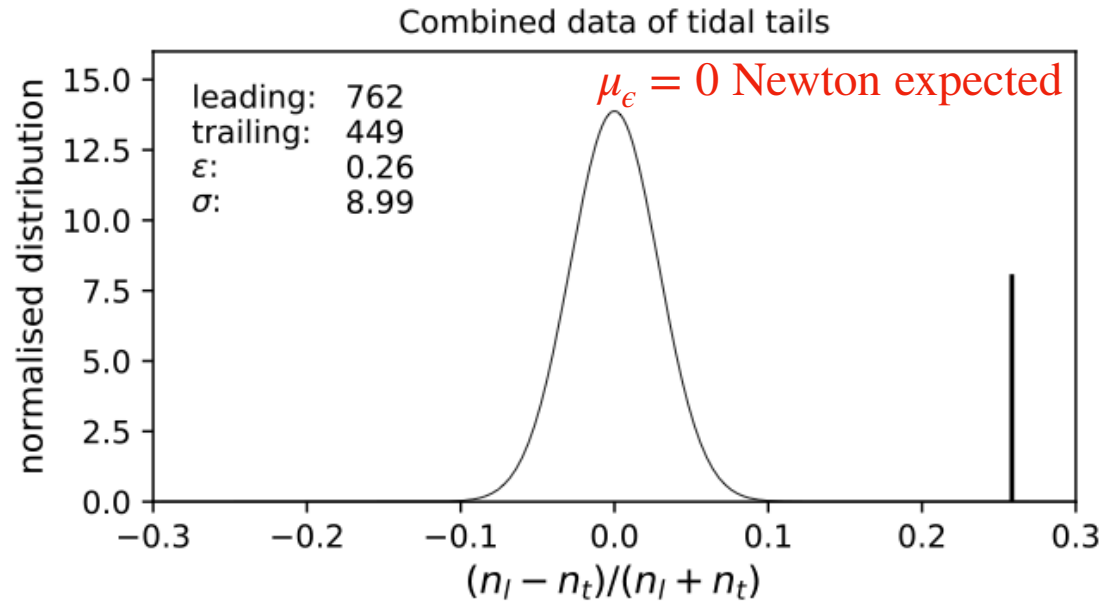
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Four nearby open star clusters analysed by 6 different teams using the older / traditional CP method.





**Figure 9.** As Fig. 4, but here the number of stars in the leading and trailing tails are combined from all observed tidal tails to assess the probability whether all measurements are one-sided asymmetric with  $n_{l,\text{sum}} > n_{t,\text{sum}}$ .

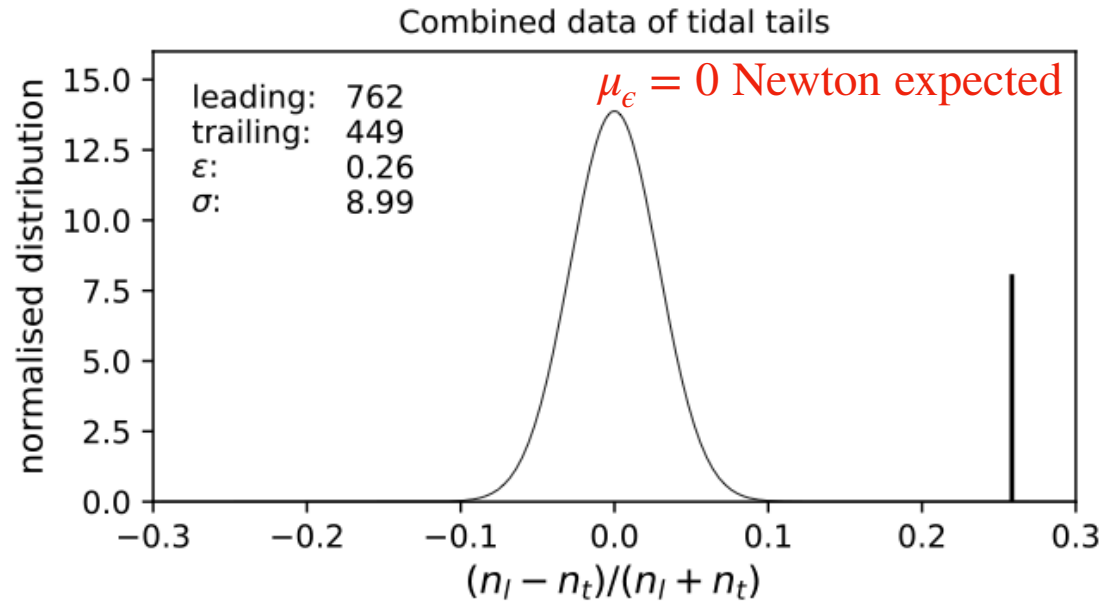


$$\epsilon = \frac{n_l - n_t}{n_l + n_t} \quad \text{asymmetry parameter}$$

$$\sigma_\epsilon = \frac{1}{\sqrt{n_l + n_t}} \quad \text{its variance}$$

$$\sigma = \frac{|\mu_\epsilon - \epsilon|}{\sigma_\epsilon} \quad \text{asymmetry significance}$$

**Figure 9.** As Fig. 4, but here the number of stars in the leading and trailing tails are combined from all observed tidal tails to assess the probability whether all measurements are one-sided asymmetric with  $n_{l,\text{sum}} > n_{t,\text{sum}}$ .



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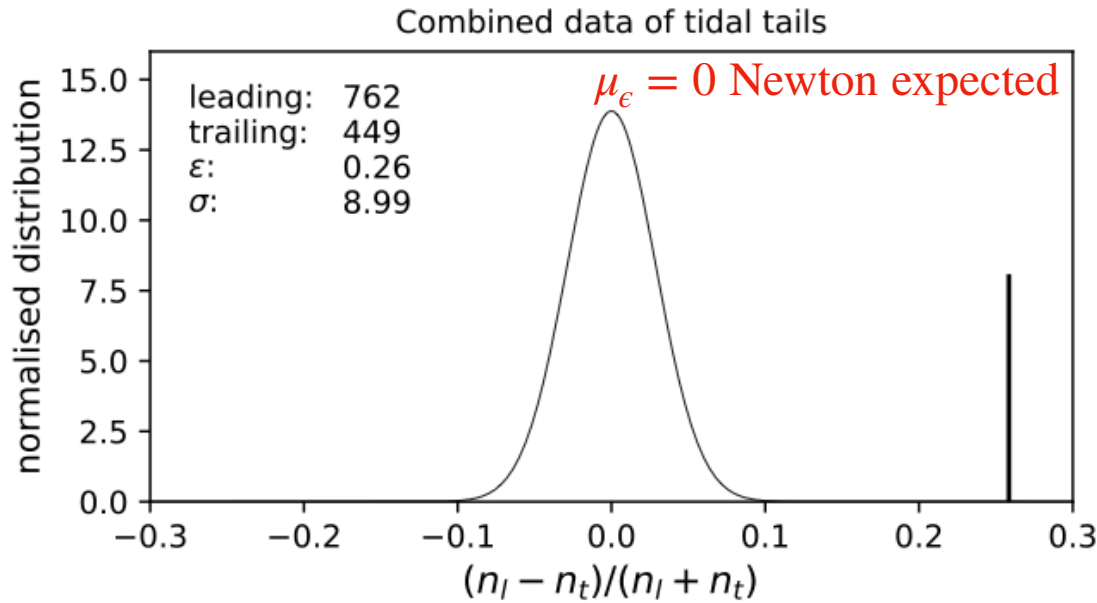
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$$\sigma = \frac{|\mu_\epsilon - \epsilon|}{\sigma_\epsilon} \quad \text{asymmetry significance}$$



Observed tidal tails  
are in 8.99sigma  
tension with  
Newtonian symmetry.

**Figure 9.** As Fig. 4, but here the number of stars in the leading and trailing tails are combined from all observed tidal tails to assess the probability whether all measurements are one-sided asymmetric with  $n_{l,\text{sum}} > n_{t,\text{sum}}$ .



$$\epsilon = \frac{n_l - n_t}{n_l + n_t}$$

asymmetry parameter

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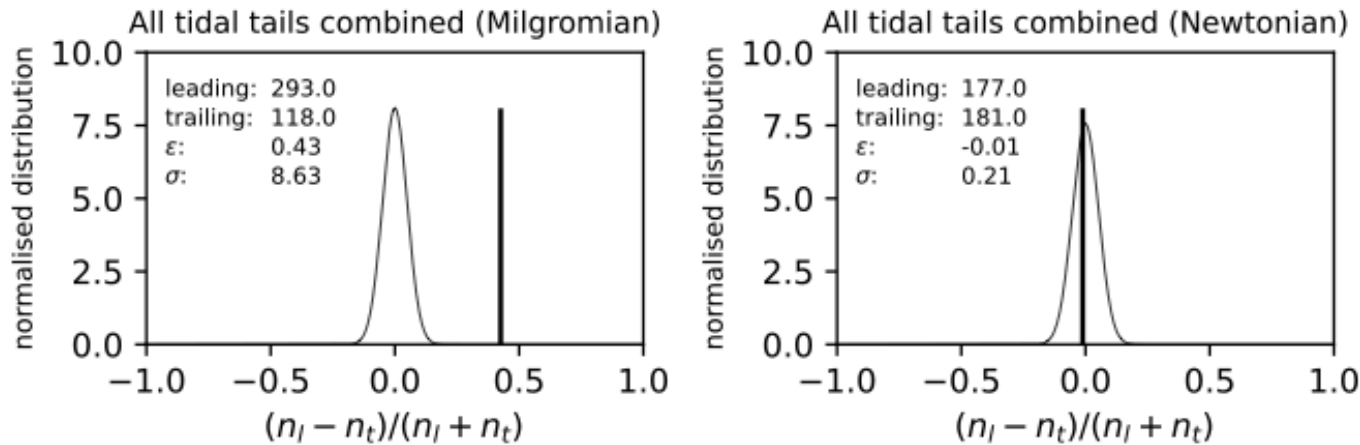
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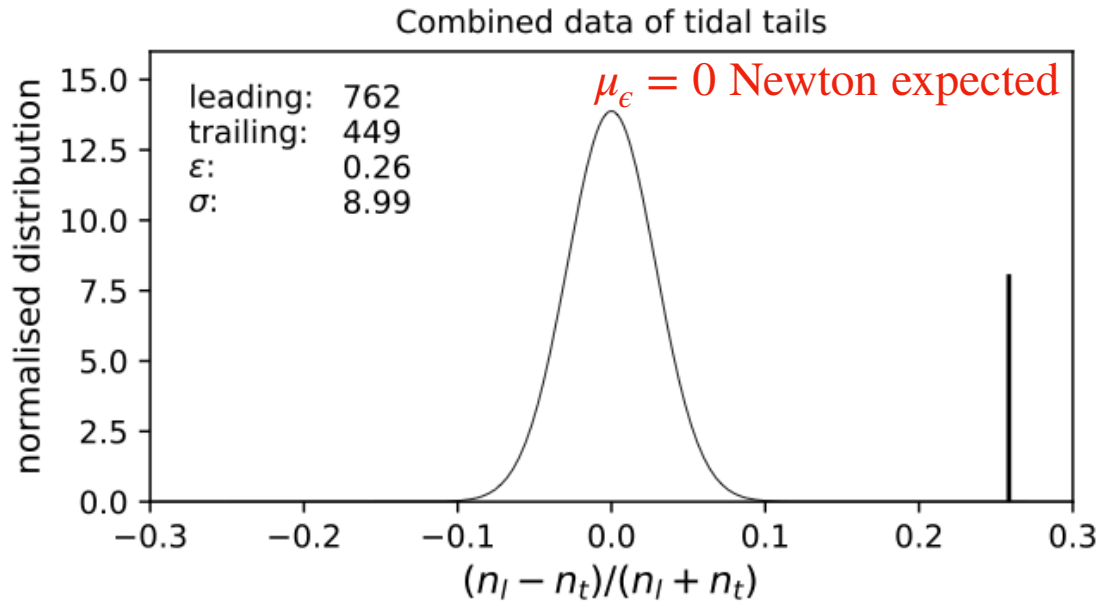
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**Figure 14.** Similar to Fig. 13. Here the leading and trailing tail numbers of all models are combined to assess the probability if all measurements are one-sided asymmetric with  $n_l > n_t$ . The left panel depicts the combined stacked Milgromian models and shows a similar and extremely significant asymmetry that is very comparable to that observed (Fig. 9), while the combined stacked Newtonian models (right panel) are consistent with the leading and trailing tail having a similar number of stars.



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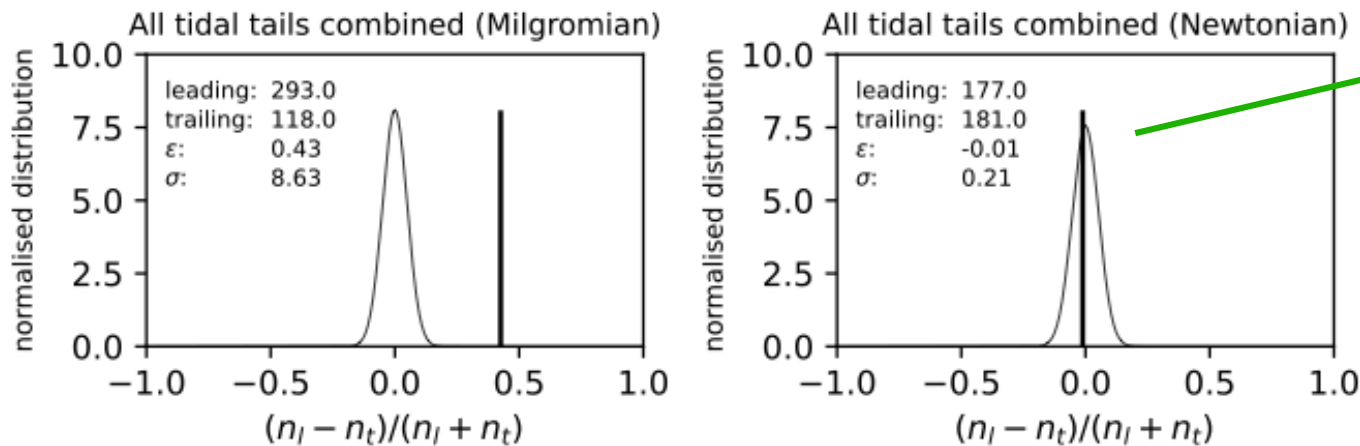
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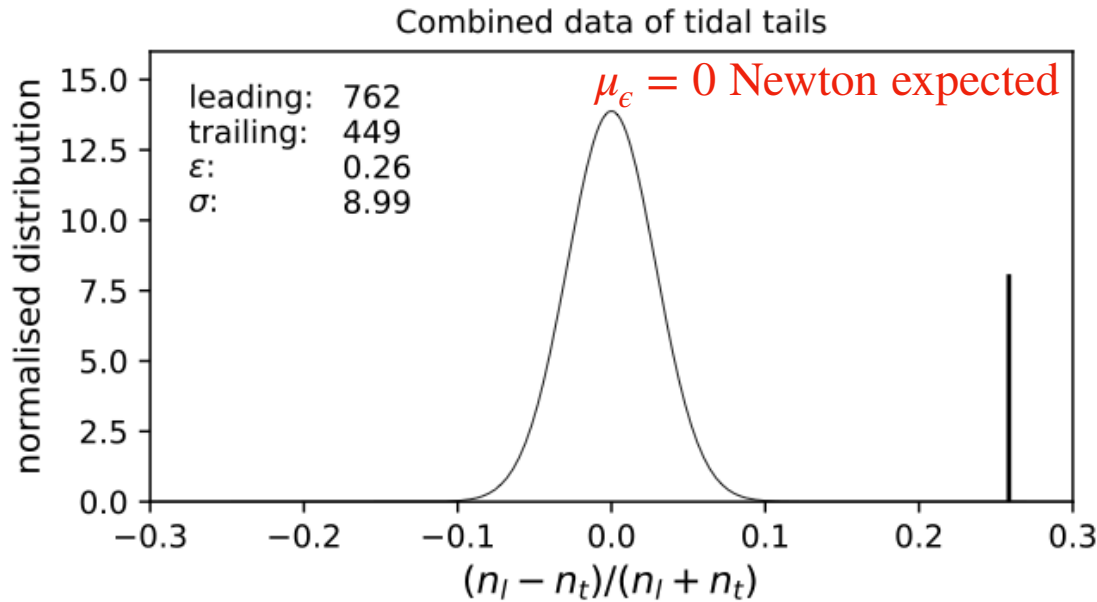
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Newtonian tidal tails  
are in 0.21sigma  
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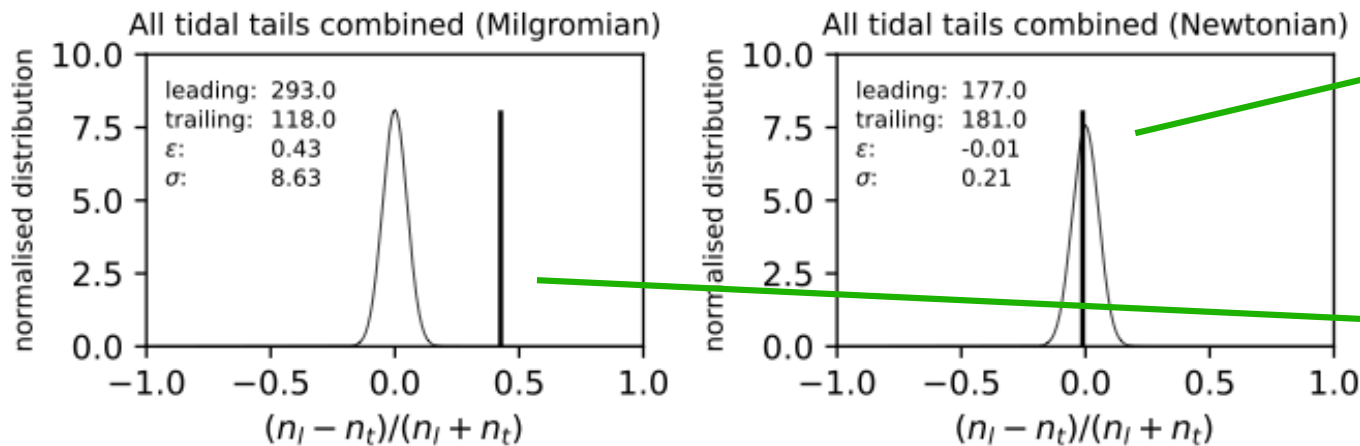
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Modelled  
Newtonian tidal tails  
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tension with  
Newtonian symmetry.

Modelled  
Milgromian tidal tails  
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tension with  
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*unambiguously*  
*compellingly*  
*absolutely*  
falsify Newtonian gravitation

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**Consistency of test results :**

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### **Consistency of test results :**

Falsification of cold and warm dark matter particles  
(dynamical friction test on 100kpc scale)

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Gravitational potential cannot be Newtonian

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### **Consistency of test results :**

Falsification of cold and warm dark matter particles  
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Gravitational potential cannot be Newtonian

The tidal tail asymmetry confirms this !

Other tests,  
**not** based  
on  
Chandrasekhar dynamical  
friction

The distribution of  
matter on scales  
of  
Mpc

# Structure of and correlations in Local group

Frighteningly symmetric structure of the Local Group



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**Everything we know  
about the Local  
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Pawlowski, Kroupa & Jerjen (2013) :

*"The discovery of  
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# Structure of and correlations in Local group

Frighteningly symmetric structure of the Local Group

Looking along the line  
between Milky Way  
and Andromeda

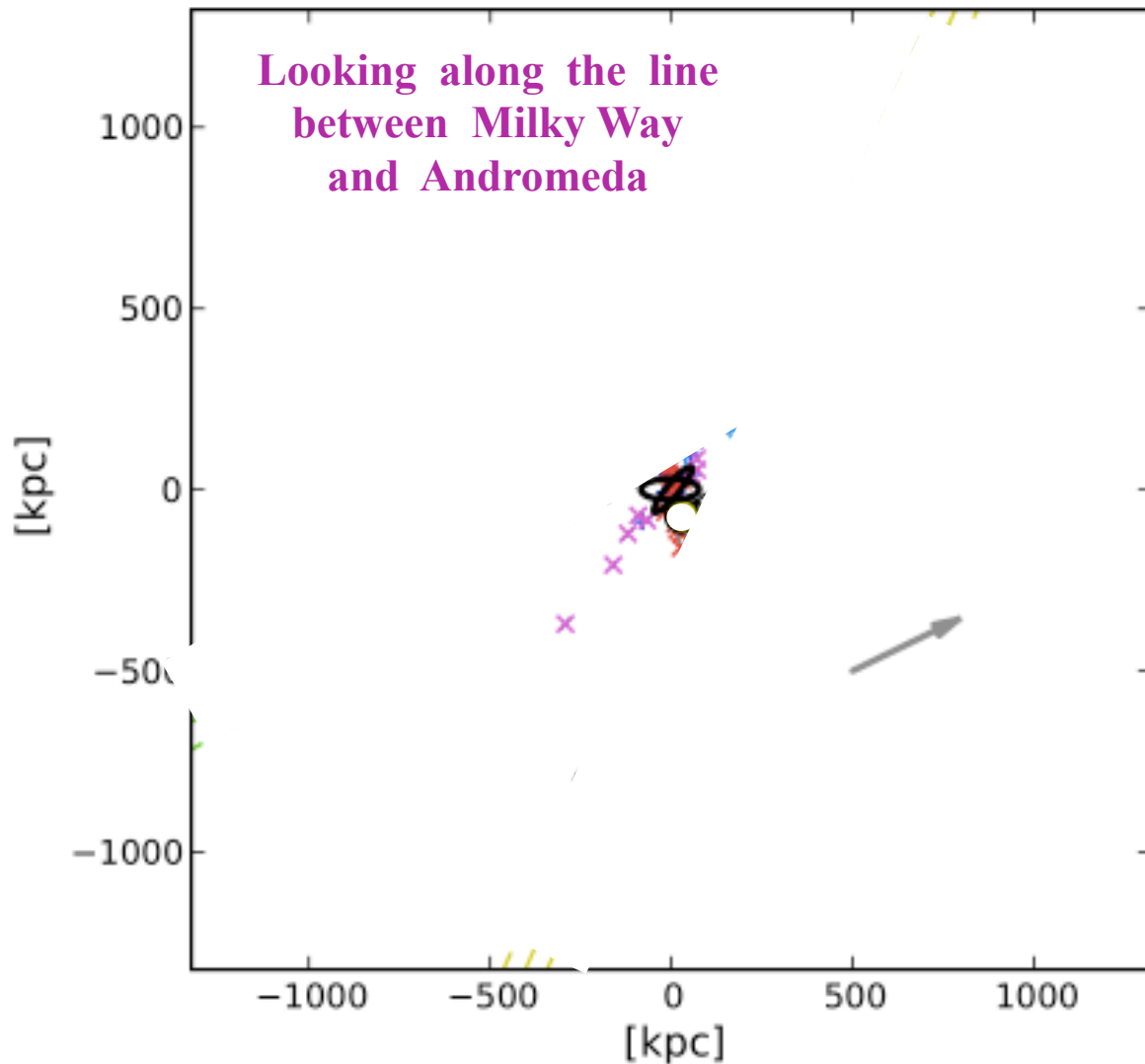
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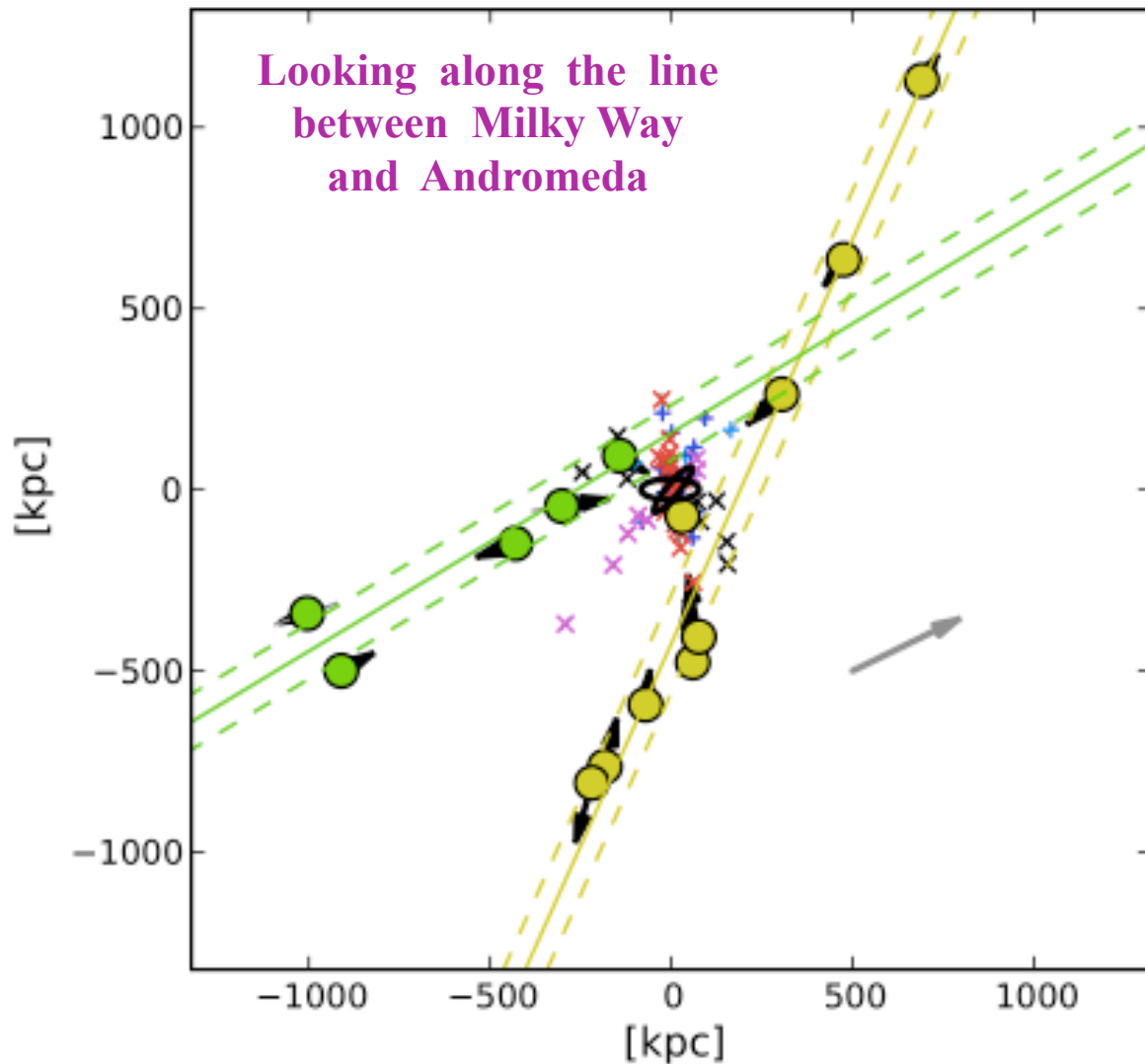
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**Figure 9.** Edge-on view of both LG planes. The orientation of the MW and M31 are indicated as black ellipses in the centre. Members of the LGP1 are plotted as yellow points, those of LGP2 as green points. MW galaxies are plotted as plus signs (+), all other galaxies as crosses (x), the colours code their plane membership as in Fig. 6. The best-fitting planes are plotted as

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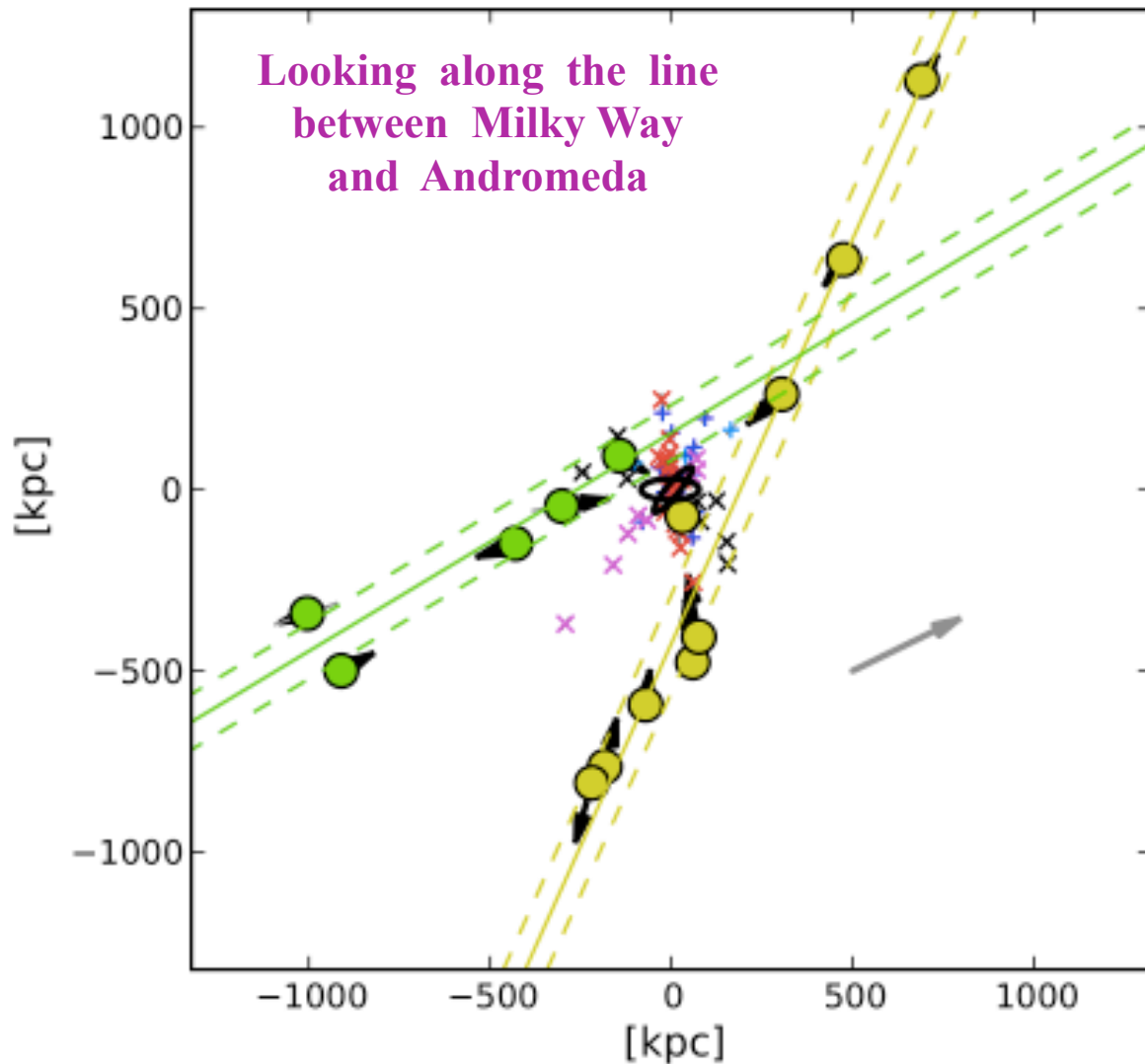
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A frightening symmetry

NOT SMOc at  $\infty$  sigma

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The distribution of  
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# KBC void and Hubble Tension

## The Cosmological Scale

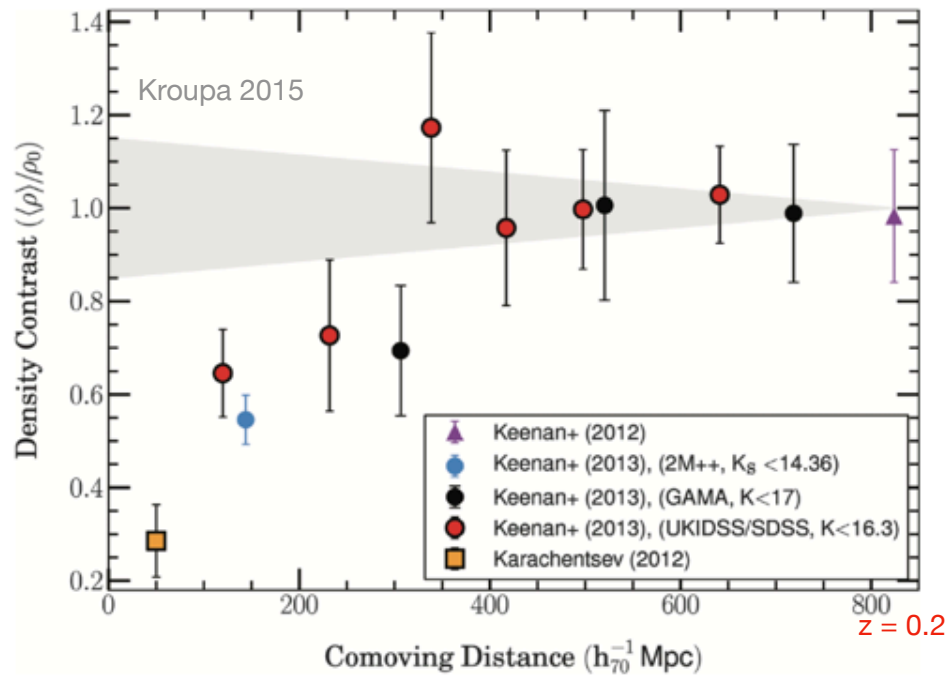


Figure 1. The KBC void: the actual density of normal matter divided by the mean cosmological density is plotted in dependence of the distance from the position of the Sun (which is in the Local Group of galaxies). The grey area indicates the density fluctuations allowed by the  $\Lambda$ CDM model. Taken from fig. 1 in [Kroupa \(2015\)](#).



# KBC void and Hubble Tension

## The Cosmological Scale

Haslbauer, Banik & Kroupa 2020 :

The under-density is evident in

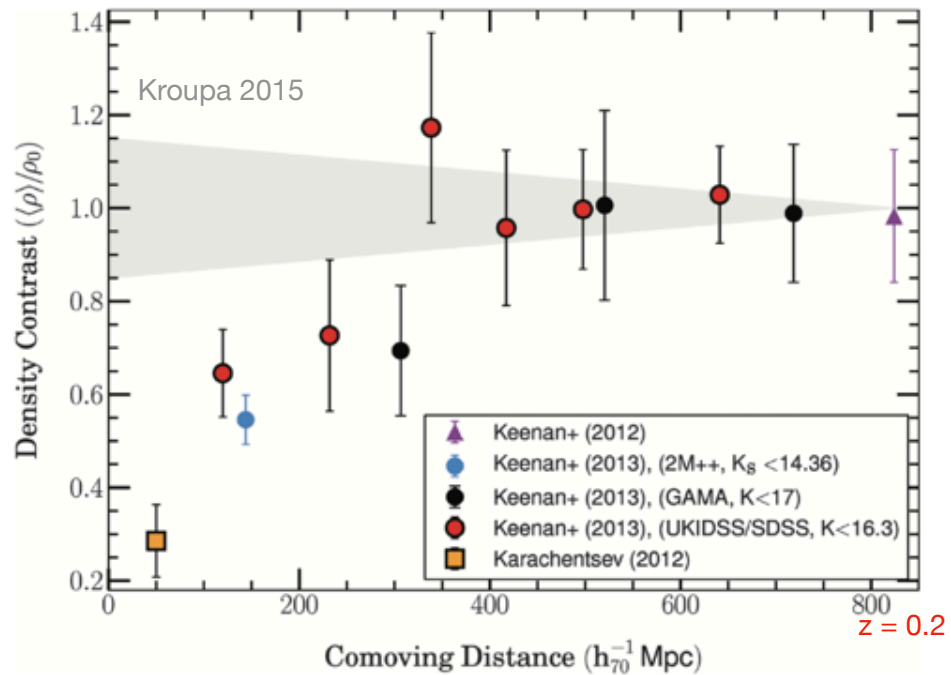


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## The Cosmological Scale

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Maddox+1990; Zucca+1997

near-infrared galaxy surveys

Keenan, Barger & Cowie'13 (KBC)

X-ray cluster surveys

Böhringer+2015; Böhringer, Chan, Collins 2020;  
Migkas+21

CMB dipole indicating large-scale bulk flows as  
expected for such a void (radio observations)

Rubart & Schwarz 2013; Rubart, Bacon & Schwarz 2014;  
Javanmardi+ 2015; Secrest+ 2020

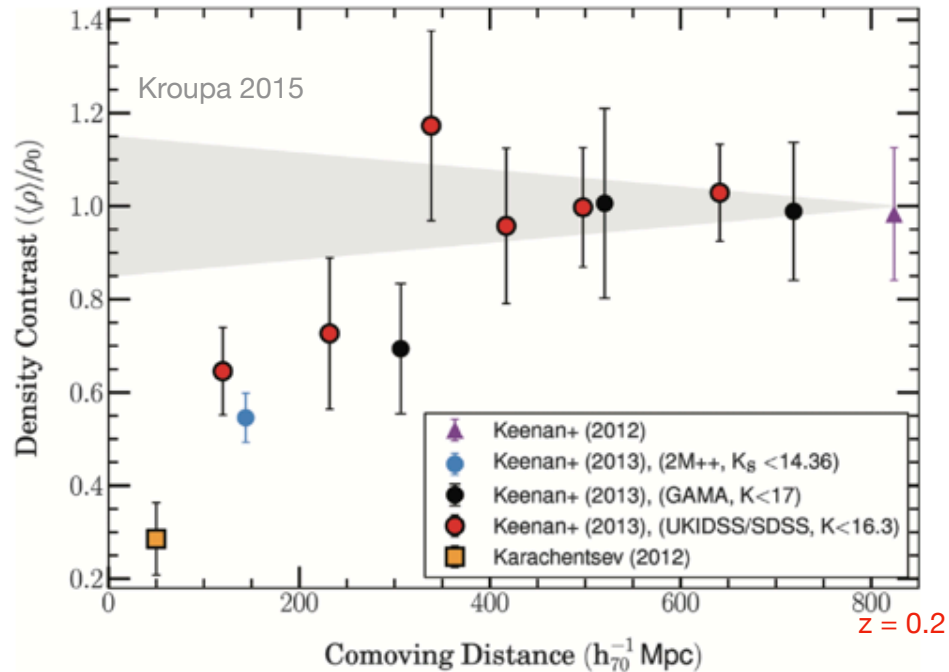


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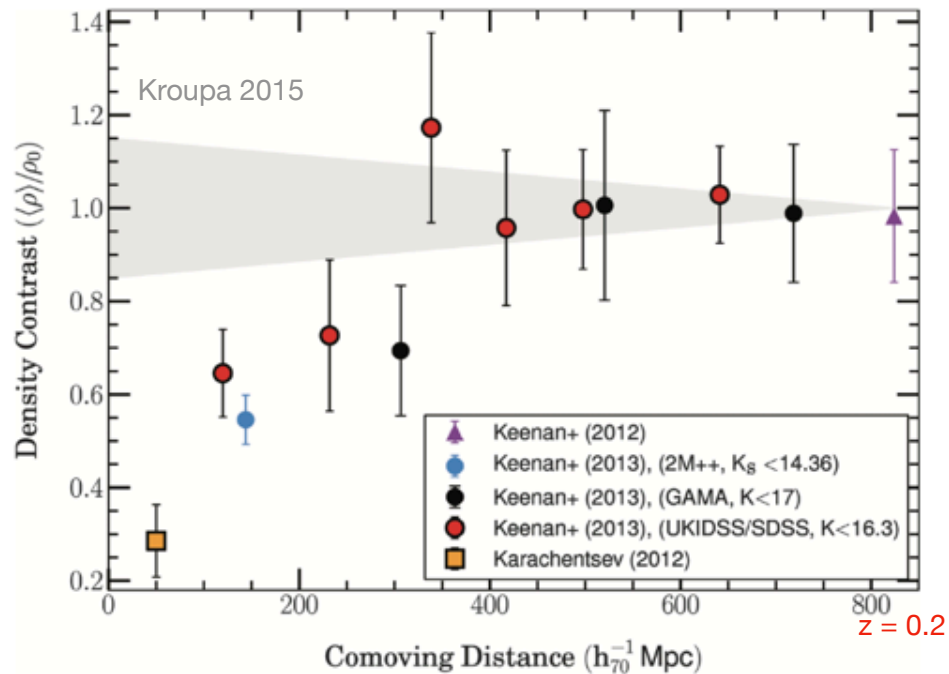


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Additionally :

Strong evidence for highly significant  
over- and under-densities in galaxy-cluster data

Migkas & Reiprich (2018); Migkas et al. (2021)

4.9 sigma exclusion of cosmological principle based  
on distribution of  $10^6$  quasars

Secrest+... Sarkar et al. (2021)

# KBC void and Hubble Tension

## The Cosmological Scale

Can the KBC void  
grow in the SMOG ?

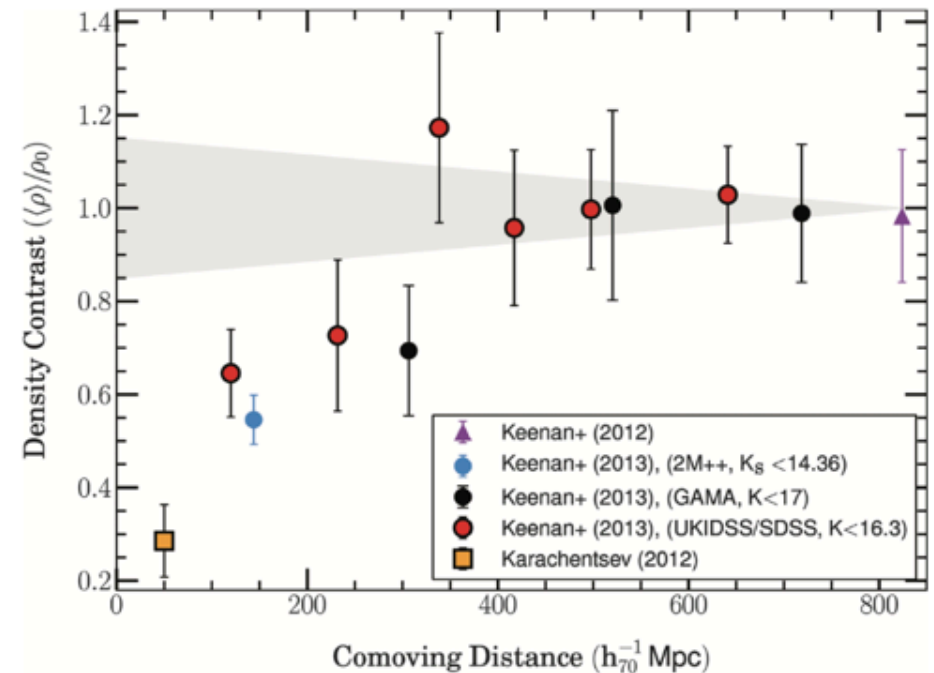


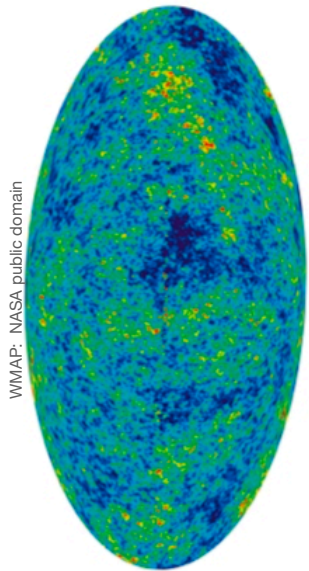
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# KBC void and Hubble Tension

## The Cosmological Scale

Can the KBC void  
grow in the SMOc ?

CMB at  $z = 1100$   
density contrast  $\approx 1e-5$



Use Millenium XXL  
SMoC/LCDM simulation  
(Angulo et al. 2012)

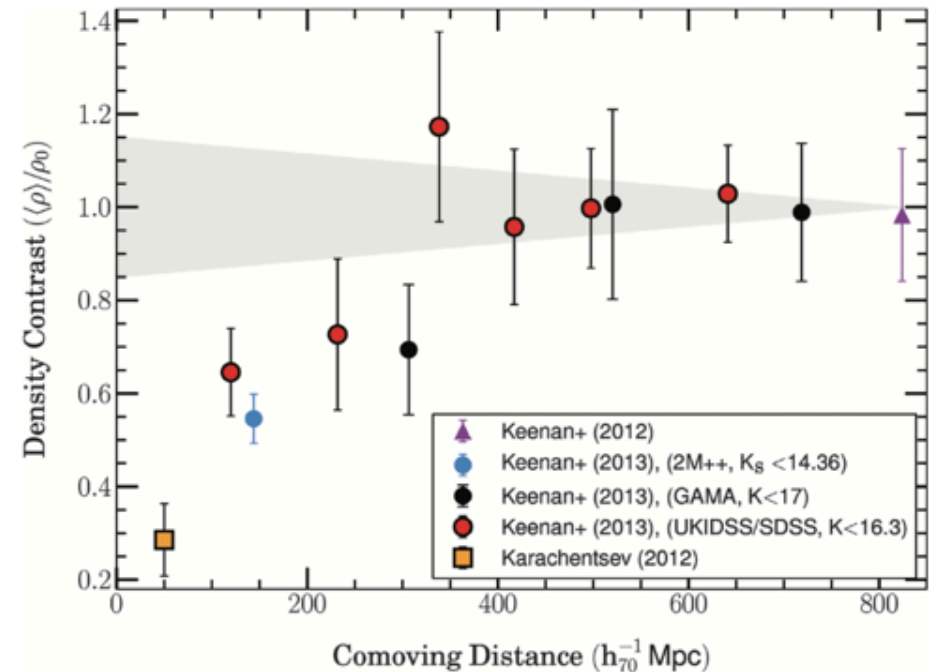


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# KBC void and Hubble Tension

The Cosmological Scale

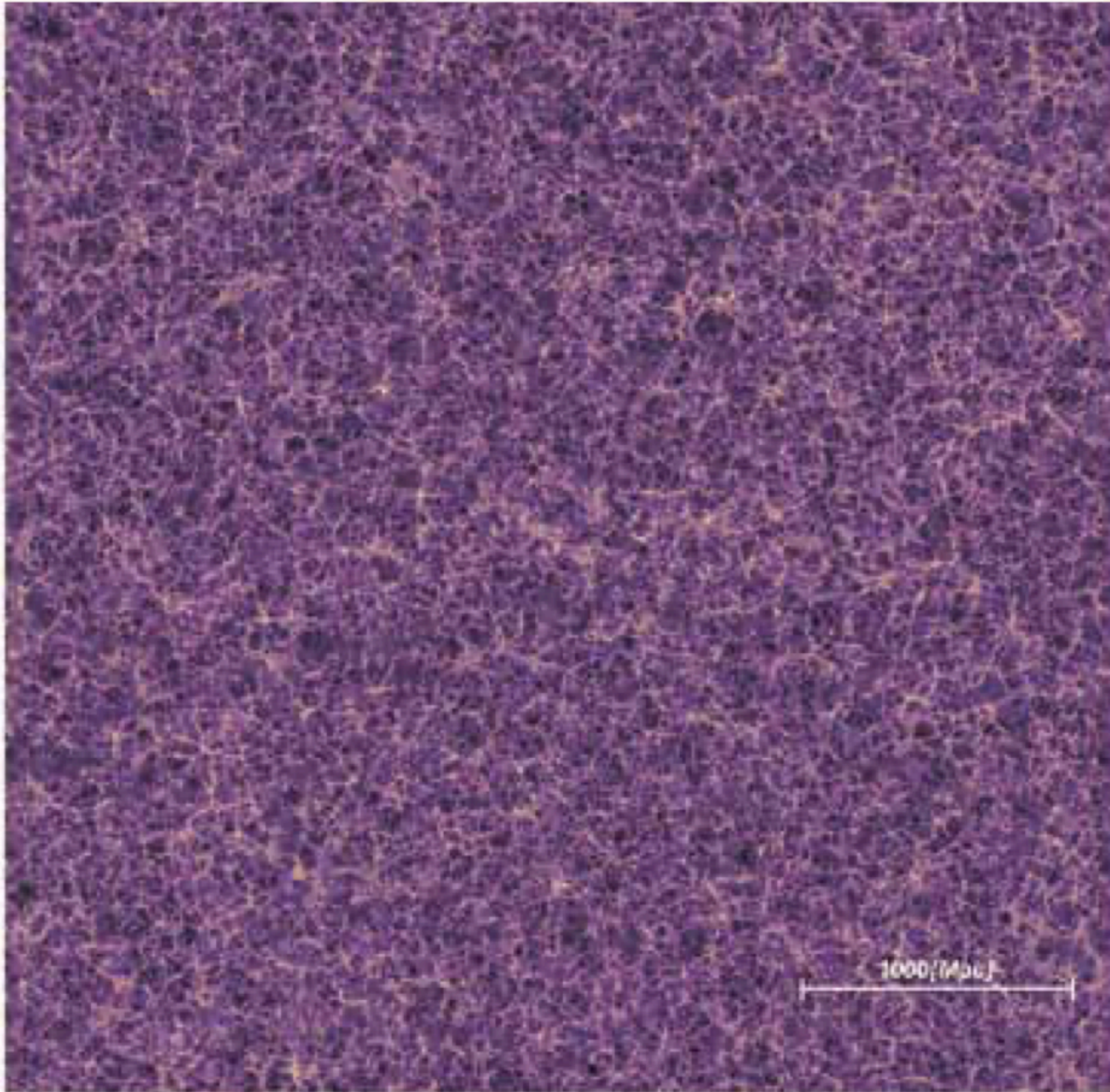
Test how often does a  
KBC void occur ?

Haslbauer, Banik & Kroupa 2020



# KBC void and Hubble Tension

The Cosmological Scale



The Millennium XXL (MXXL)  
simulation (SMoC)

Angulo et al. 2012

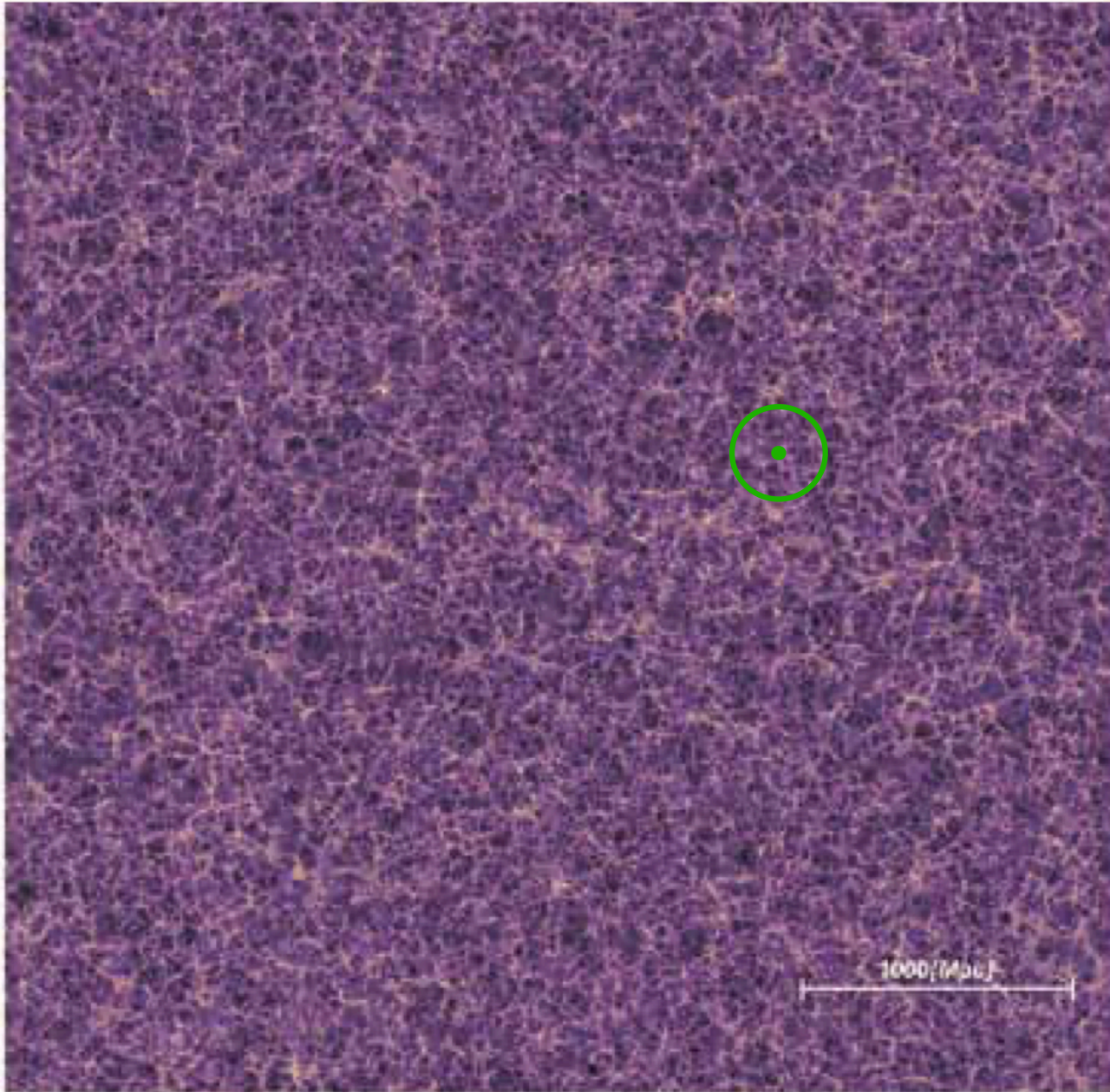
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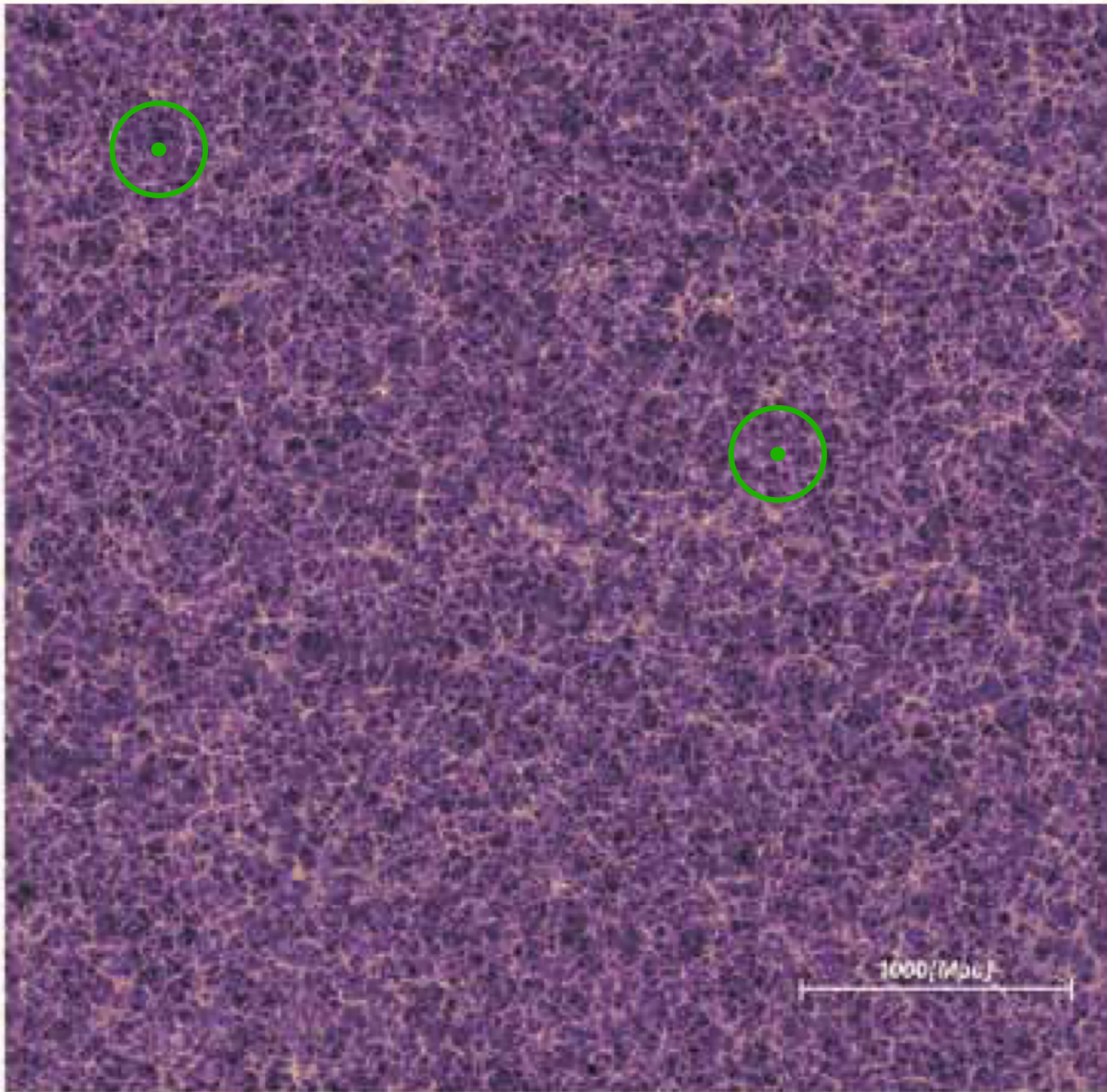
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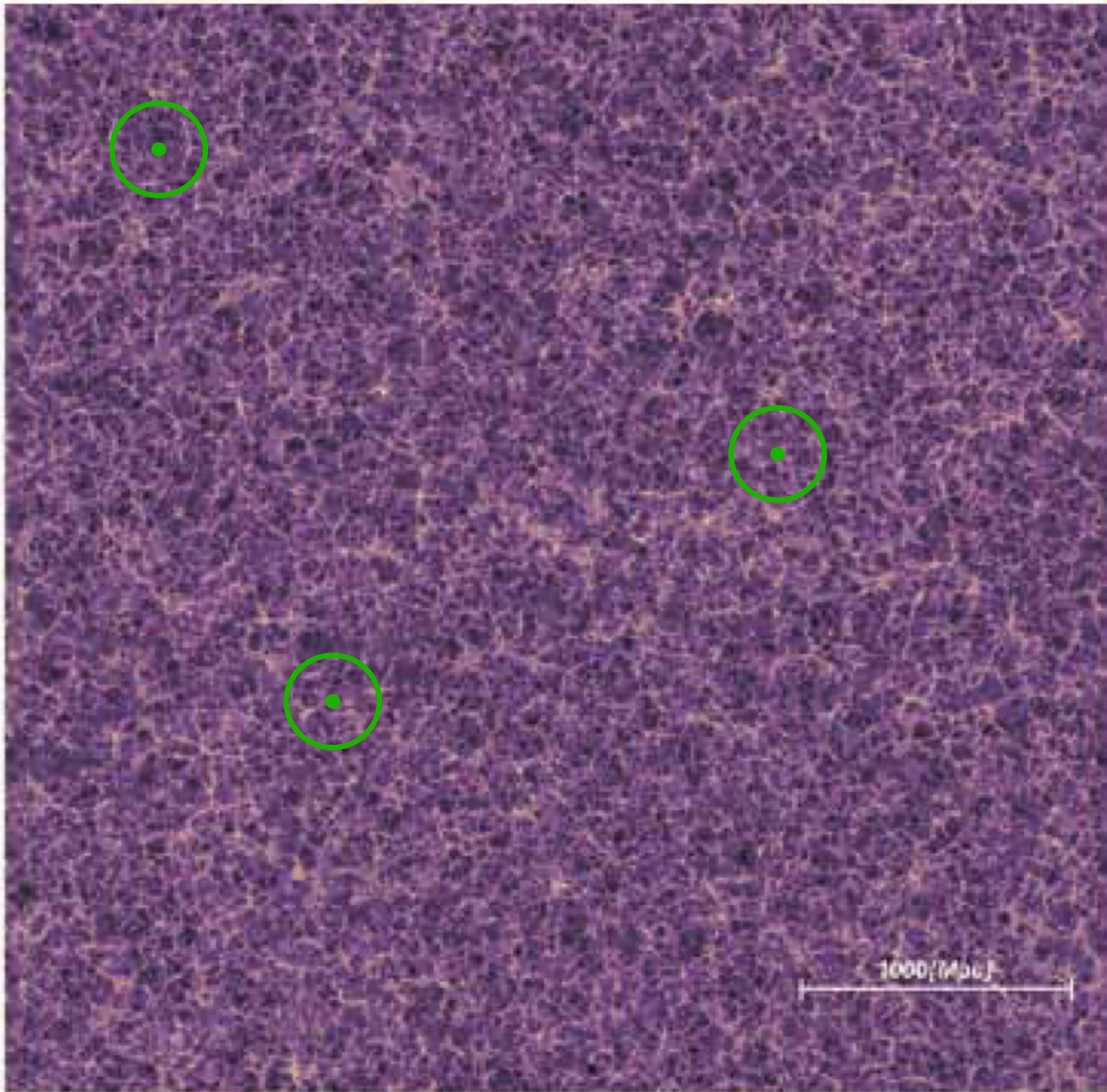
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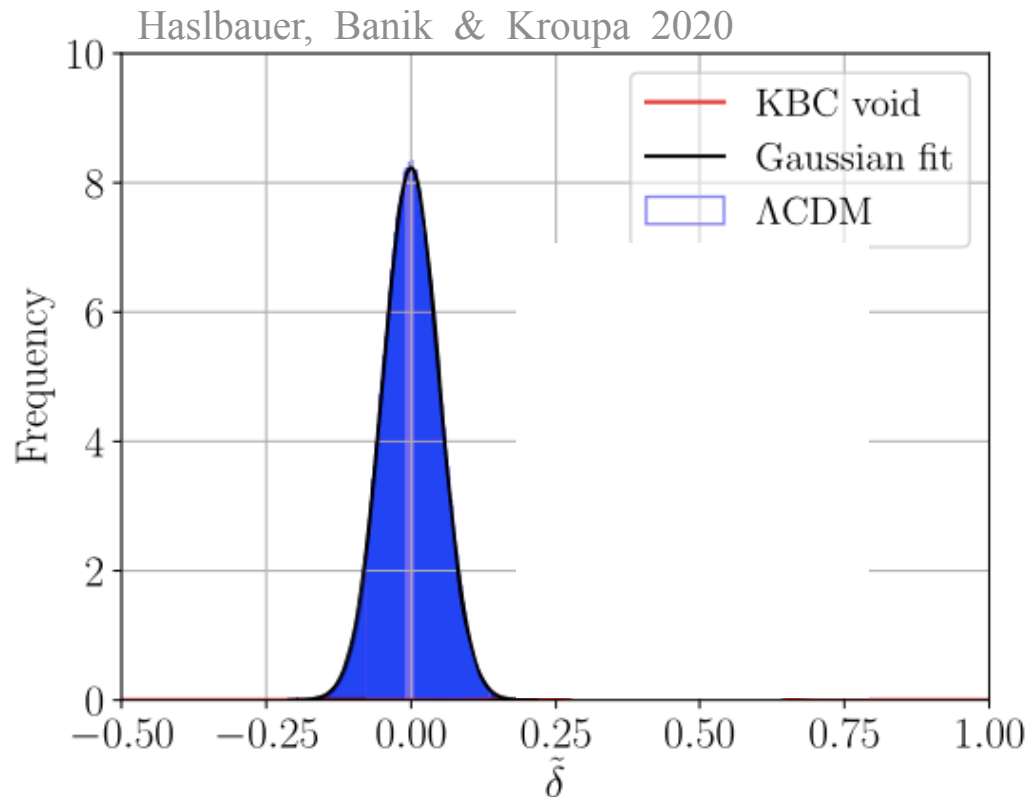
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Haslbauer, Banik & Kroupa 2020

# KBC void and Hubble Tension

## The Cosmological Scale

### The KBC Void + Hubble Tension

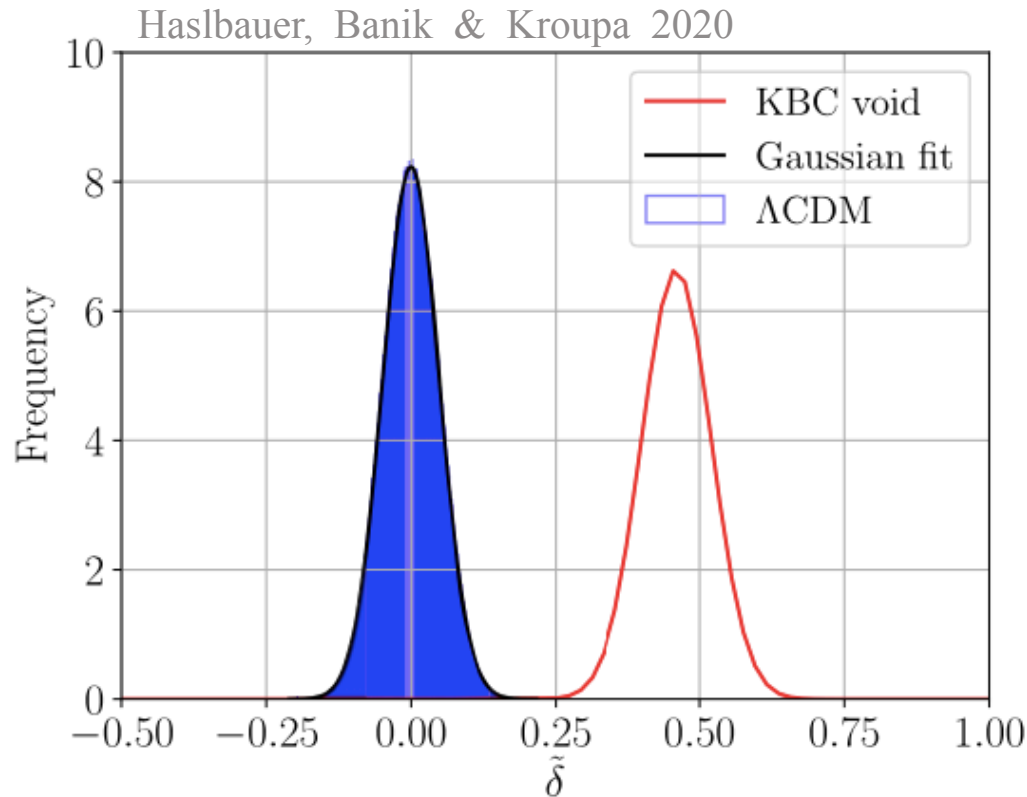


**Figure 1.** Distribution of the apparent relative density contrast  $\tilde{\delta}$  (equation 22) of spheres with a 300 Mpc radius less an inner 40 Mpc hole in the  $\Lambda$ CDM MXXL simulation, calculated at redshift  $z = 0$  (Section 2.1). The red solid curve shows the observed density contrast of  $\delta_{\text{obs}} = 0.46 \pm 0.06$  with Gaussian errors (see also fig. 11 and table 1 in Keenan et al. 2013). The  $\tilde{\delta}$  values closely follow a Gaussian distribution with a dispersion of  $\sigma_{\Lambda\text{CDM}} = 0.048$  (the black curve). A more detailed Gaussianity test is performed in Appendix A. Both curves are normalized to the same area.

# KBC void and Hubble Tension

The Cosmological Scale

The KBC Void + Hubble Tension

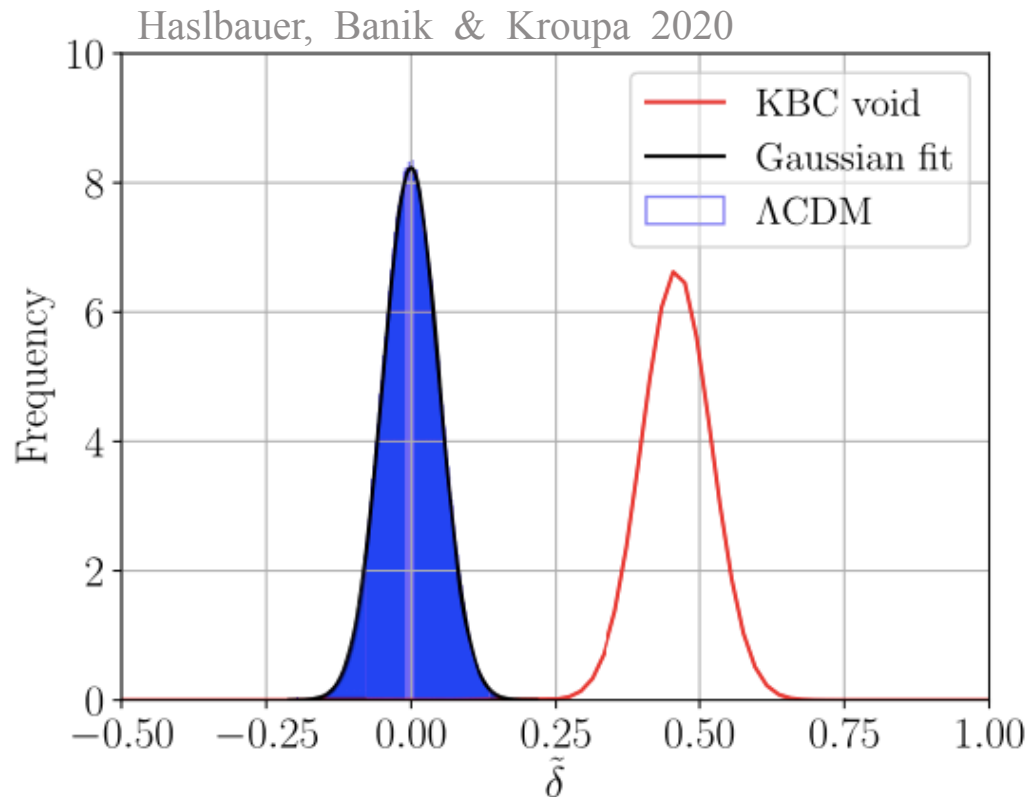


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# KBC void and Hubble Tension

The Cosmological Scale

The KBC Void + Hubble Tension



Difference of **>6 sigma**

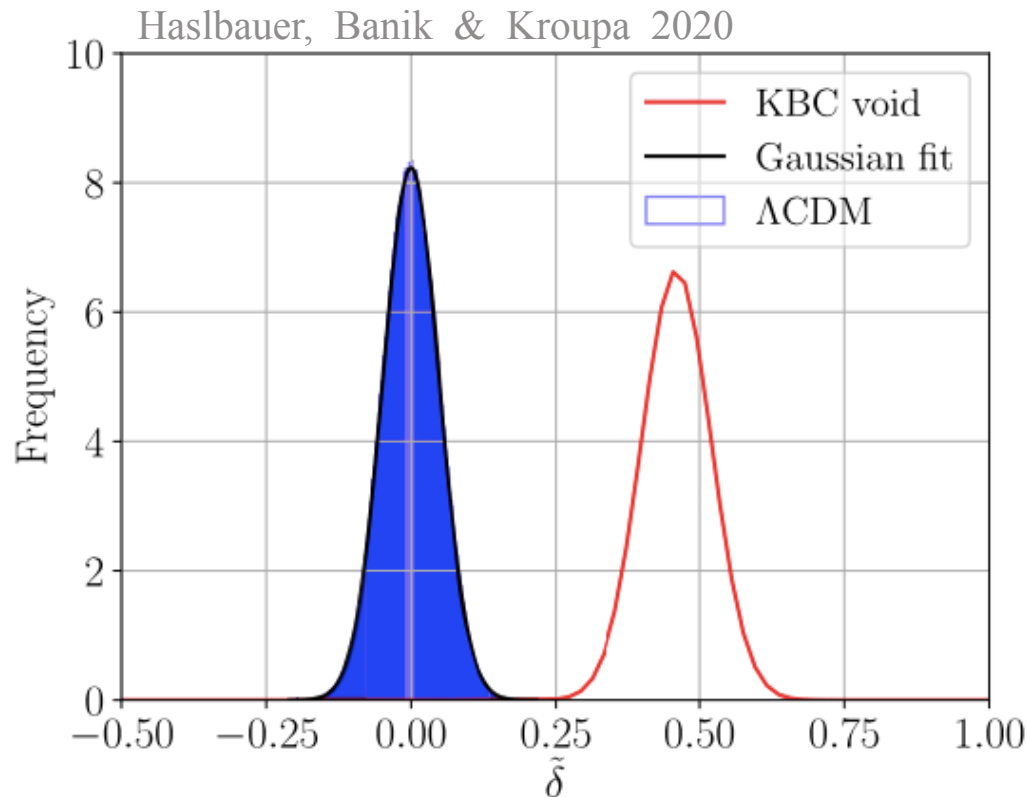
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The Cosmological Scale

The KBC Void + Hubble Tension



Difference of  $>6$  sigma

Not SMOc at  $>6\sigma$  confidence

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# KBC void and Hubble Tension

The Cosmological Scale

Haslbauer, Banik &  
Kroupa 2020 ;  
Mazurenko, Banik  
et al. 2023

# KBC void and Hubble Tension

The Cosmological Scale

Haslbauer, Banik &  
Kroupa 2020 ;  
Mazurenko, Banik  
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observed KBC void

diameter:  $\approx 1$  Gpc

density contrast:  $\approx 50\%$

---



# KBC void and Hubble Tension

The Cosmological Scale

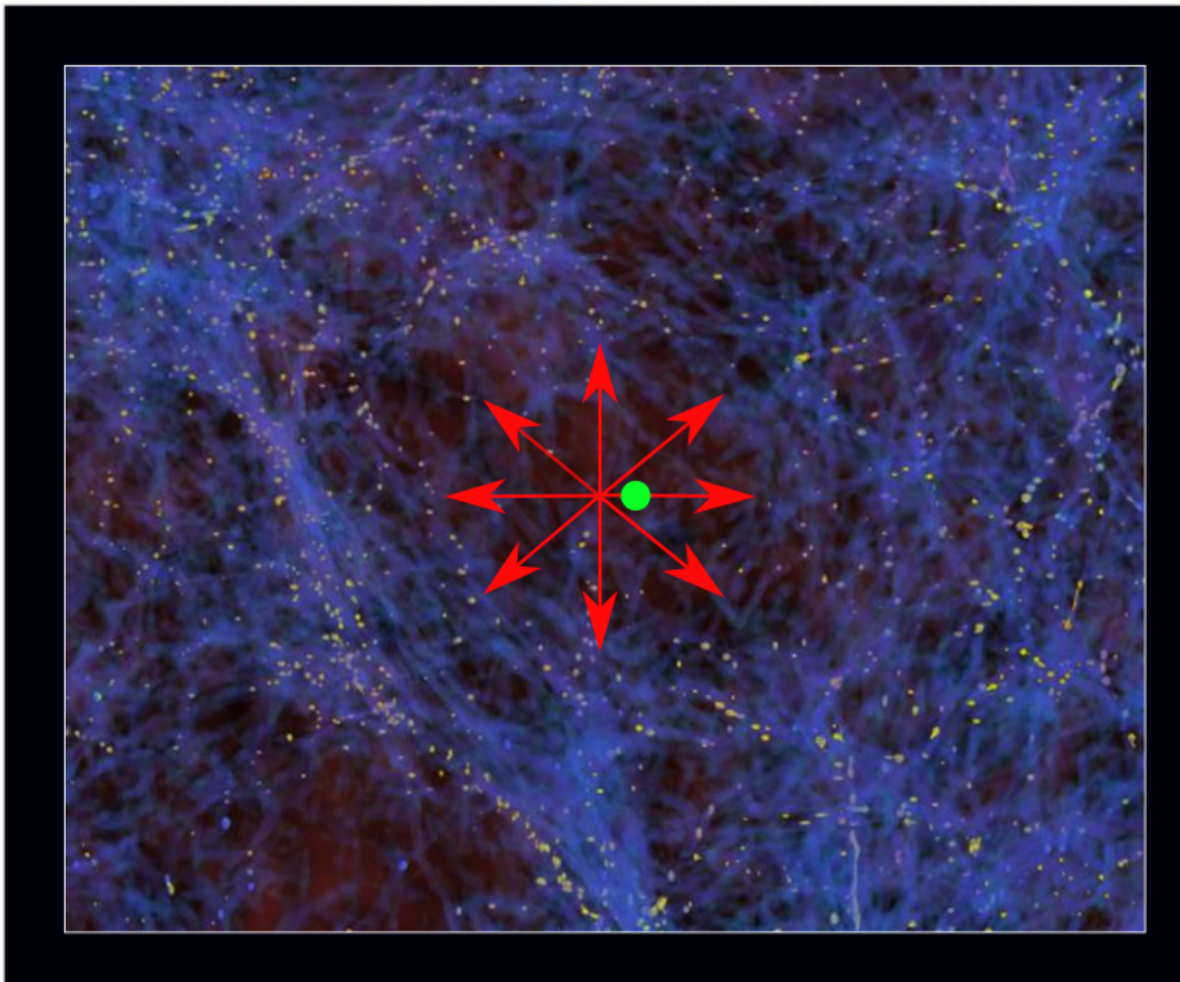
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there exists no Hubble Tension !!!



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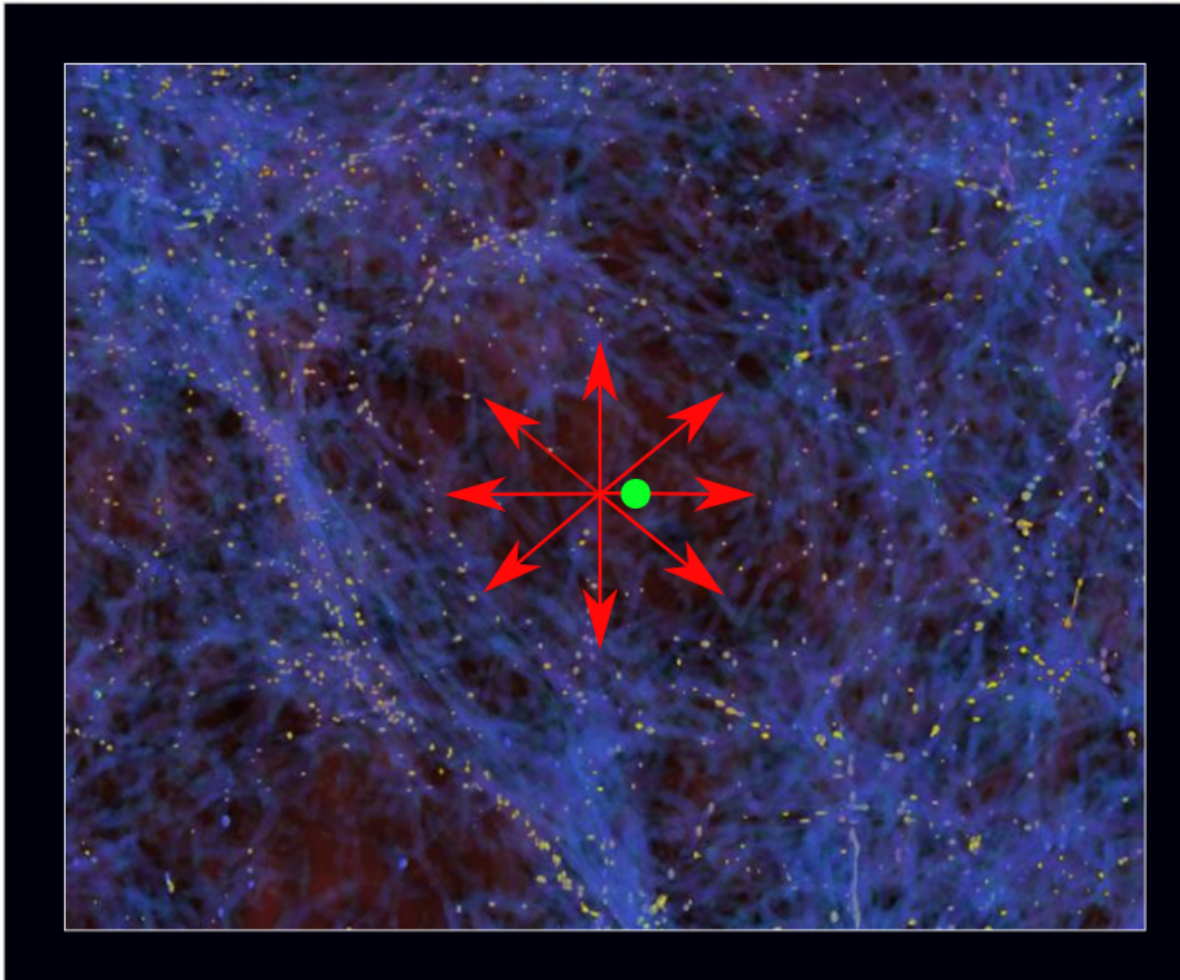
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The KBC void  
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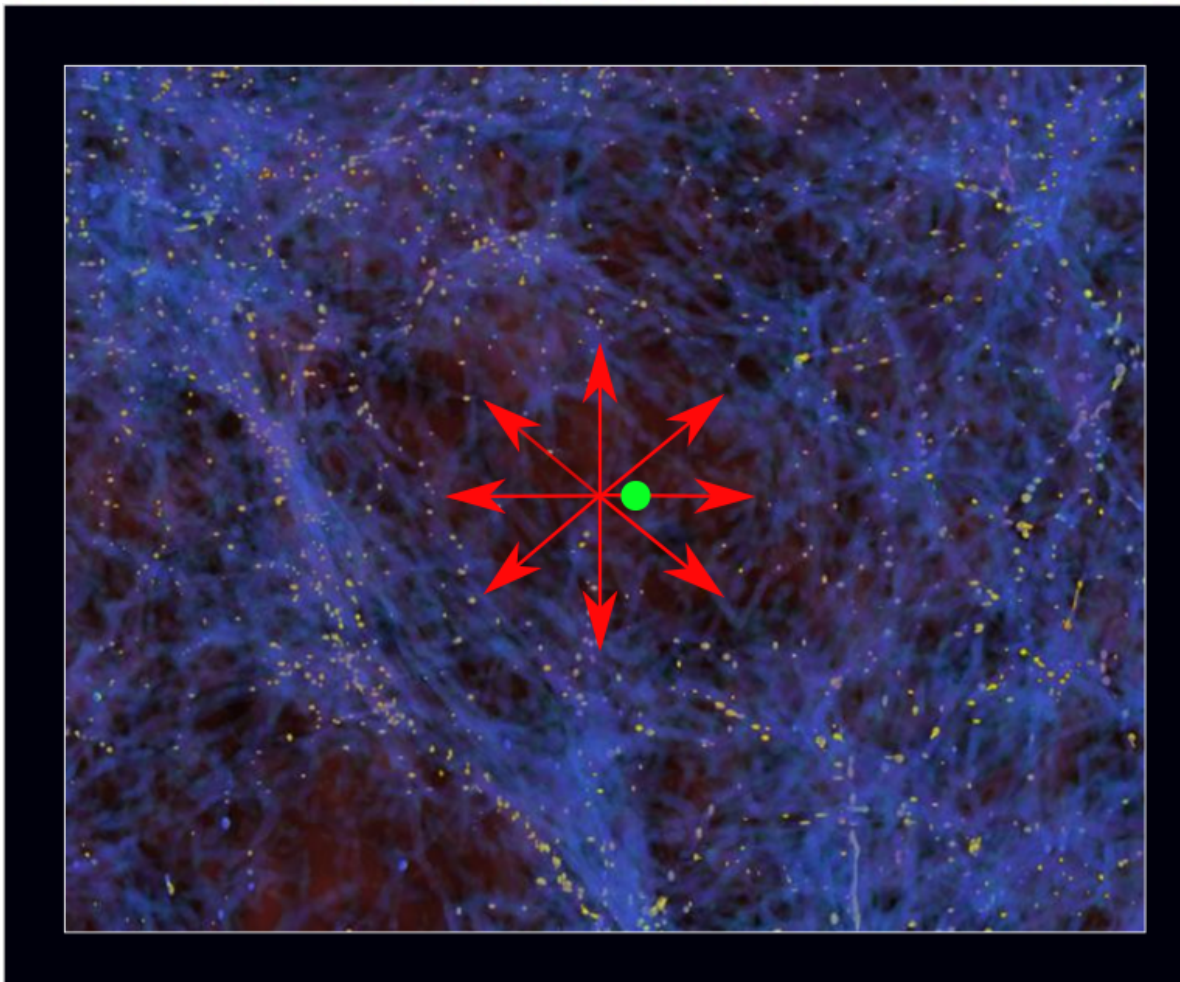
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Bulk flows of galaxies  
correctly predicted  
in this model

Mazurenko, Banik  
et al. 2023

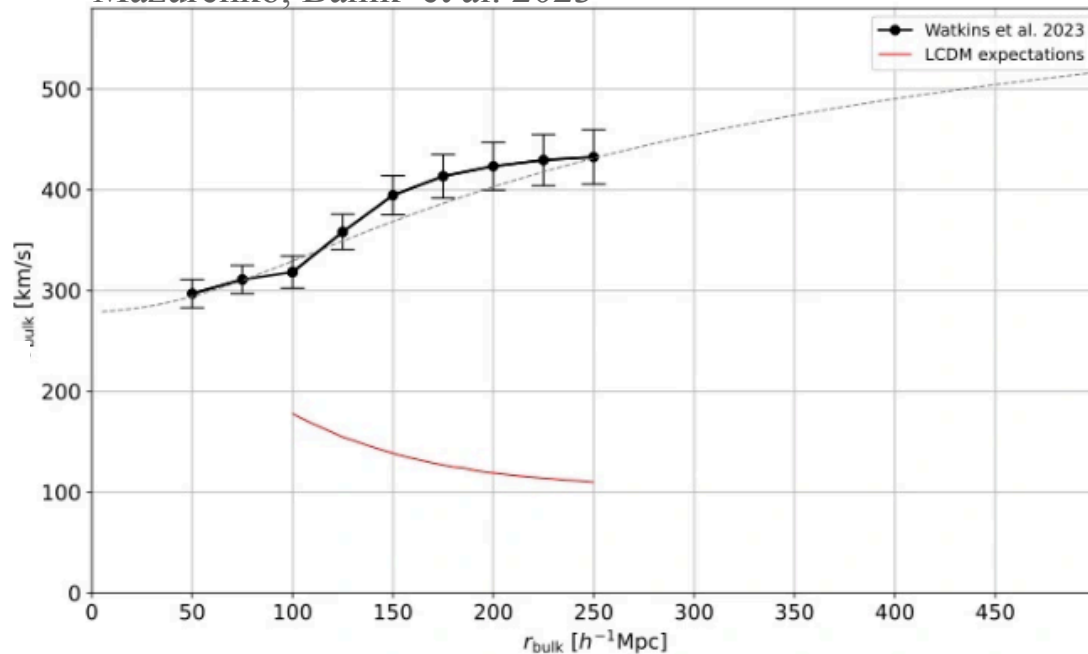


# KBC void and Hubble Tension

## The Cosmological Scale

Haslbauer, Banik &  
Kroupa 2020 ;  
Mazurenko, Banik  
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Mazurenko, Banik et al. 2023



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3: The bulk flow of galaxies (the average speed of many galaxies, y-axis) is plotted versus the distance from the observer on the x-axis. The data from [Watkins et al. \(2023\)](#) are shown as solid black circles. The MOND-based cosmological model is shown as the dotted line assuming the local void has a specific density profile, that the Local Group is located 116 Mpc (about 380 million light years) away from the void centre and that the Local Group is moving with 627 km/s relative to the CMB and about 200 km/s slower than the local bulk flow (within some 150 million light years). In other words, the Local Group's velocity relative to the CMB has been reduced to 627 km/s by small-scale flows in the local region. Thus, the MOND-cosmology-based bulk flow (dotted black line) is in (stunning) agreement with the data in terms of its amplitude and shape, while the LCDM model predicts bulk velocities (solid red line) that are in major disagreement with the observations. Adapted from [Mazurenko et al. \(2023\)](#).

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Mazurenko, Banik  
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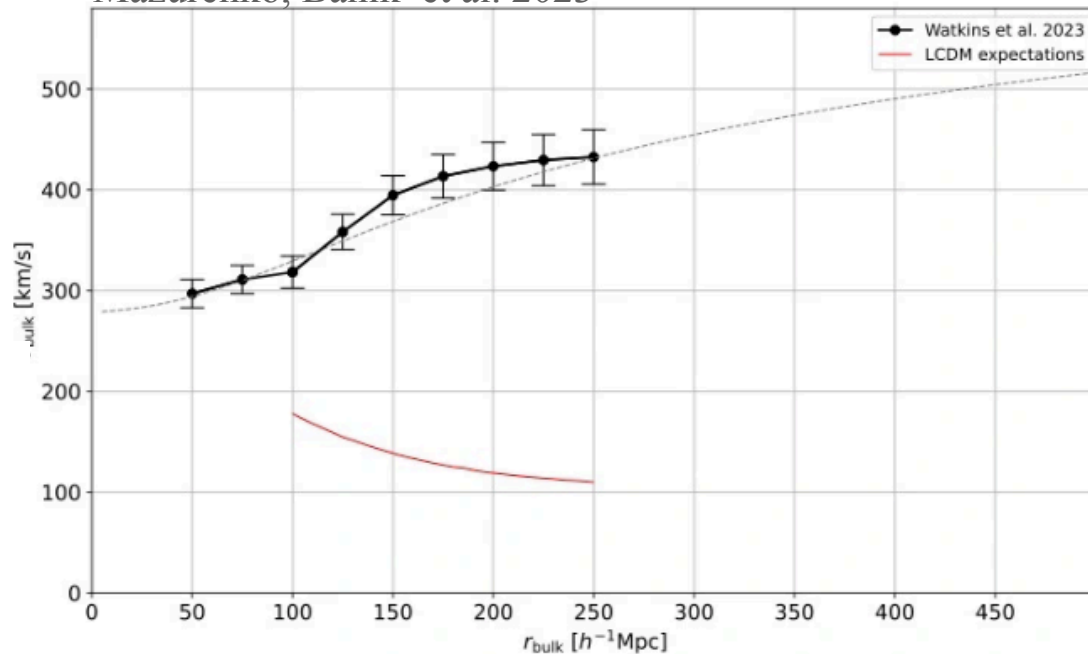
From The Dark Matter Crisis #86

# KBC void and Hubble Tension

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Haslbauer, Banik &  
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3: The bulk flow of galaxies (the average speed of many galaxies, y-axis) is plotted versus the distance from the observer on the x-axis. The data from [Watkins et al. \(2023\)](#) are shown as solid black circles. The MOND-based cosmological model is shown as the dotted line assuming the local void has a specific density profile, that the Local Group is located 116 Mpc (about 380 million light years) away from the void centre and that the Local Group is moving with 627 km/s relative to the CMB and about 200 km/s slower than the local bulk flow (within some 150 million light years). In other words, the Local Group's velocity relative to the CMB has been reduced to 627 km/s by small-scale flows in the local region. Thus, the MOND-cosmology-based bulk flow (dotted black line) is in (stunning) agreement with the data in terms of its amplitude and shape, while the LCDM model predicts bulk velocities (solid red line) that are in major disagreement with the observations. Adapted from [Mazurenko et al. \(2023\)](#).

From The Dark Matter Crisis #86

Bulk flows of galaxies  
correctly predicted  
in this model

Mazurenko, Banik  
et al. 2023

-----> talk by Indranil Banik  
on Wed.

The distribution of  
matter on scales  
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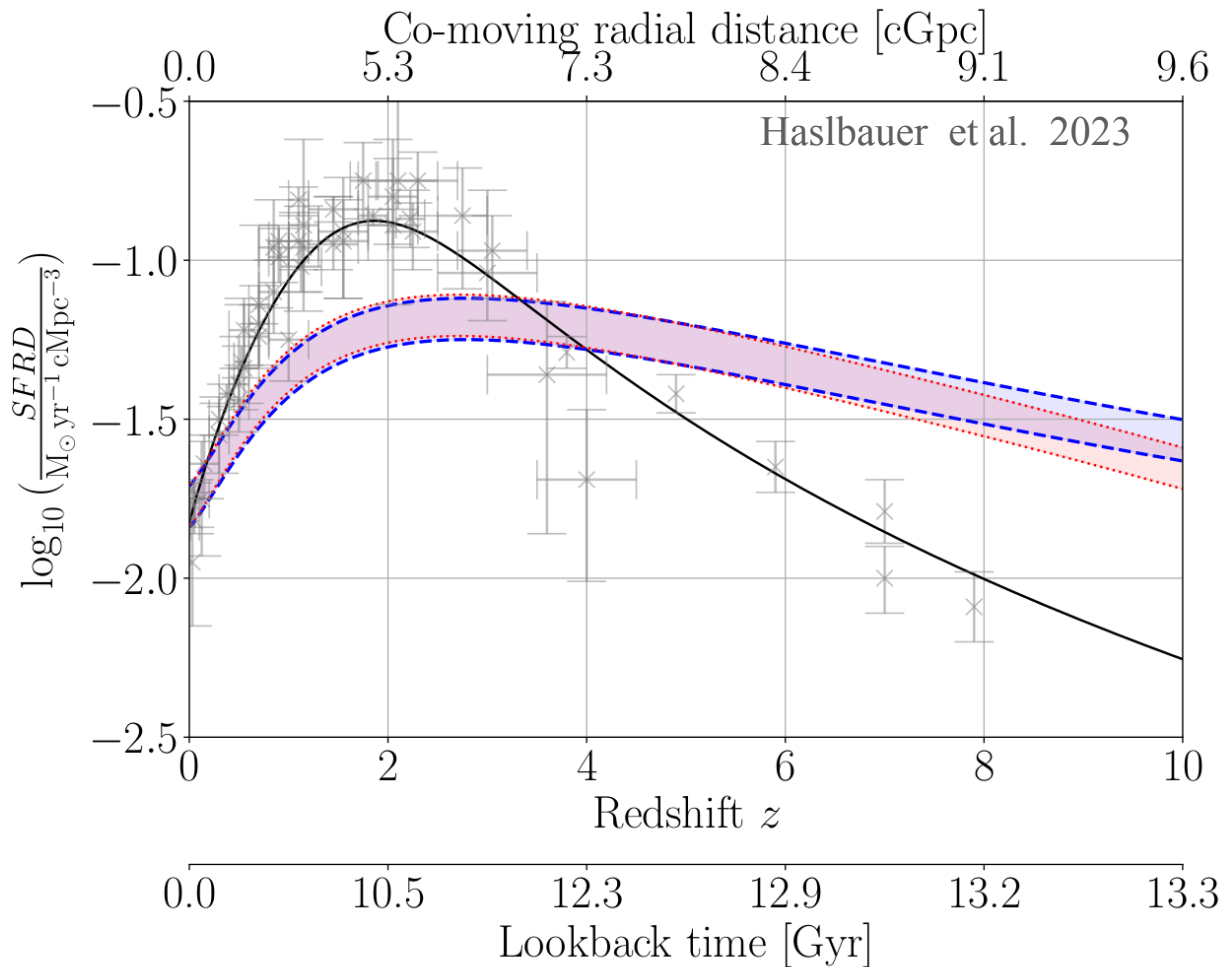
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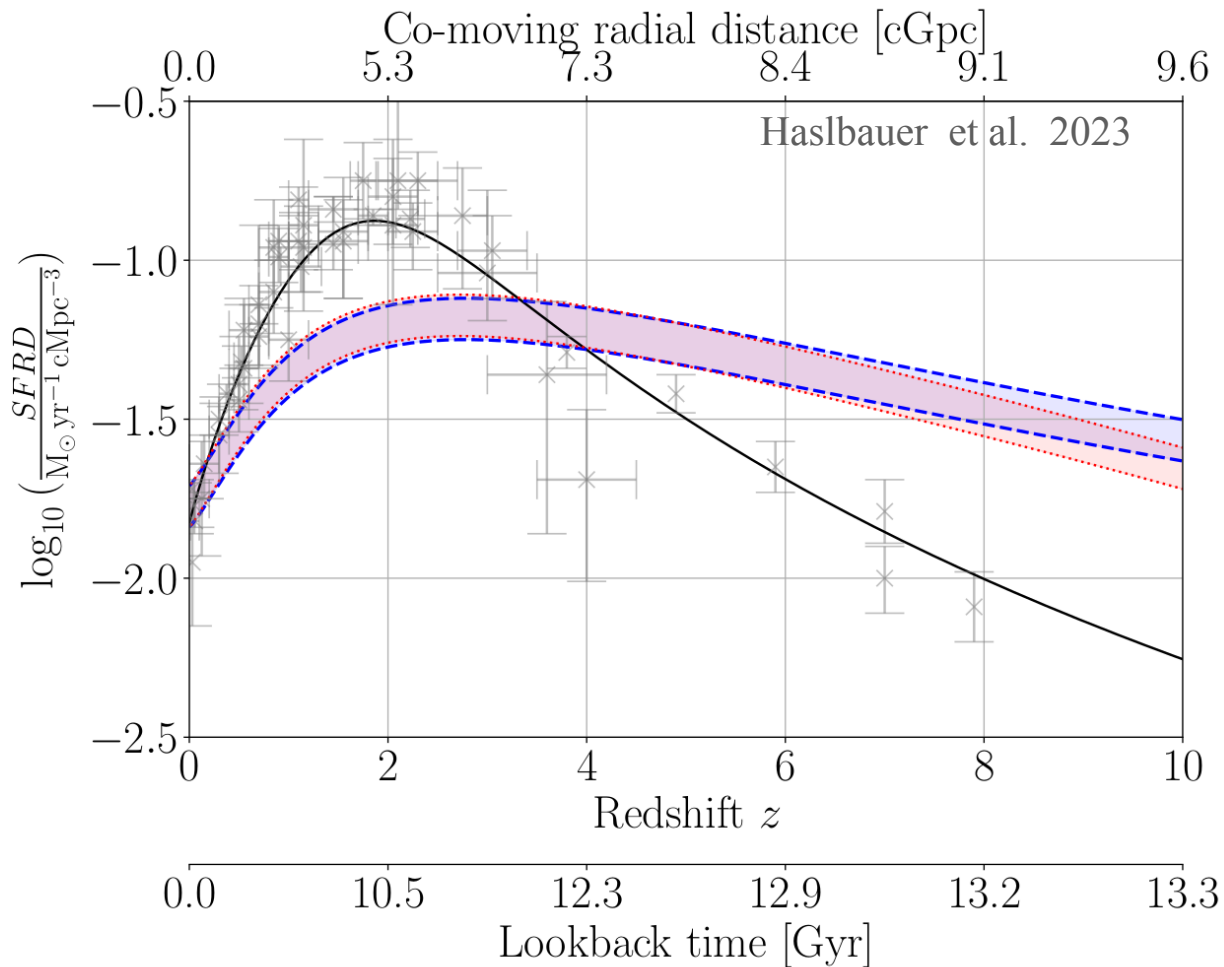
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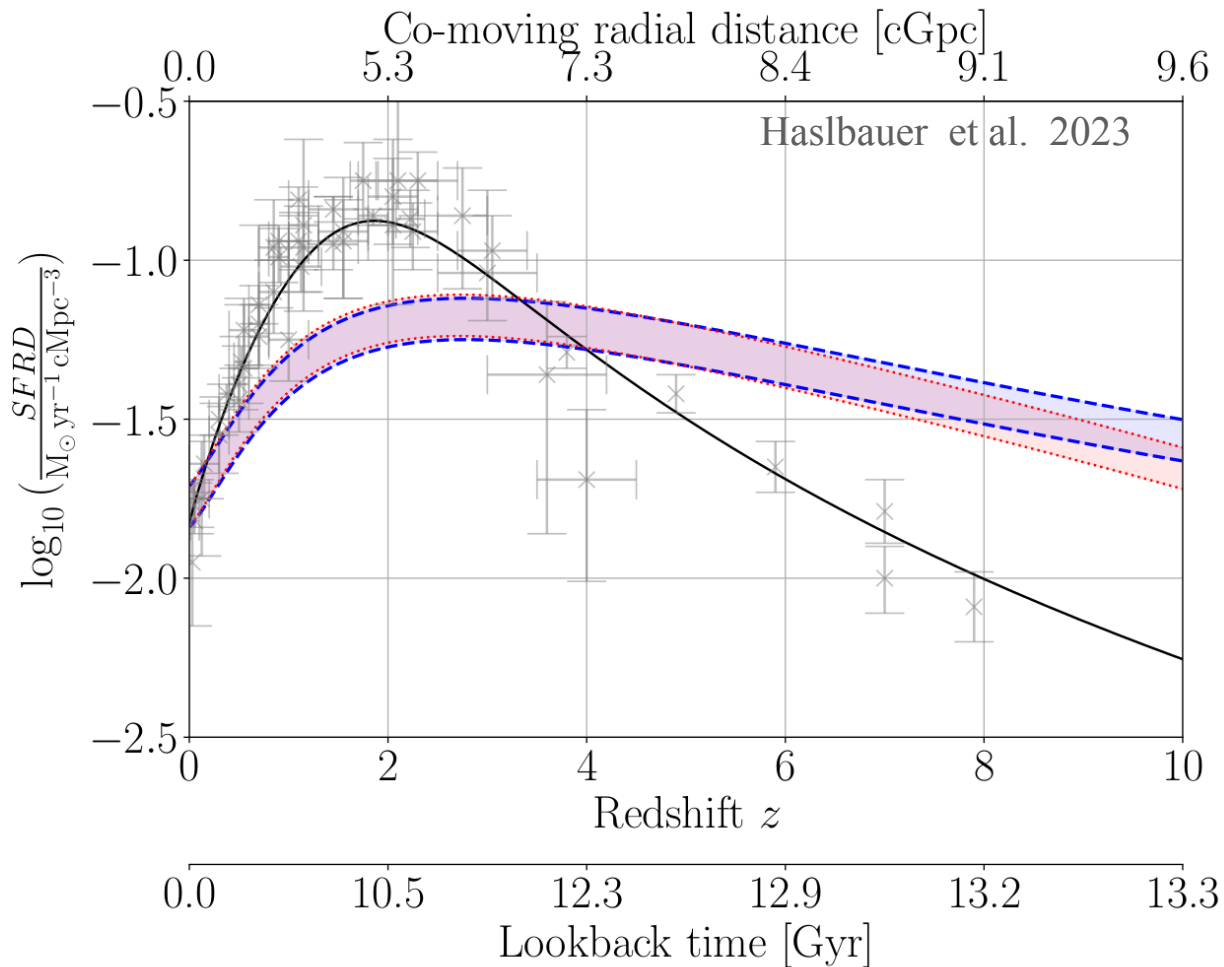


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➔ Not SMOc at  $\infty\sigma$  confidence.

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Schwarz et al. 2016

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(Yan, Jerabkova+2021 ; Eappen & Kr 2022).

# Overview of SMoC constraints

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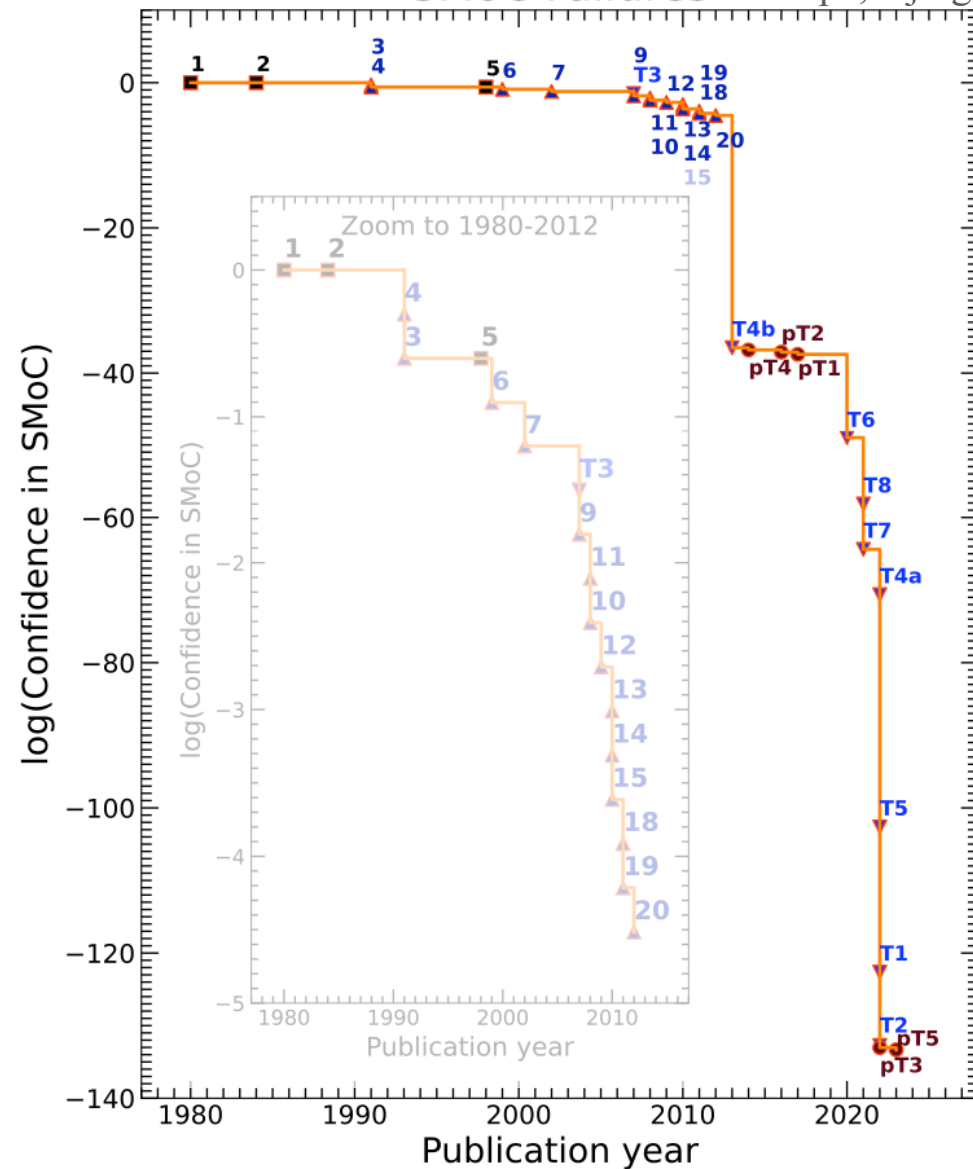
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## SMoC Failures Kroupa, Gjergo et al. 2023

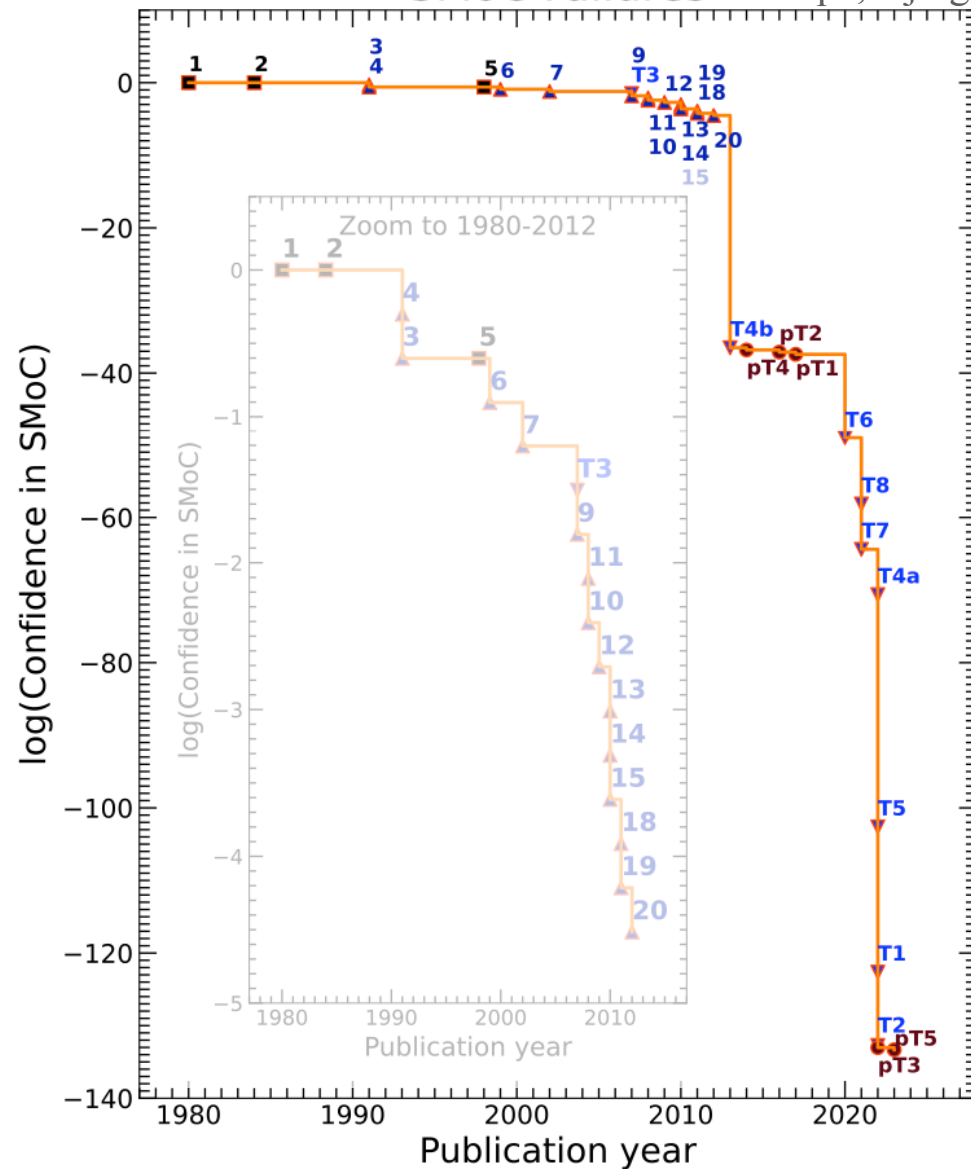


POS(CORFU2022)231

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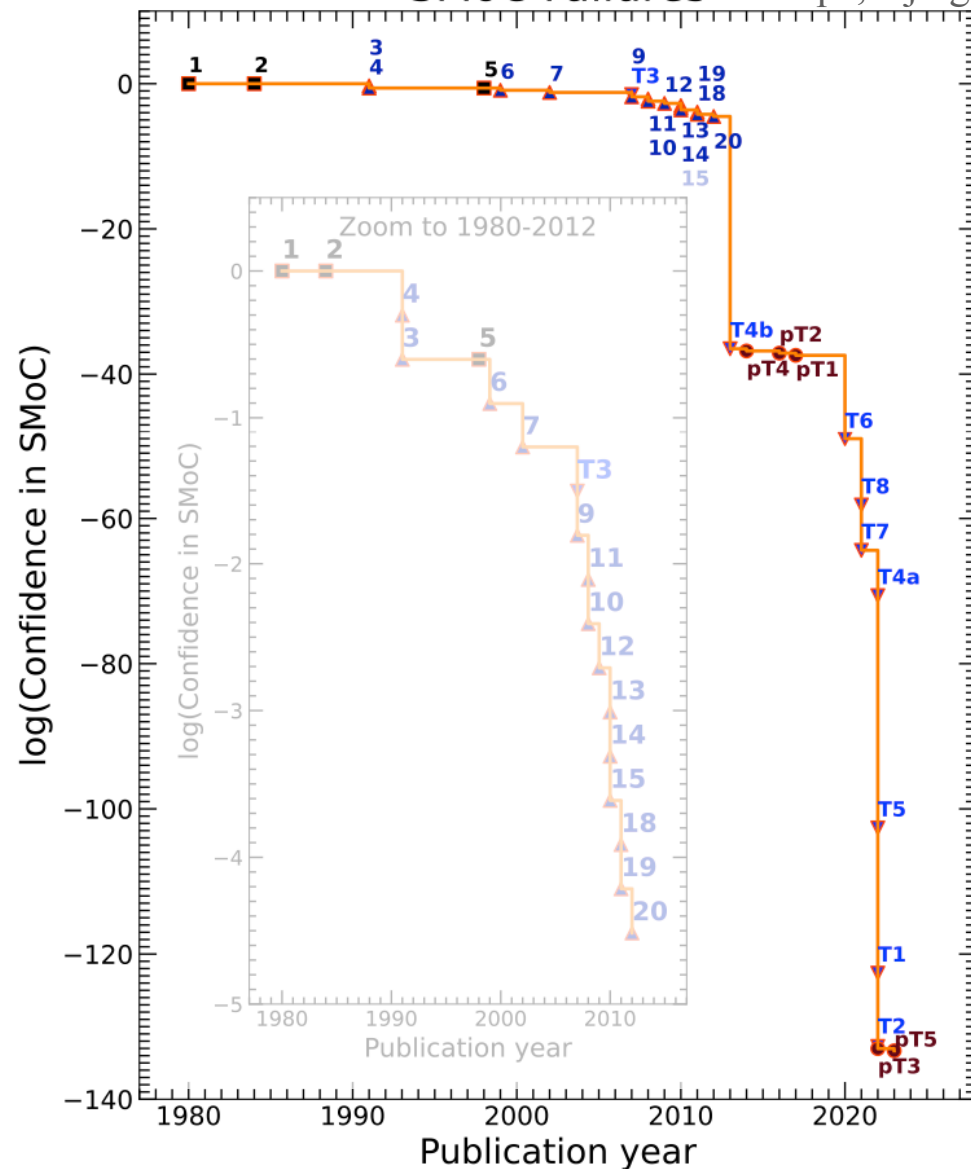
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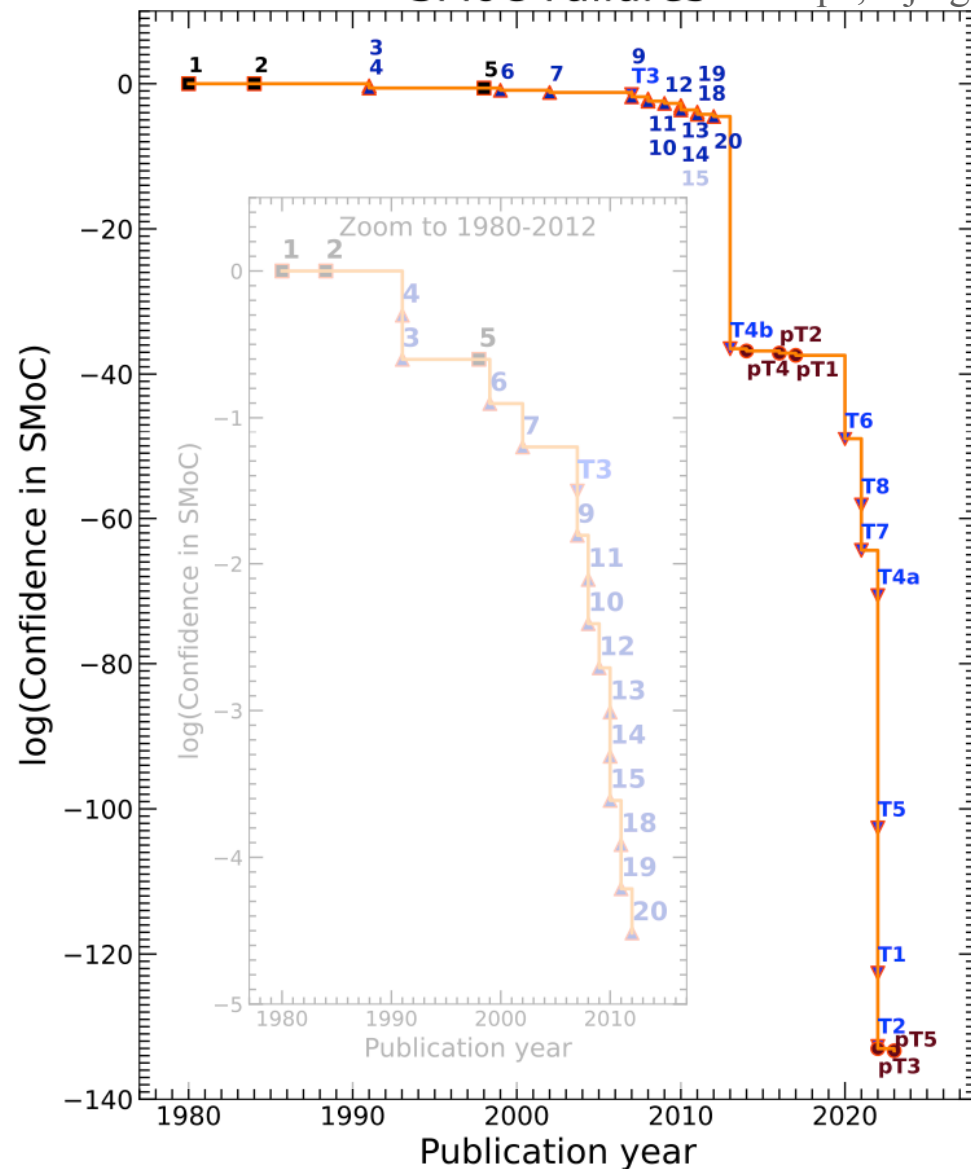
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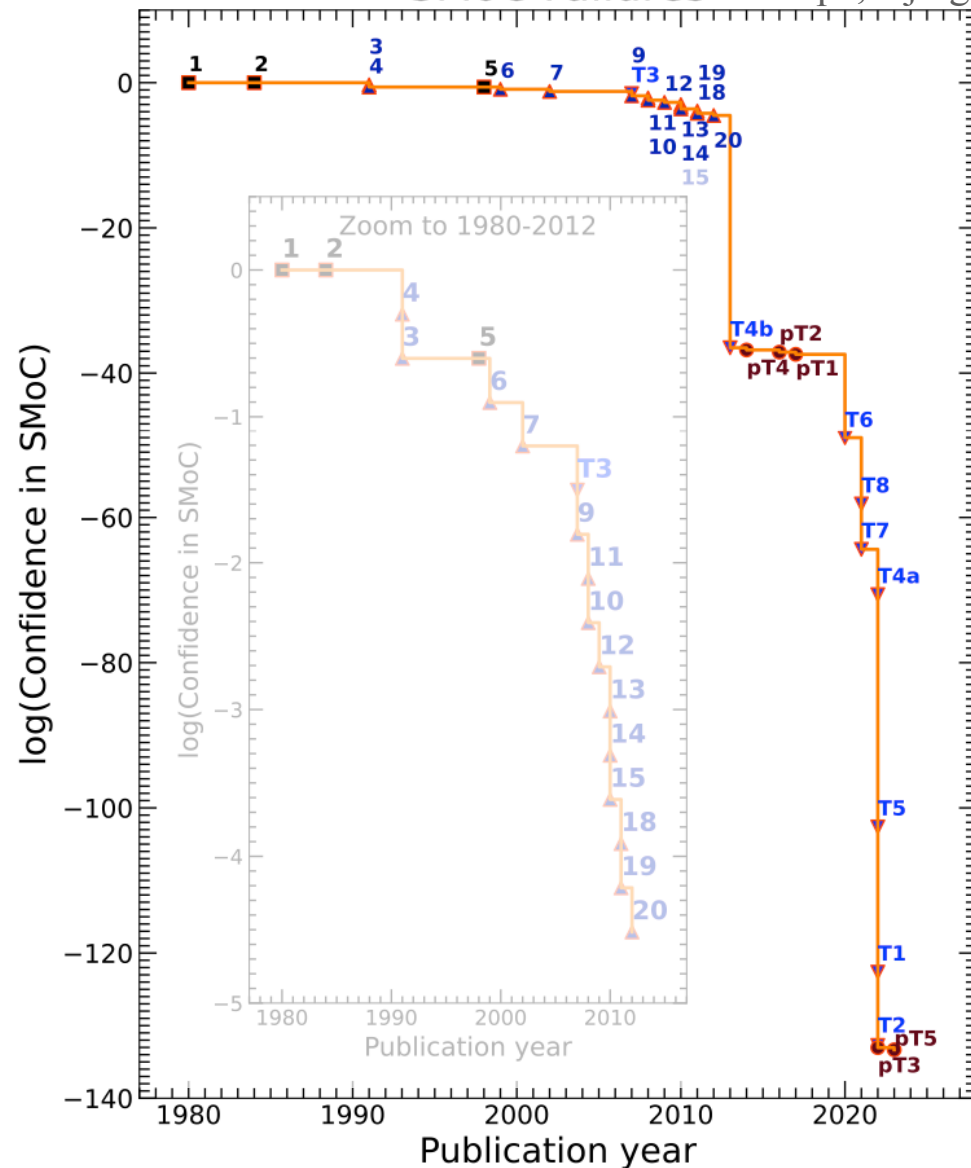
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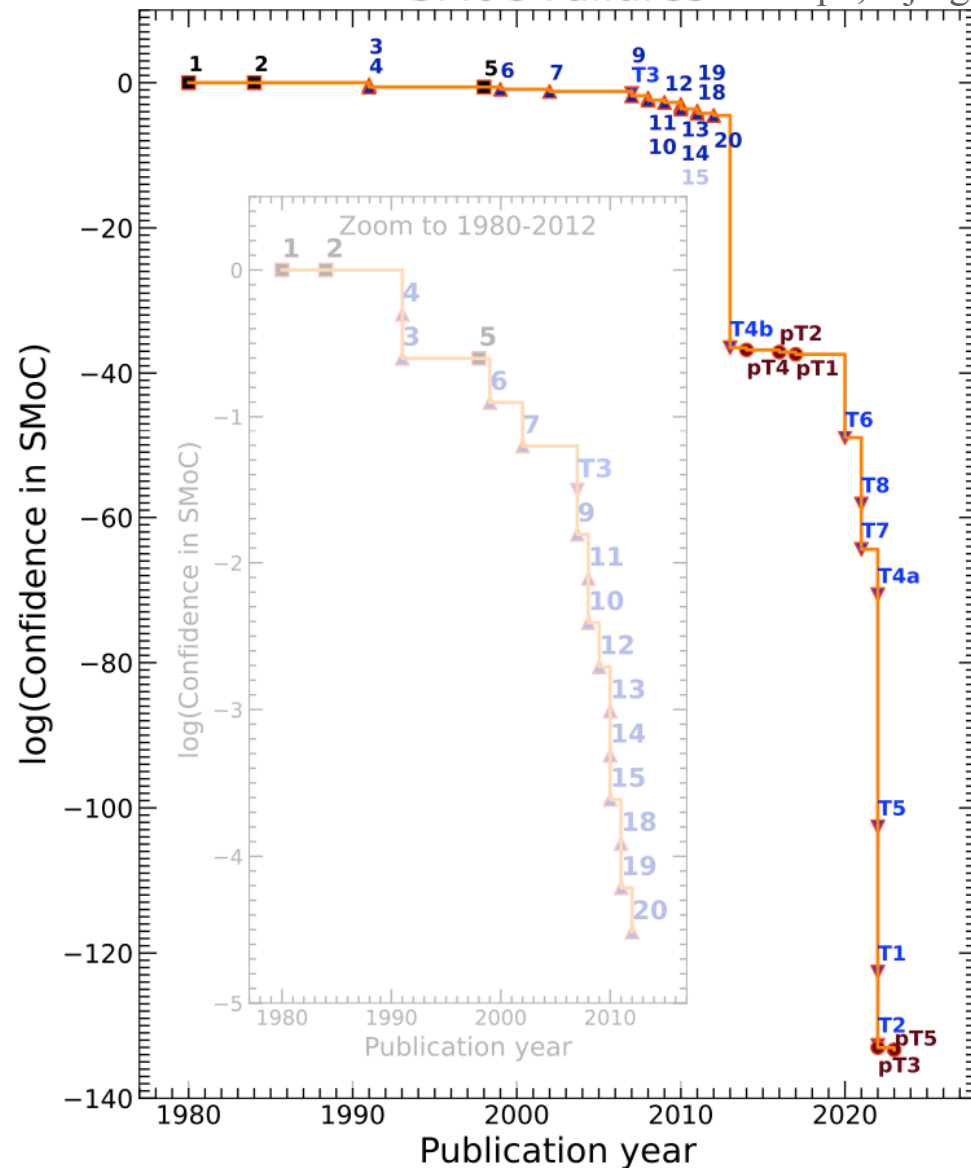
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Future outlook

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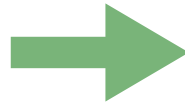


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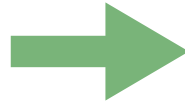
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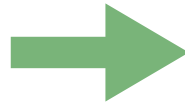
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Simulations : Katz, McGaugh et al. 2013 -- pure Nbody

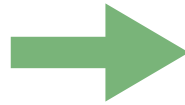
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Much work on this in Bonn and Prague

### 1) The **nuHDM model** :

with *inflation*, *dark energy* and *sterile neutrinos* as hot dark matter

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# Comparison on the Cosmological Scale

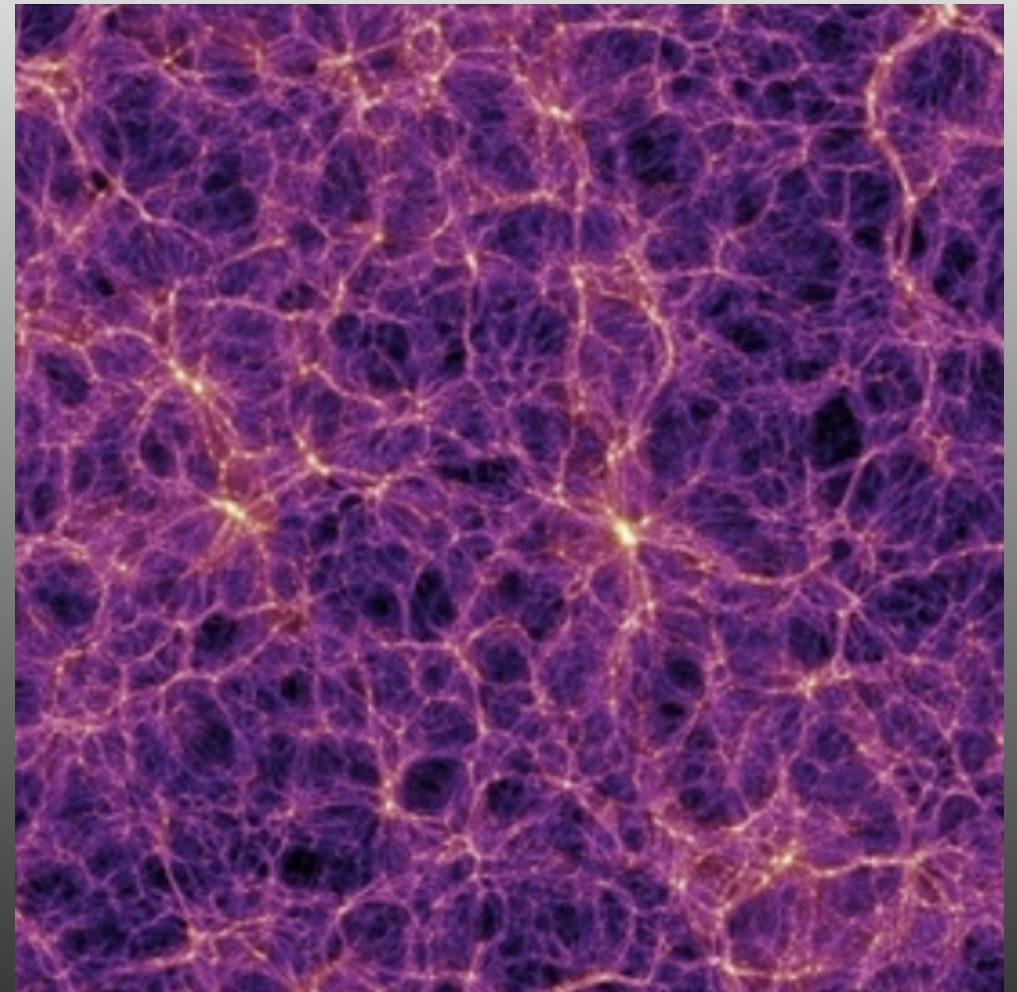
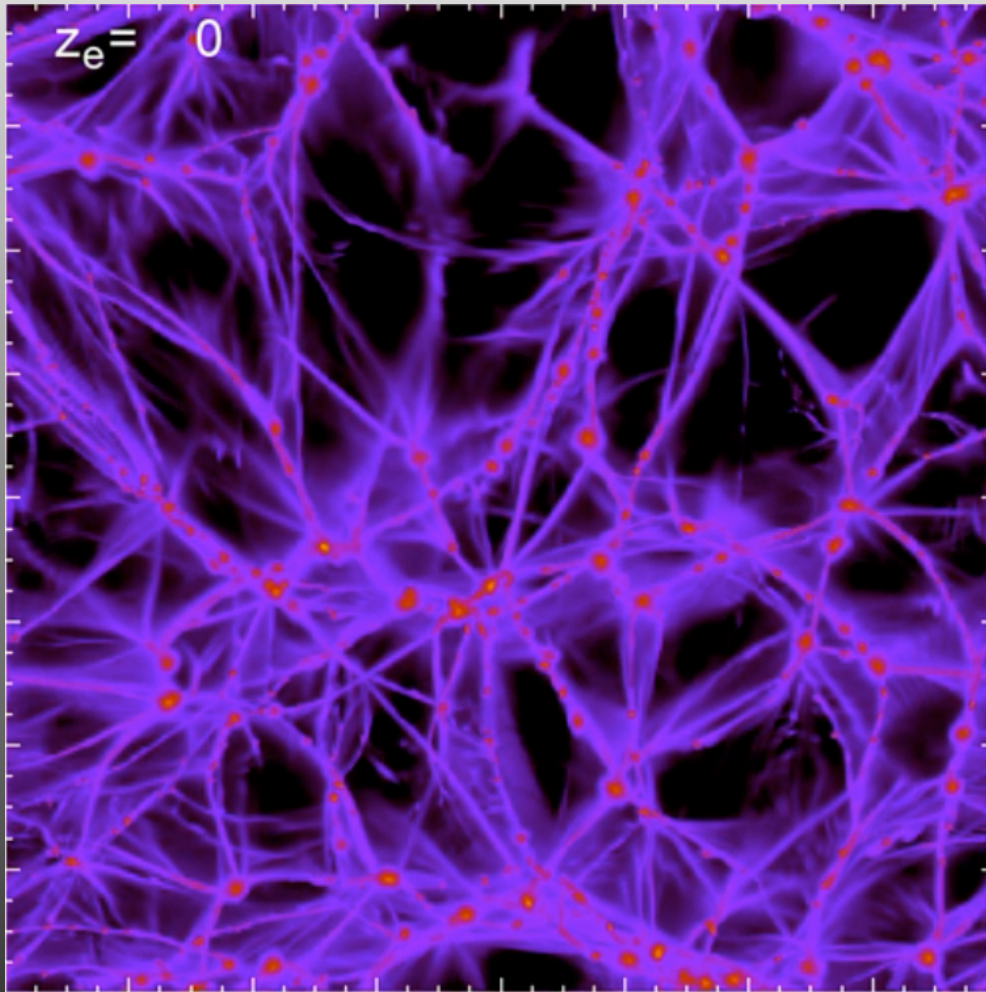
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400Mpc x 400Mpc

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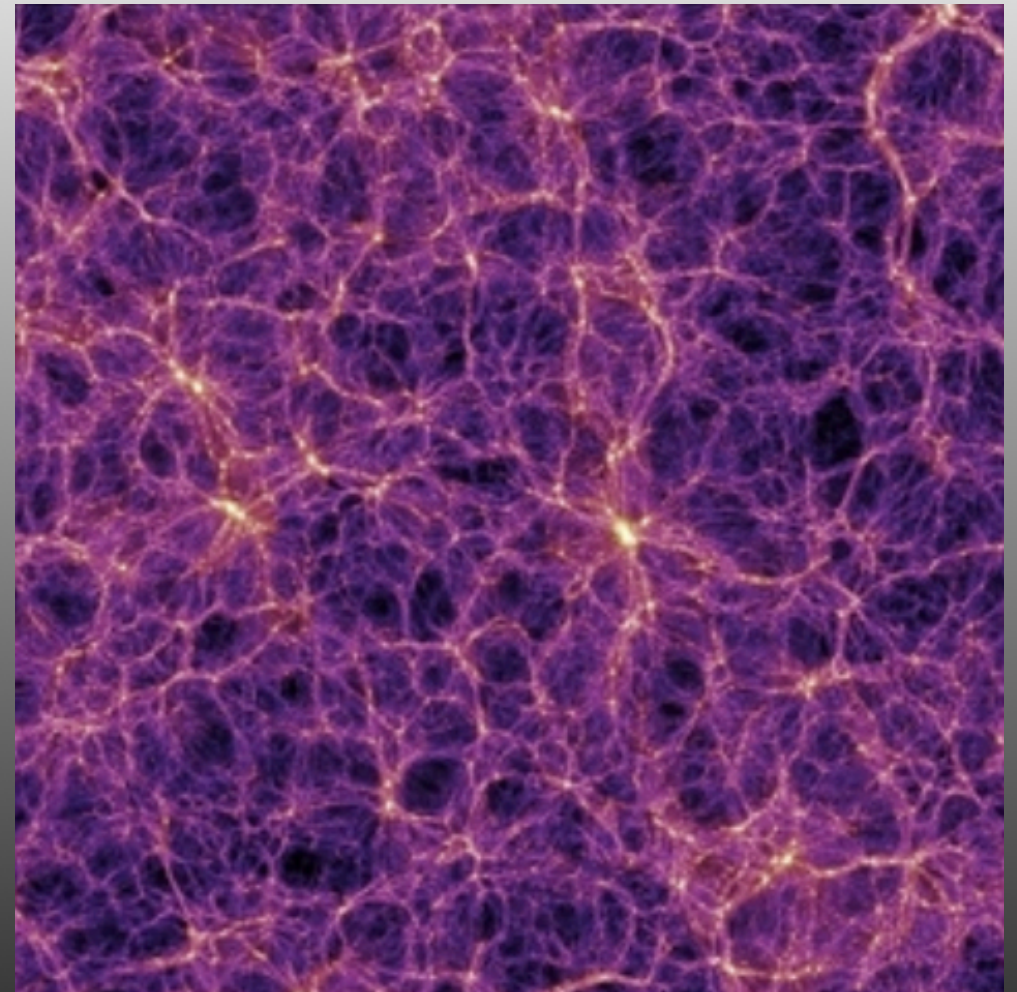
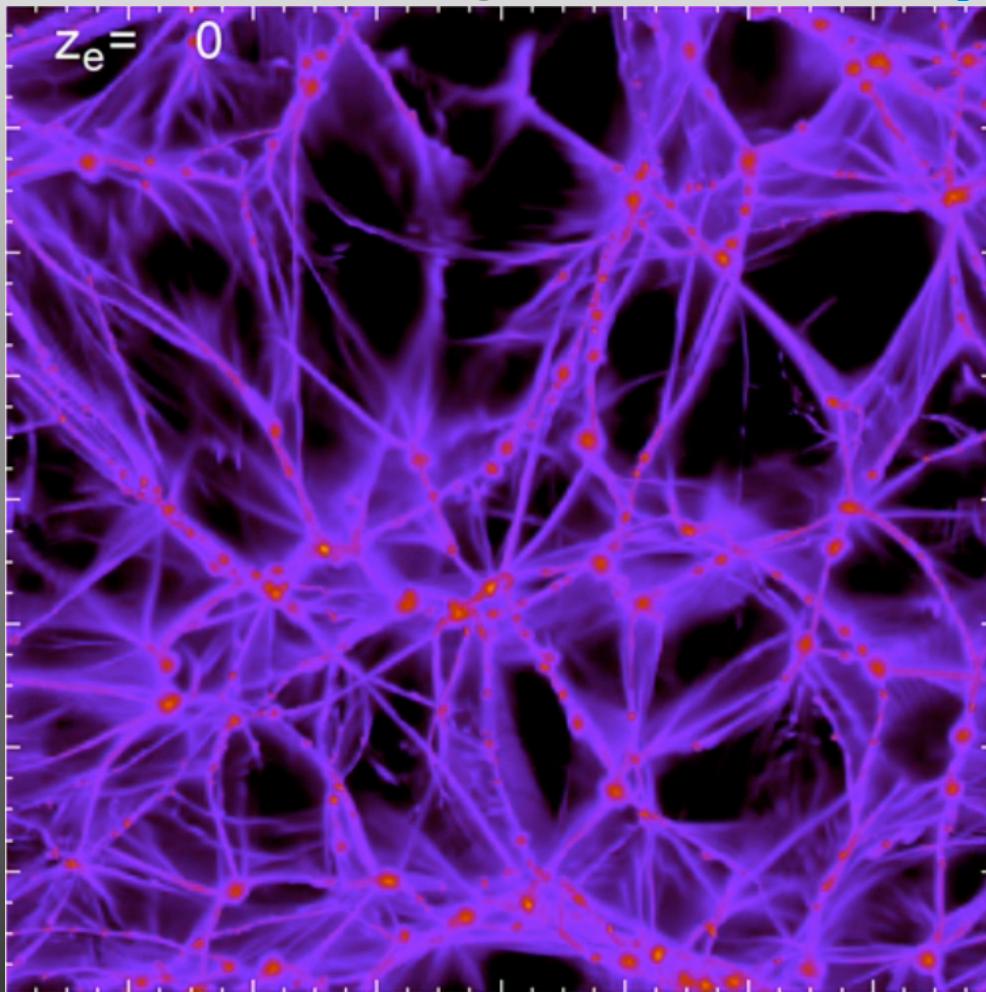
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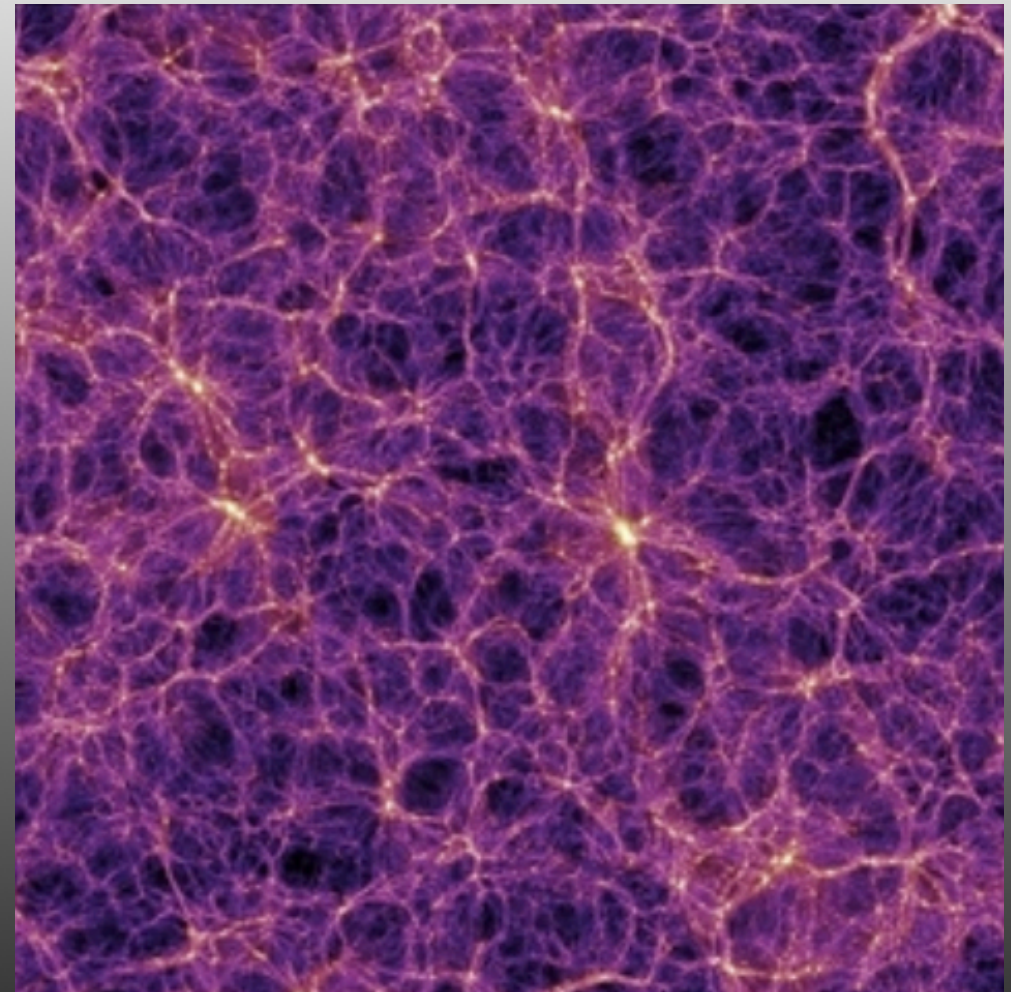
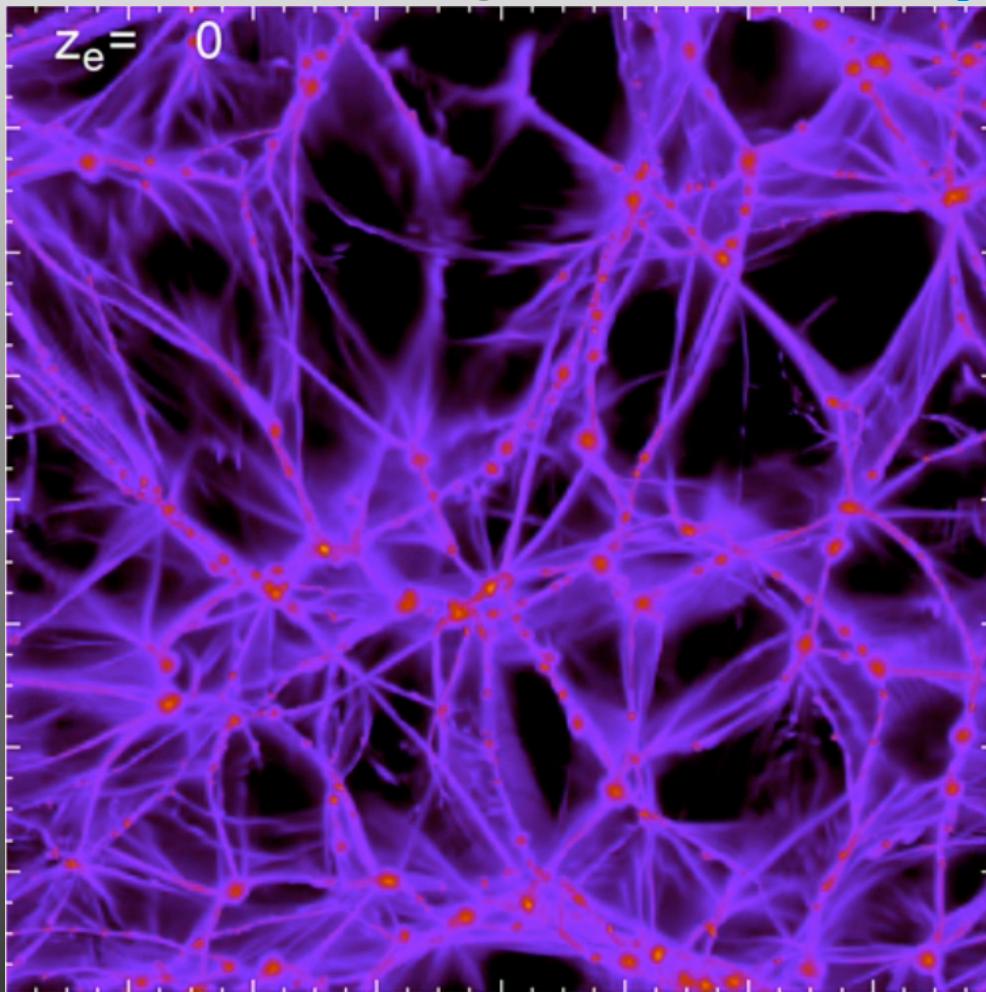
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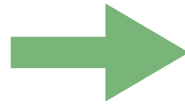
But, the model may be too homogeneous on scales  $>300\text{Mpc}$   
(compared to real Universe which is inhomogeneous on  $5\text{Gpc}$  scales)

LC/WDM is not on the table any longer !



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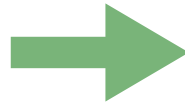


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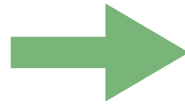
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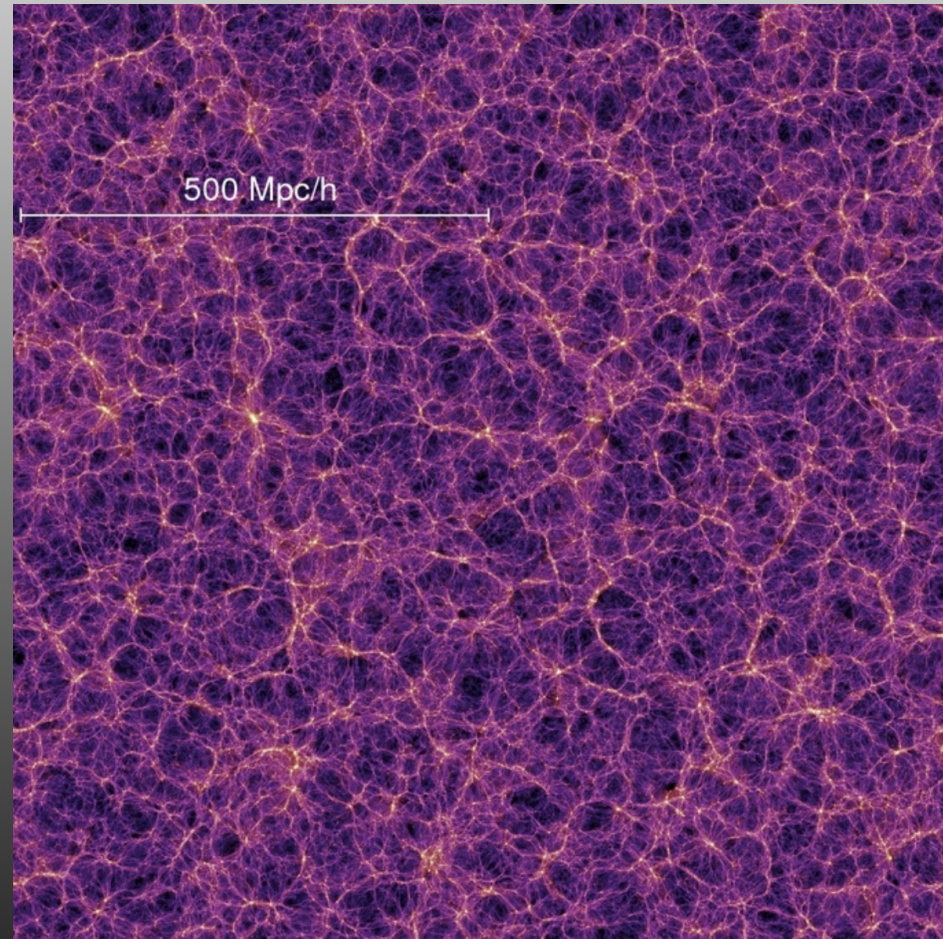
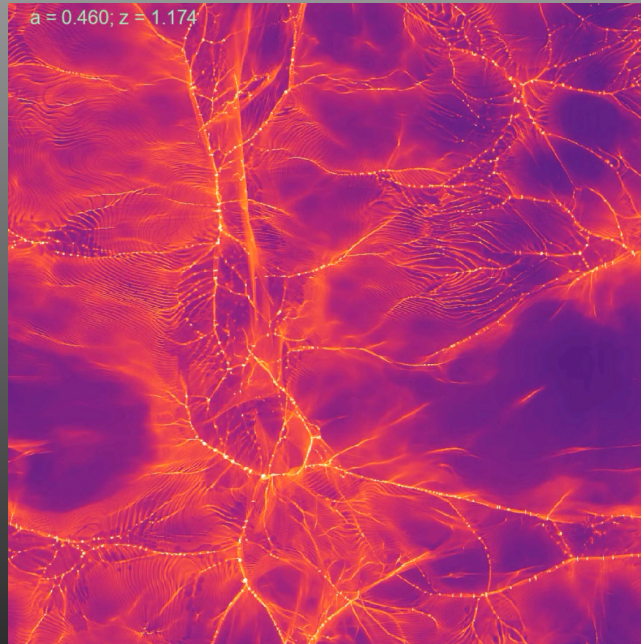
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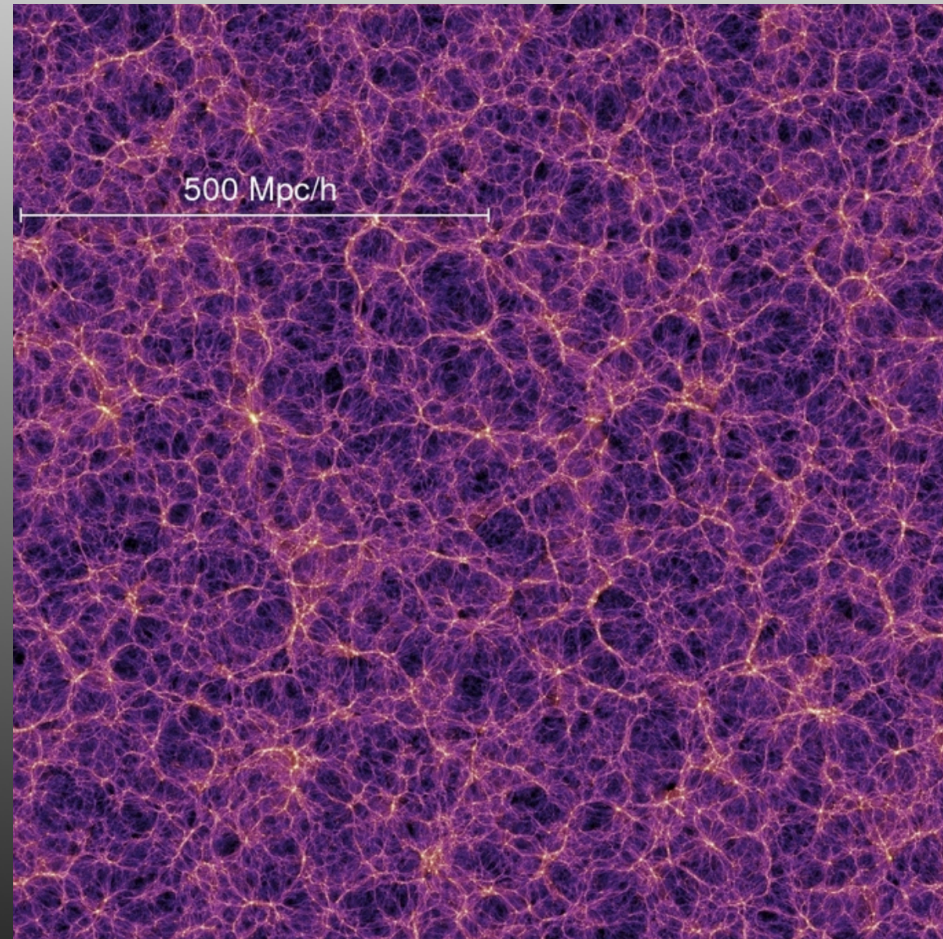
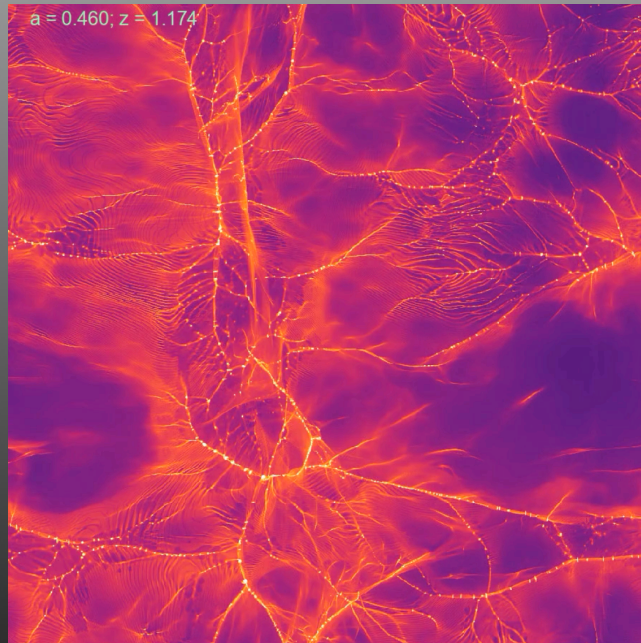
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The END

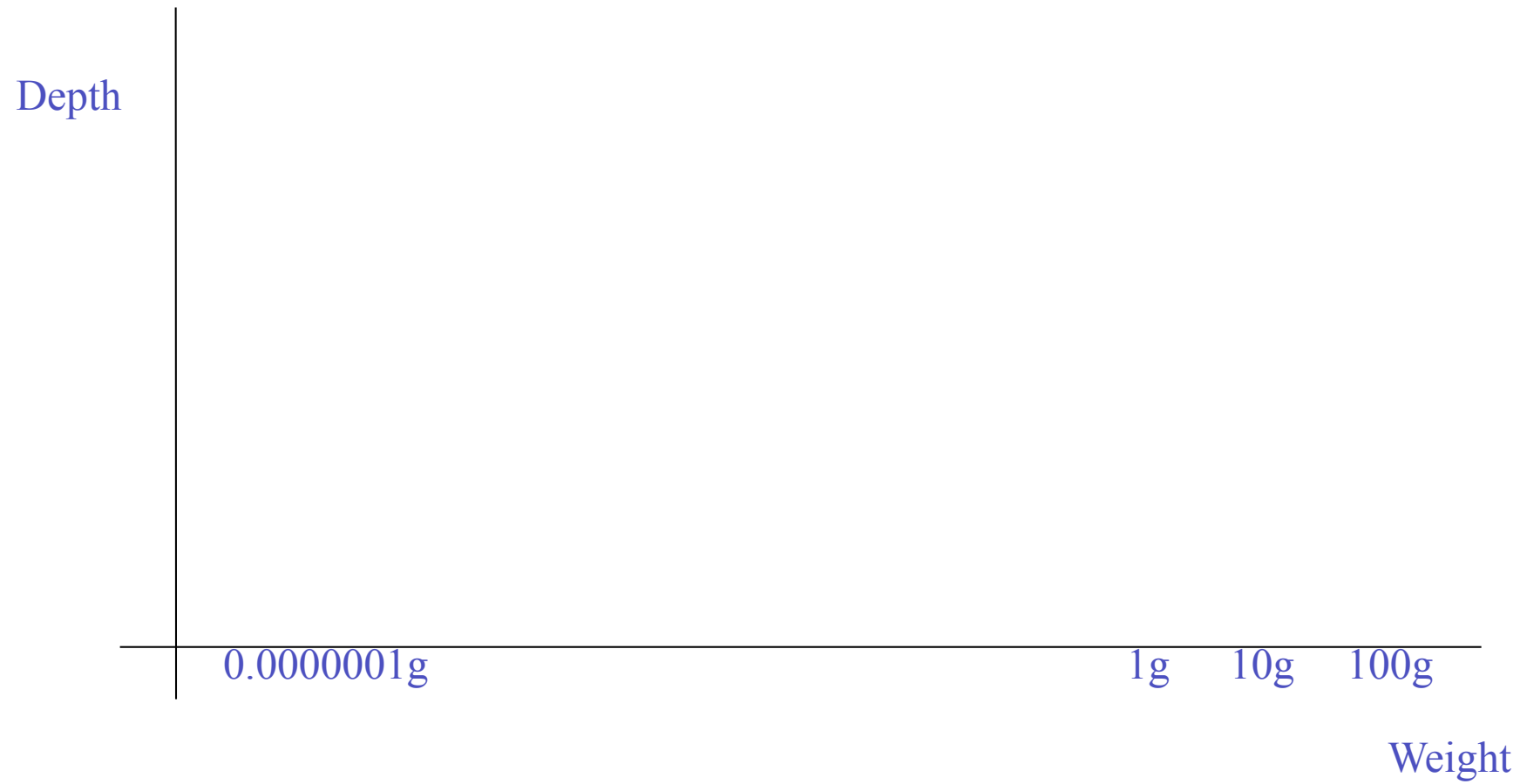
# Different-than-Newtonian dynamics or gravitation



Should one expect an empirical law to hold  
over an extrapolation of orders of  
magnitude ?

# *Gedankenexperiment*

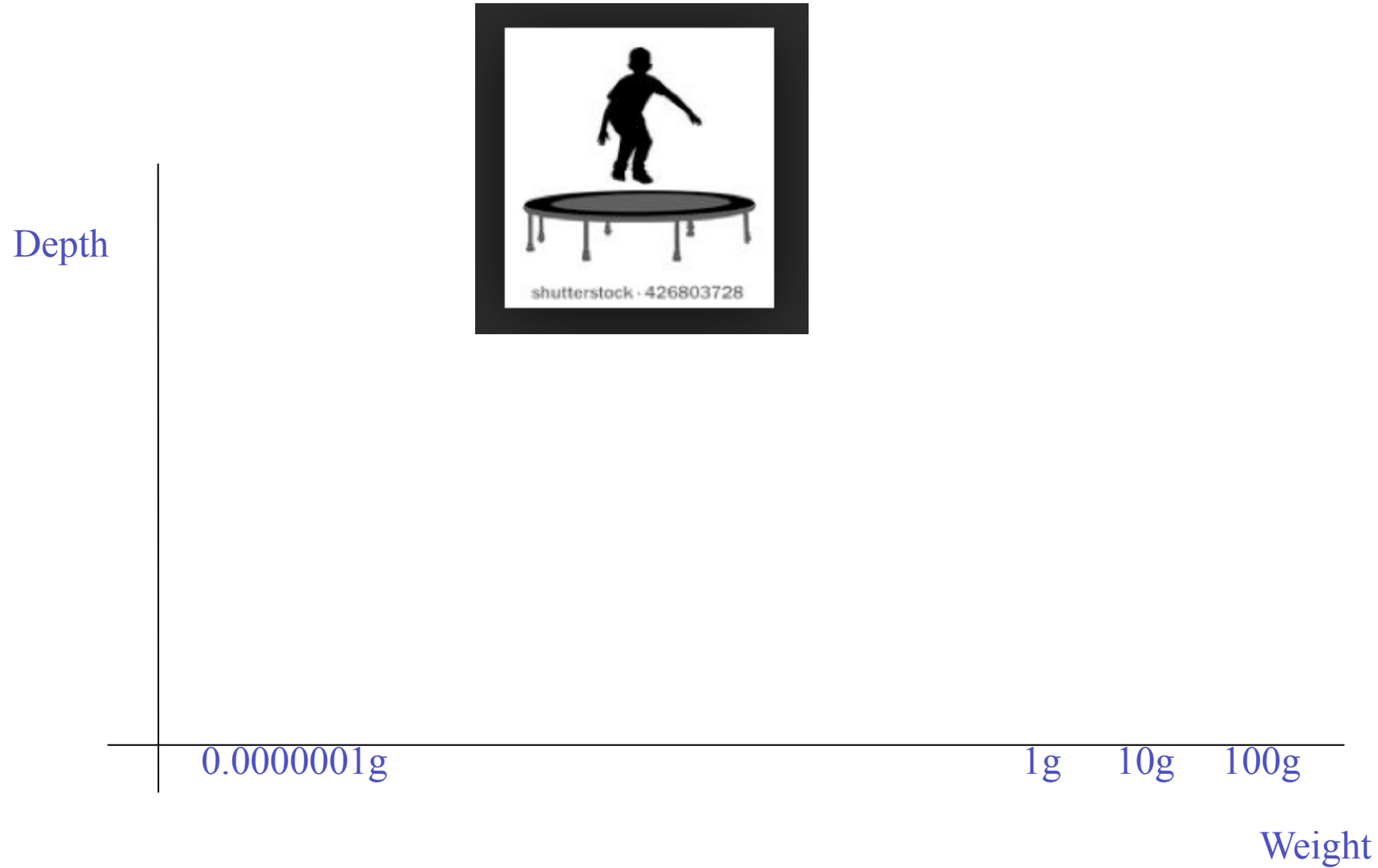
by Indranil Banik  
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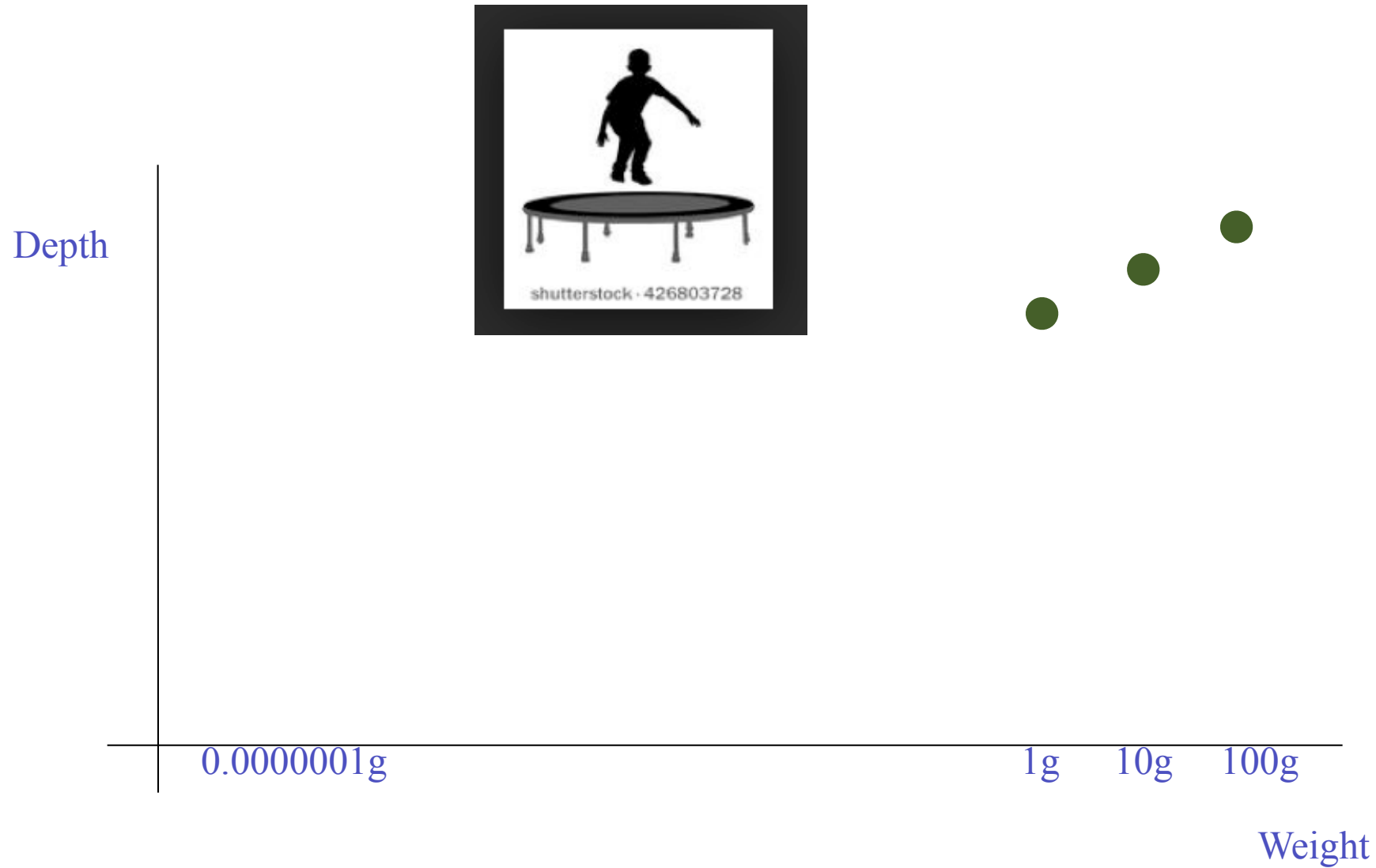
Depth of a trampoline with increasing weight :



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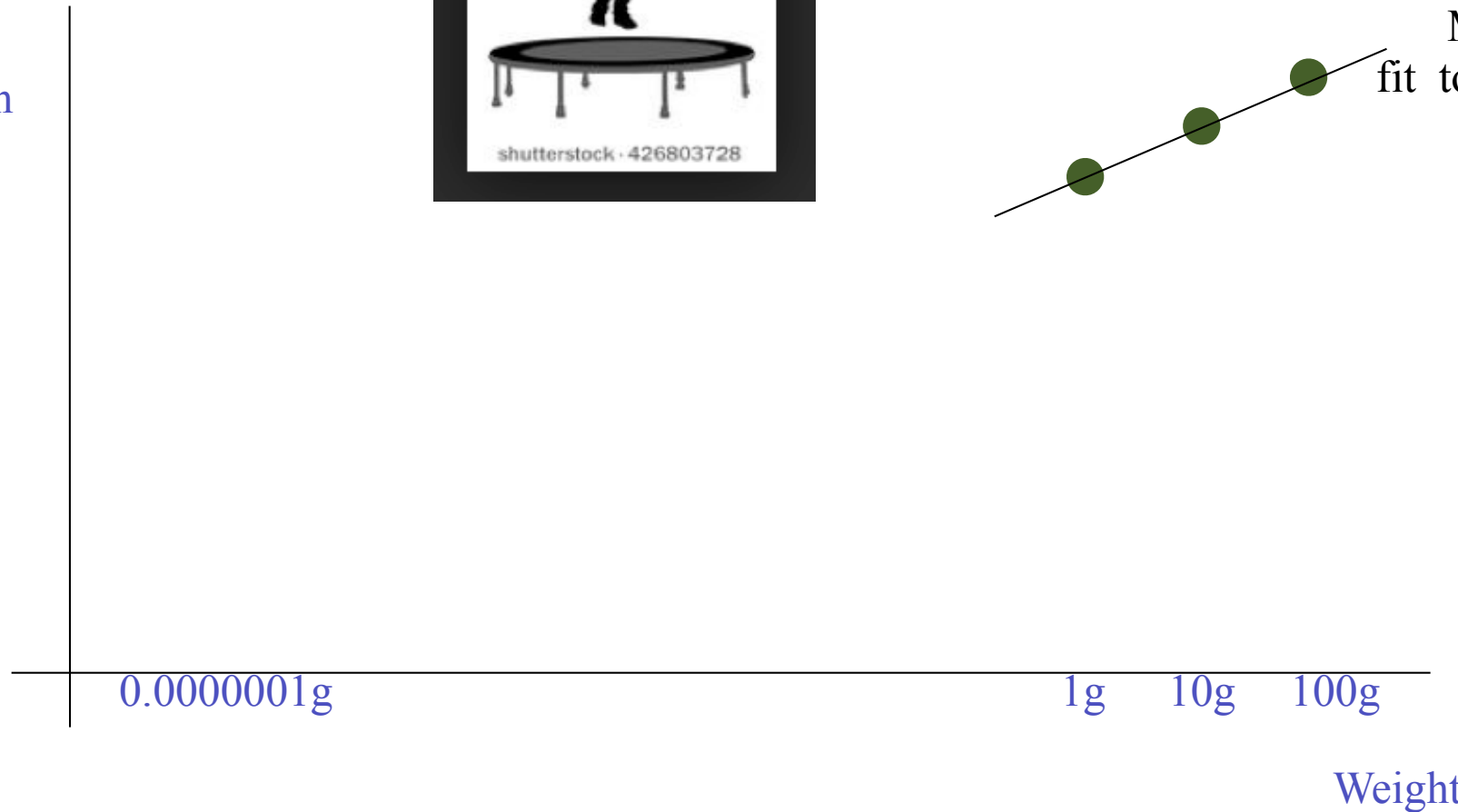
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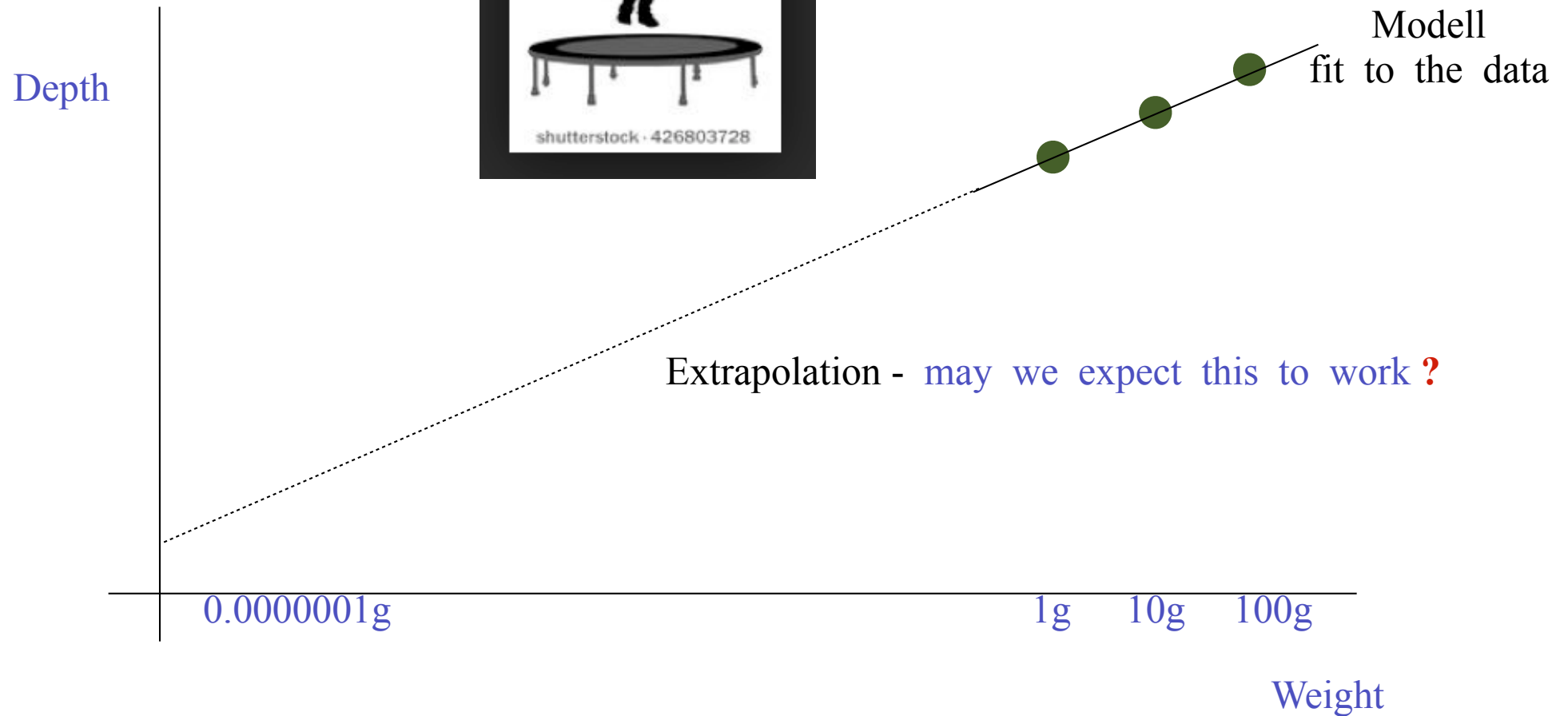
Depth



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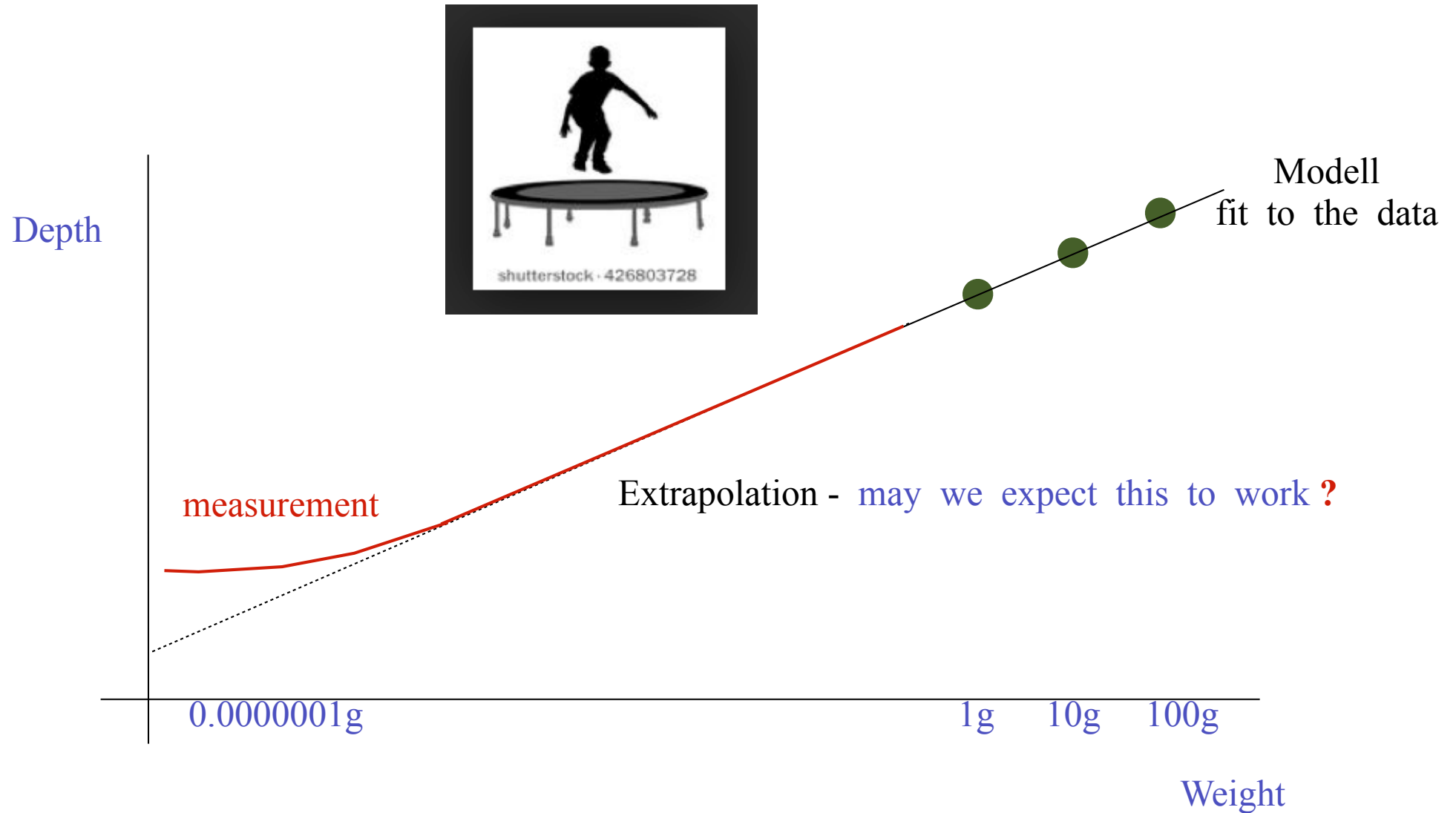
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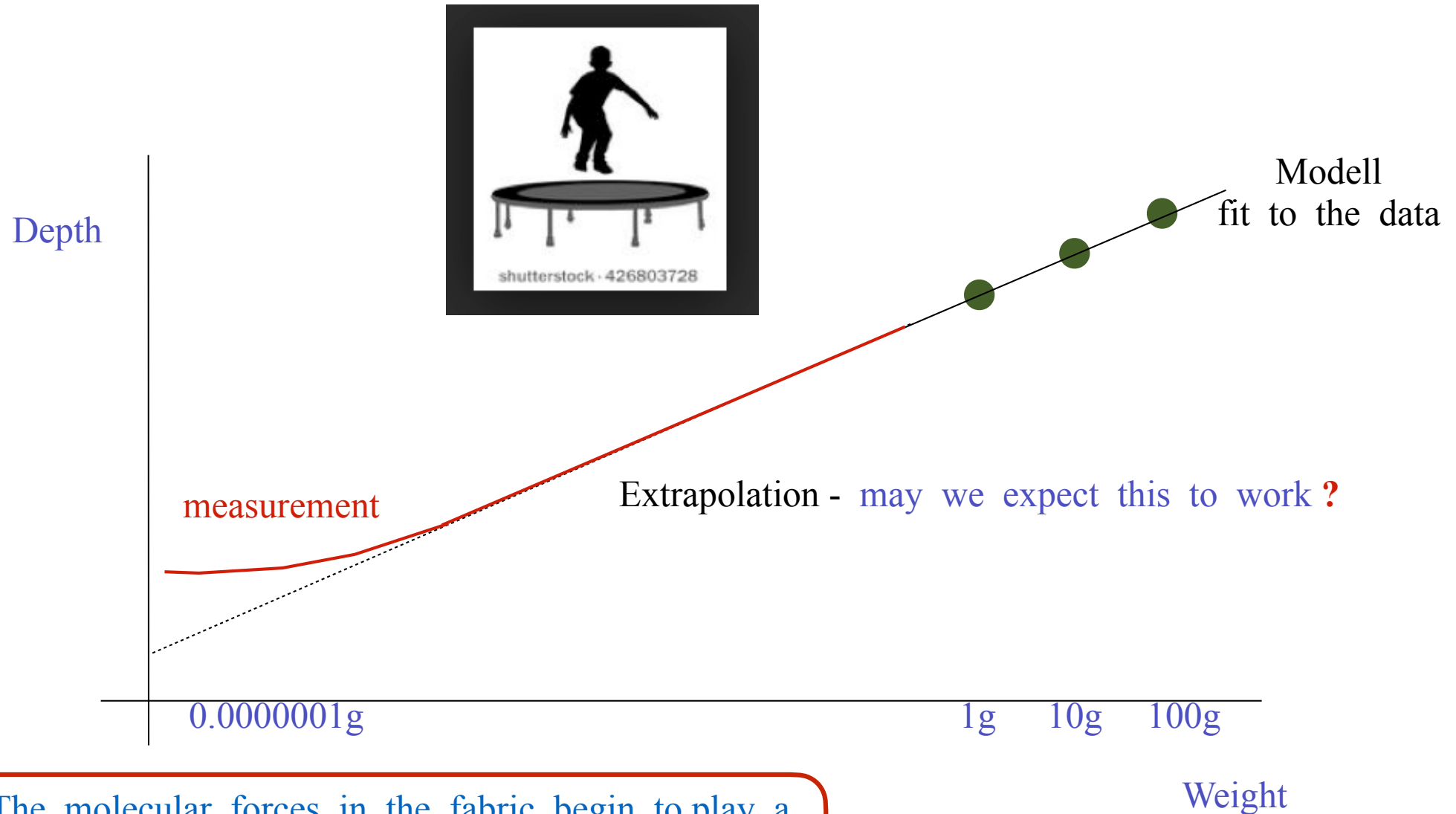
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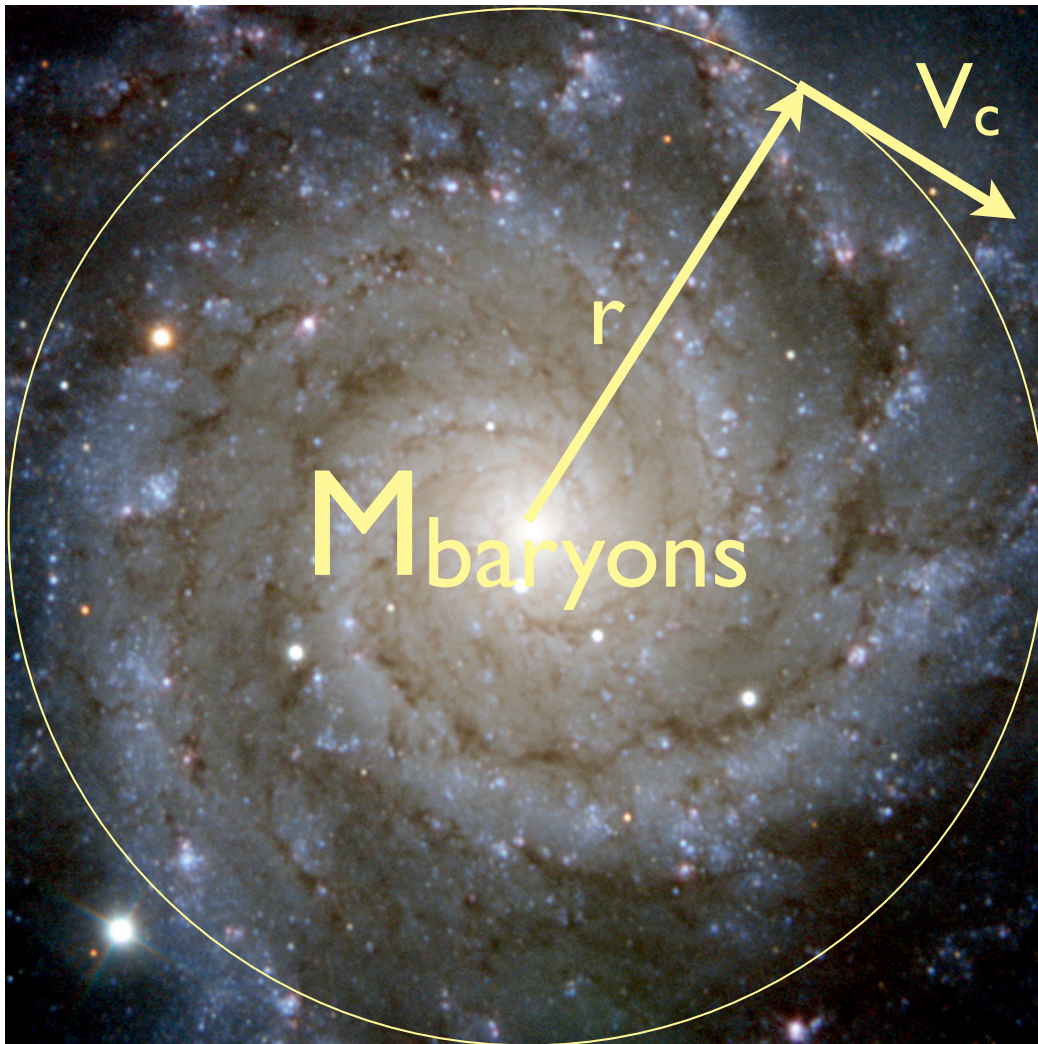
The molecular forces in the fabric begin to play a role and the system shifts from bulk properties to molecular-based behaviour.

## Disc galaxies



Balance between  
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According to Newton :

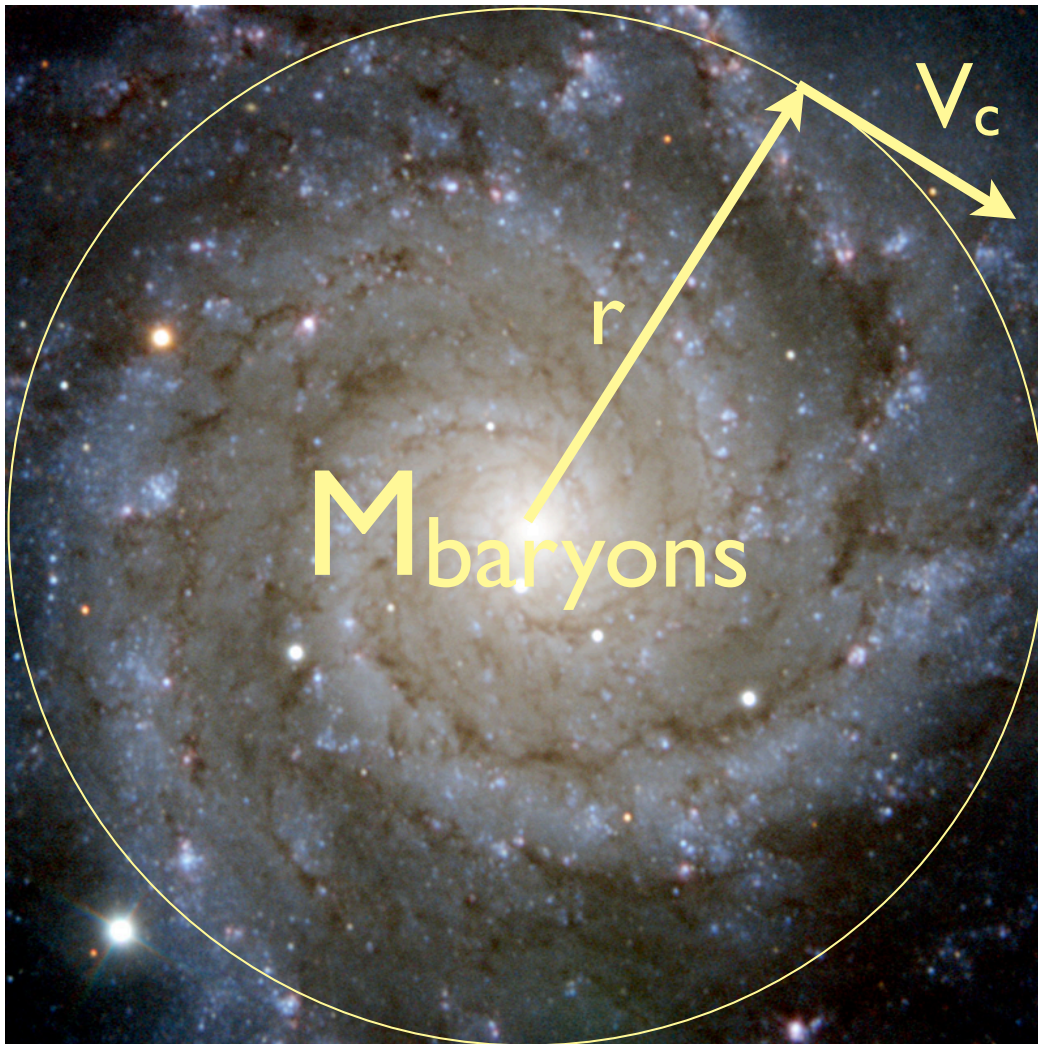
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Measured :

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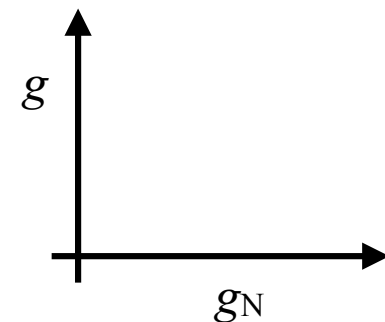
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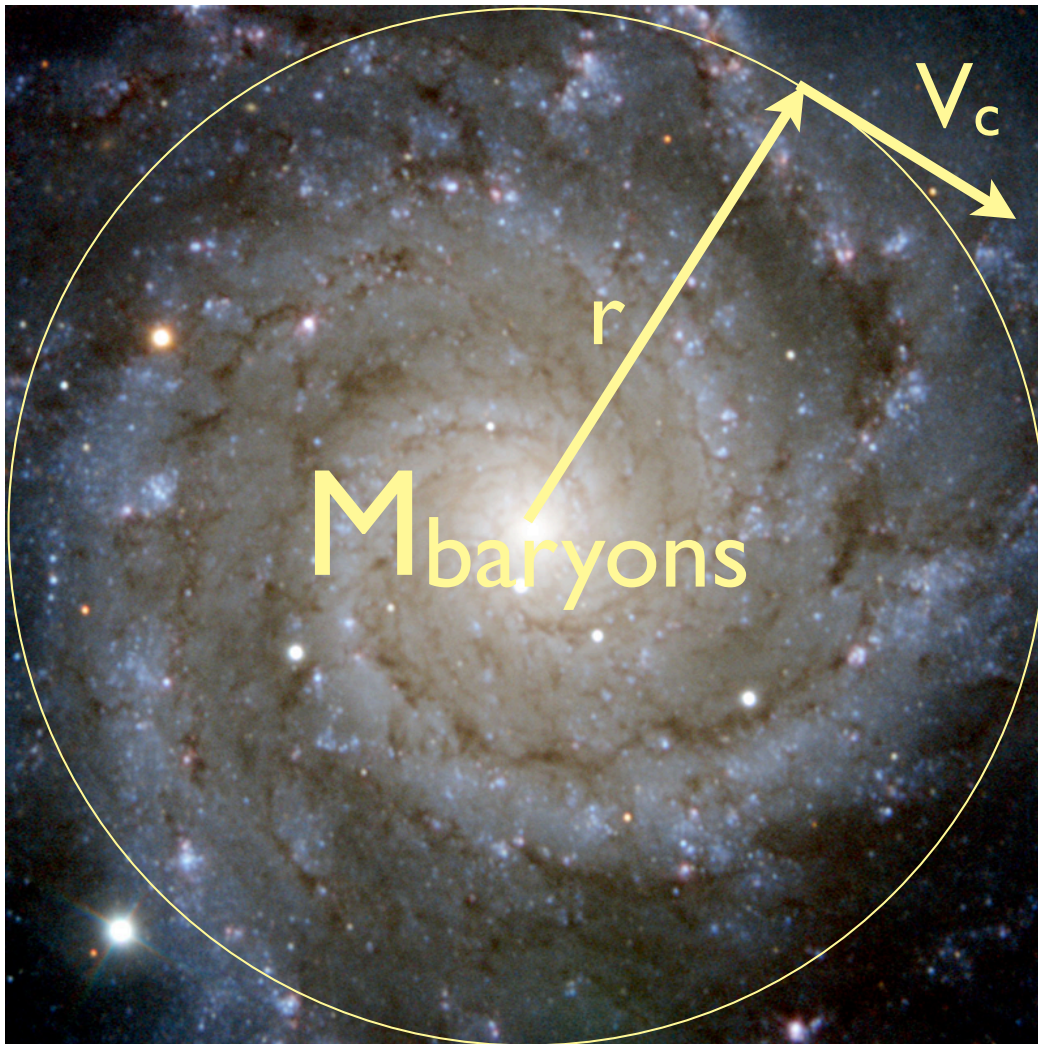
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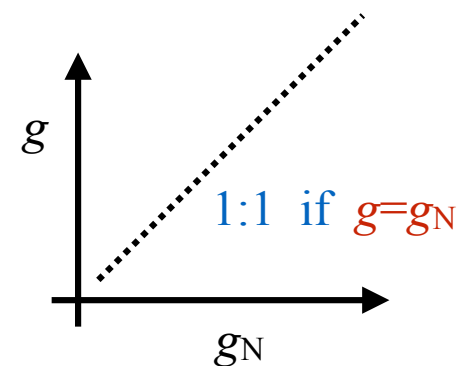
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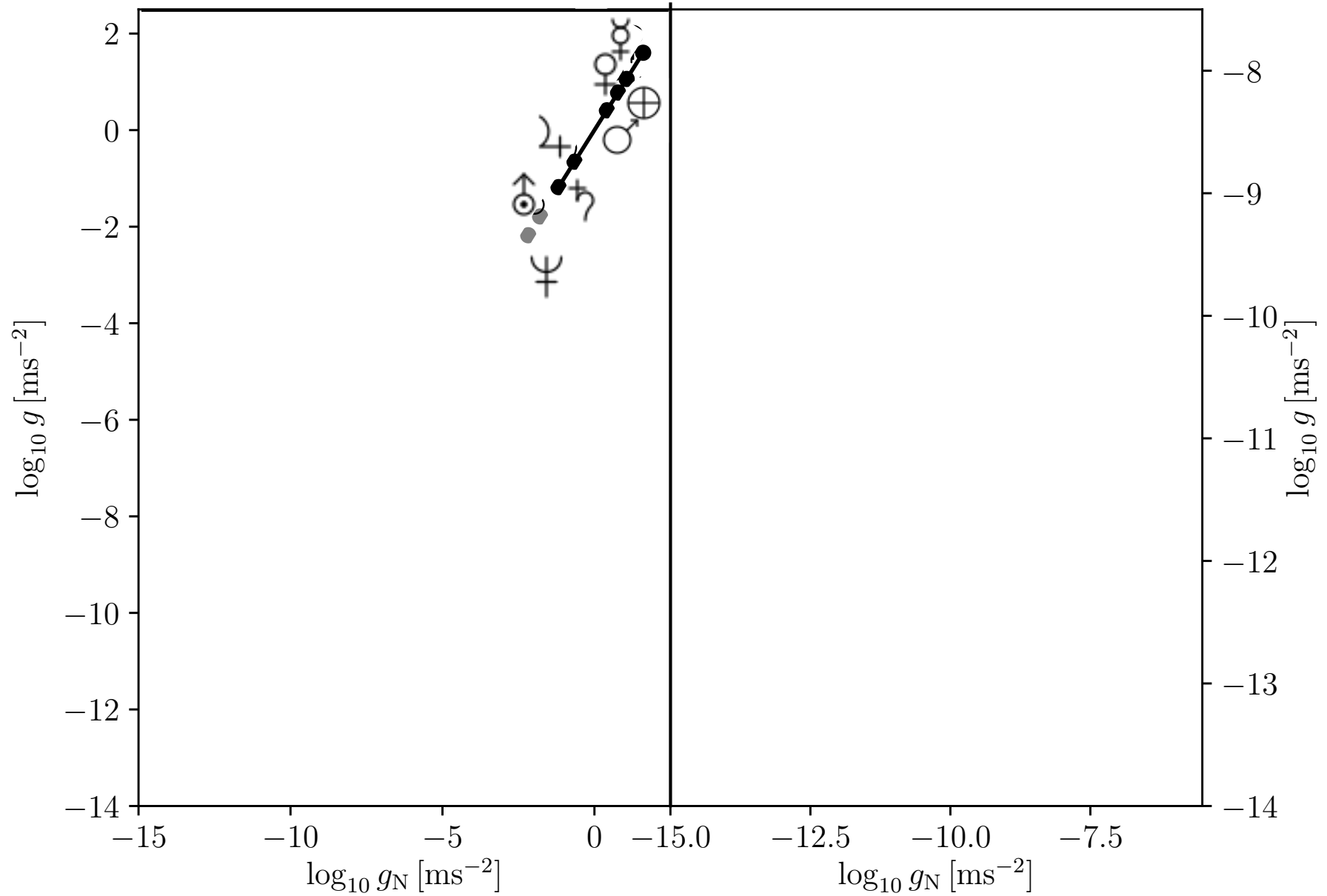
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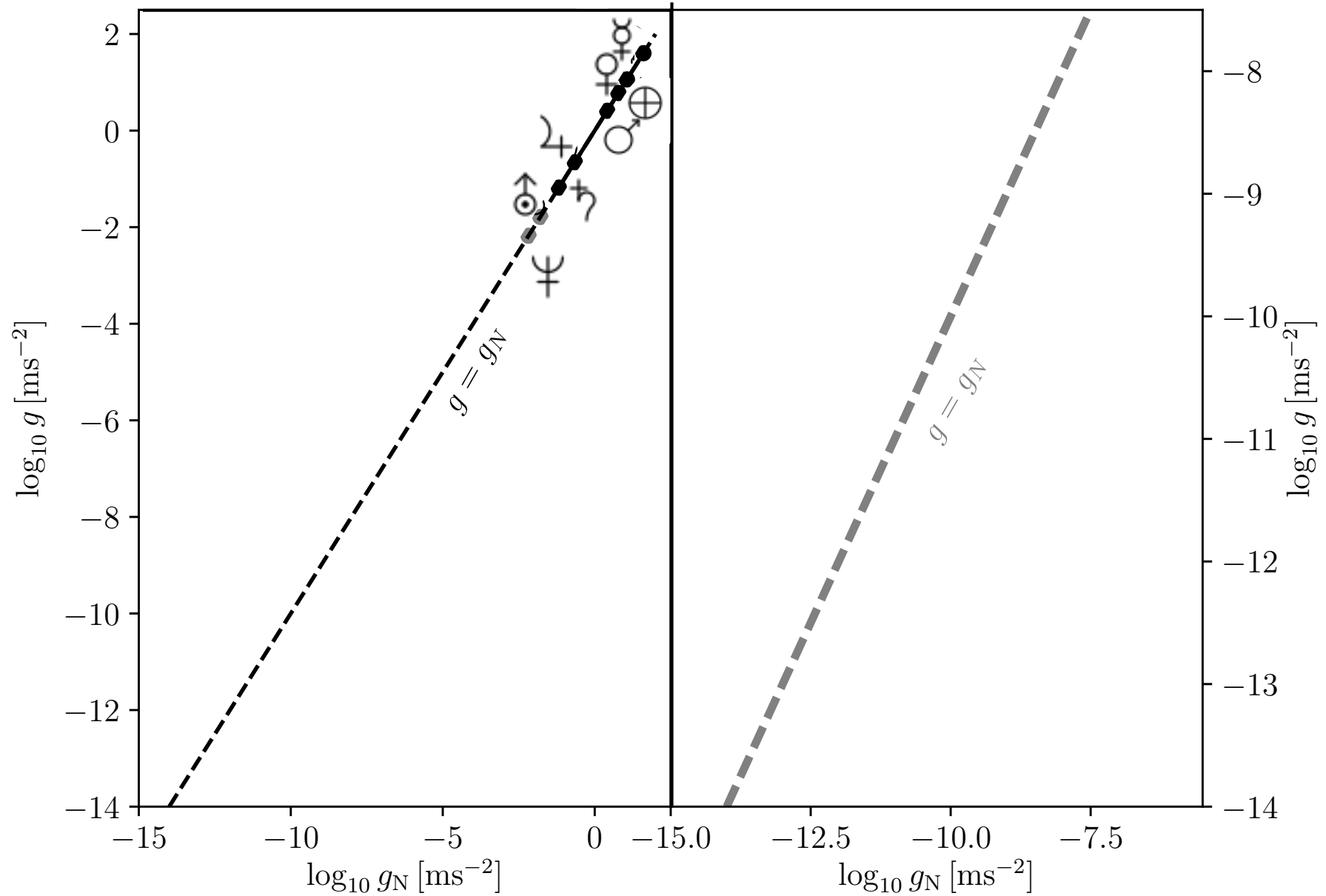
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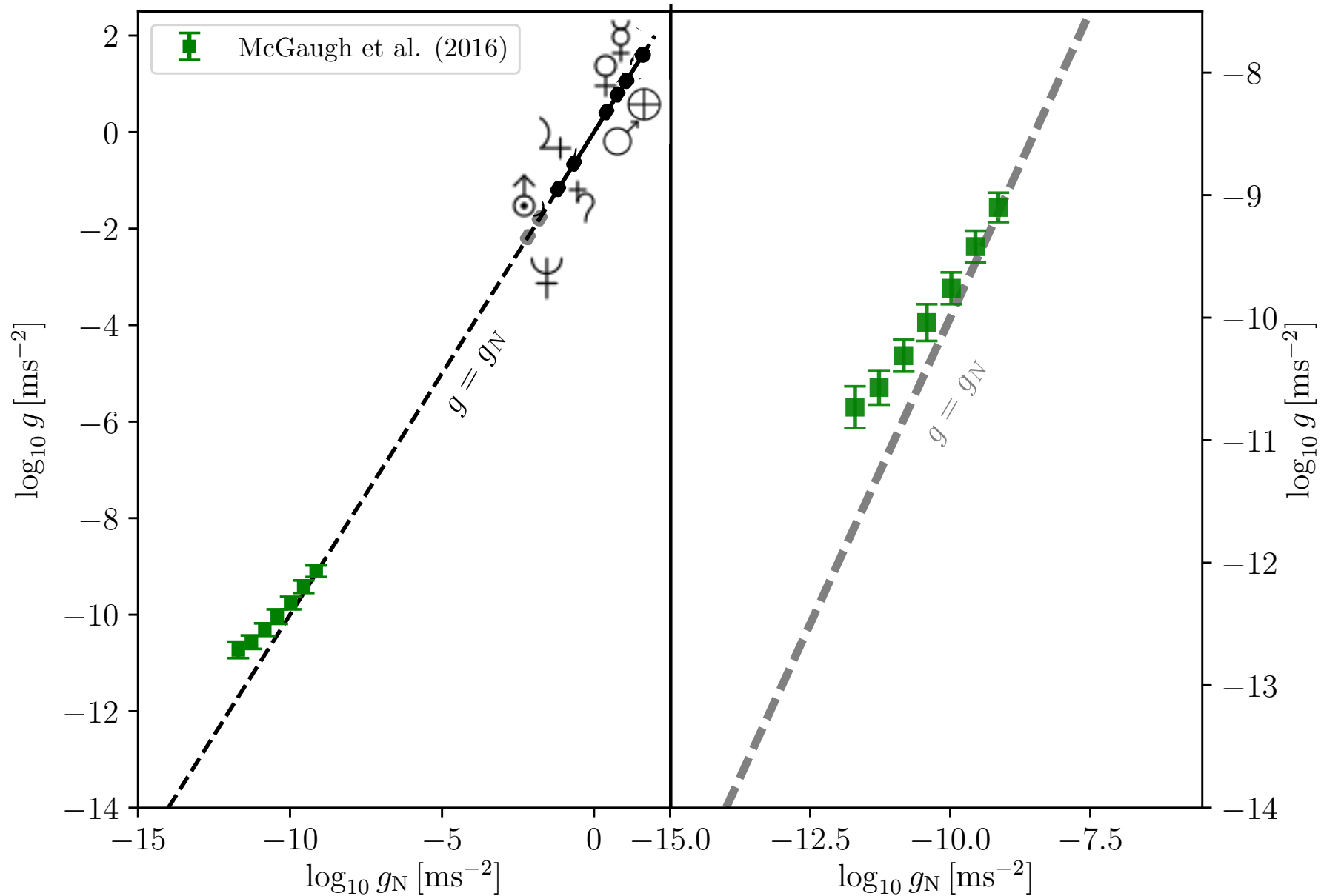
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D2016 =  
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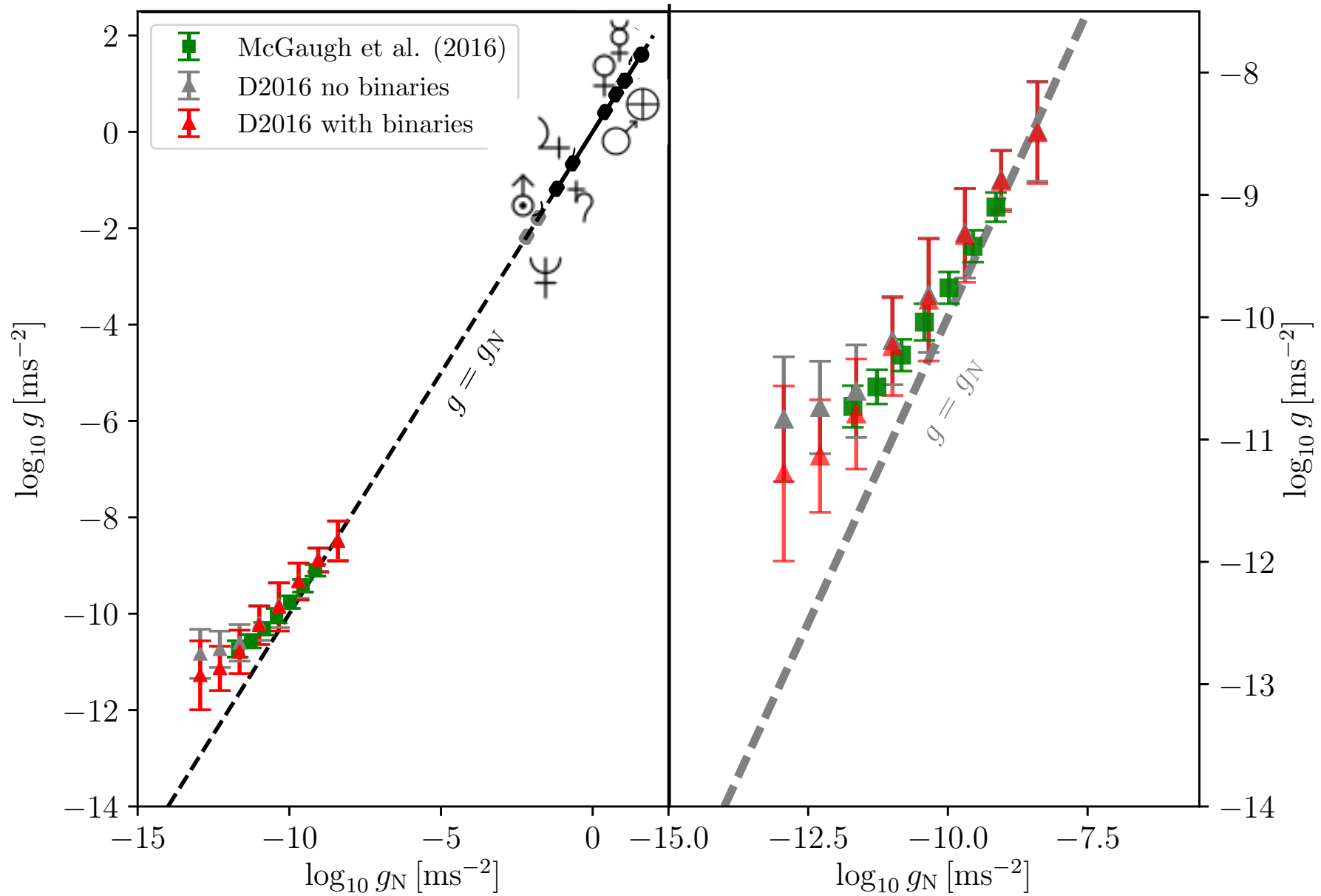
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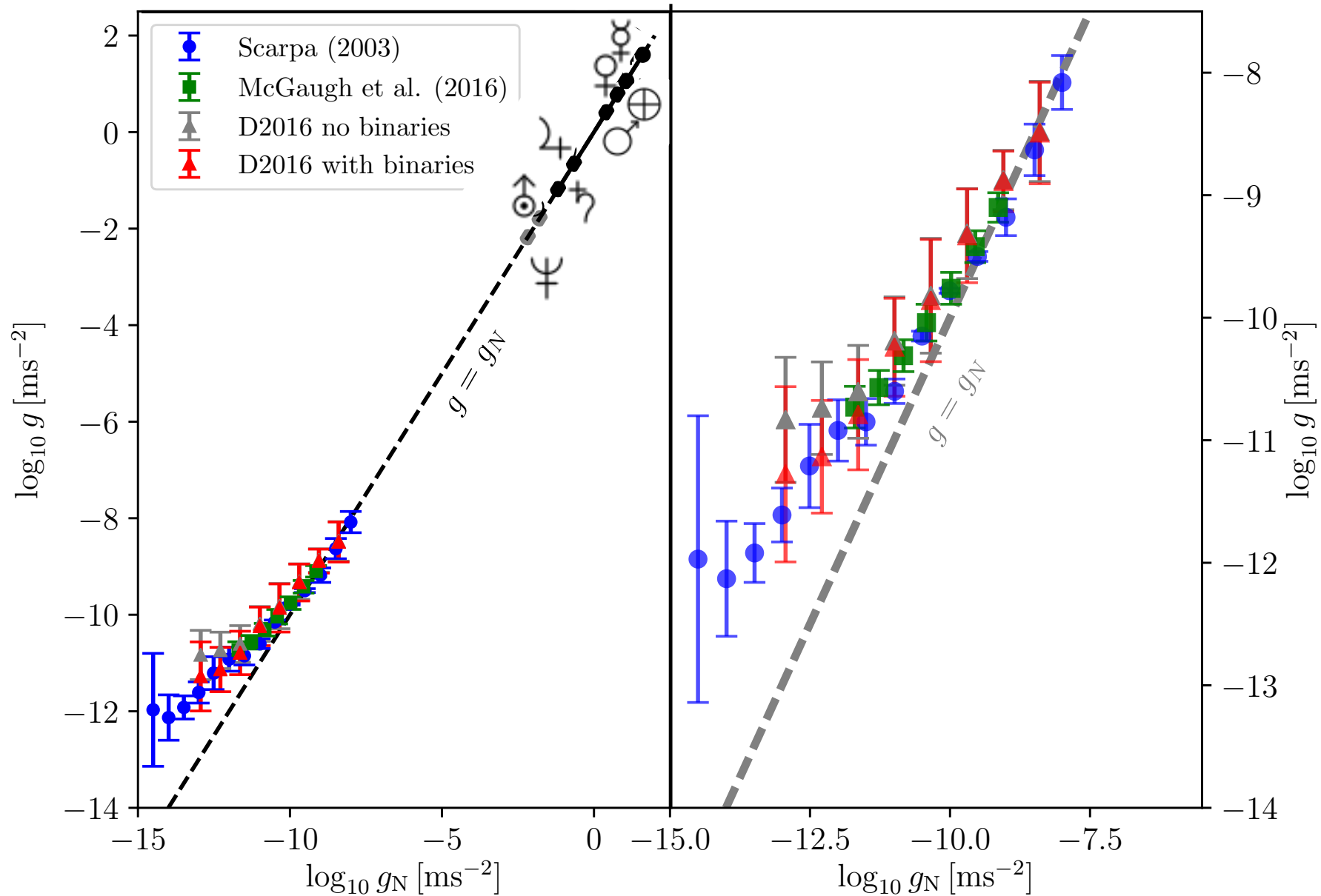
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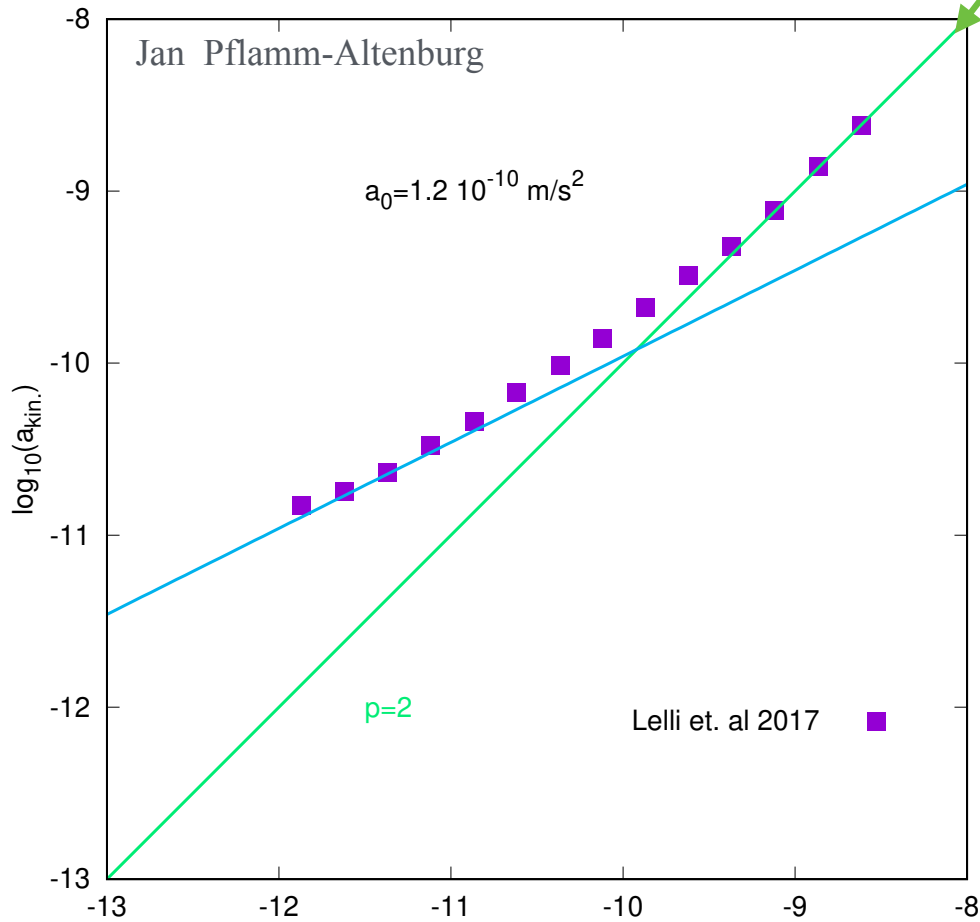
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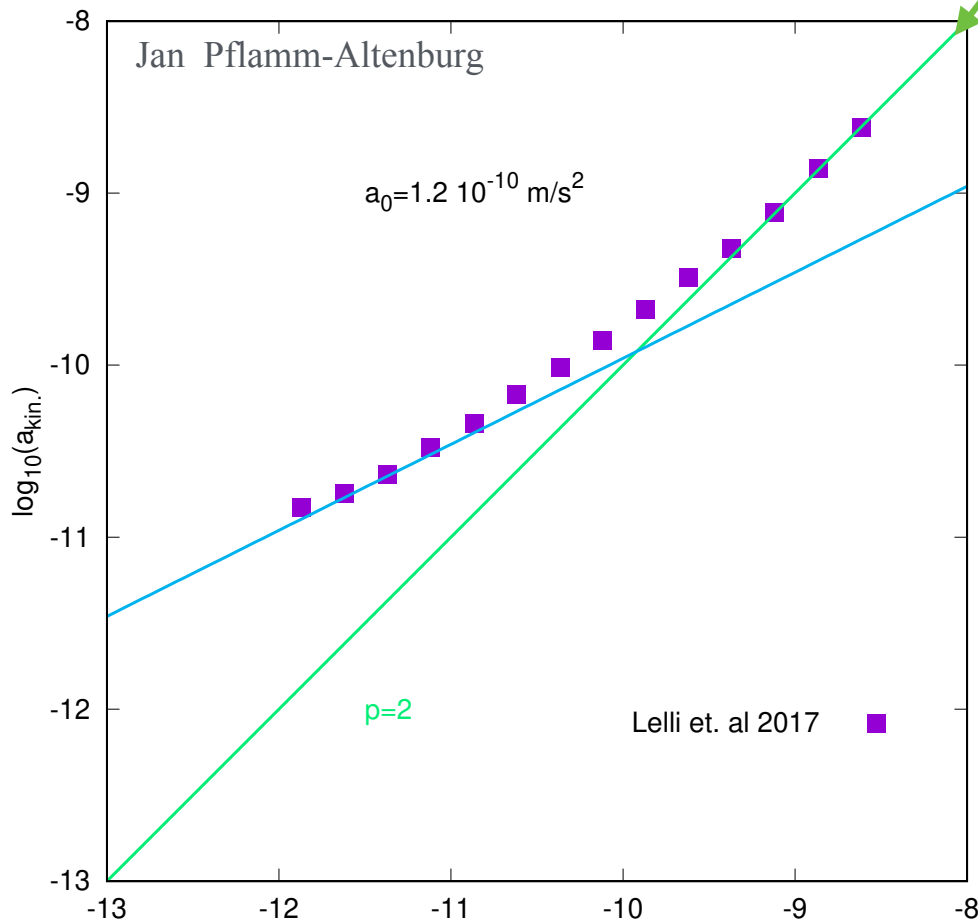
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→ Newtonian gravitation

$p=3$  non-standard Poisson equation

→ which gravitational dynamics ?



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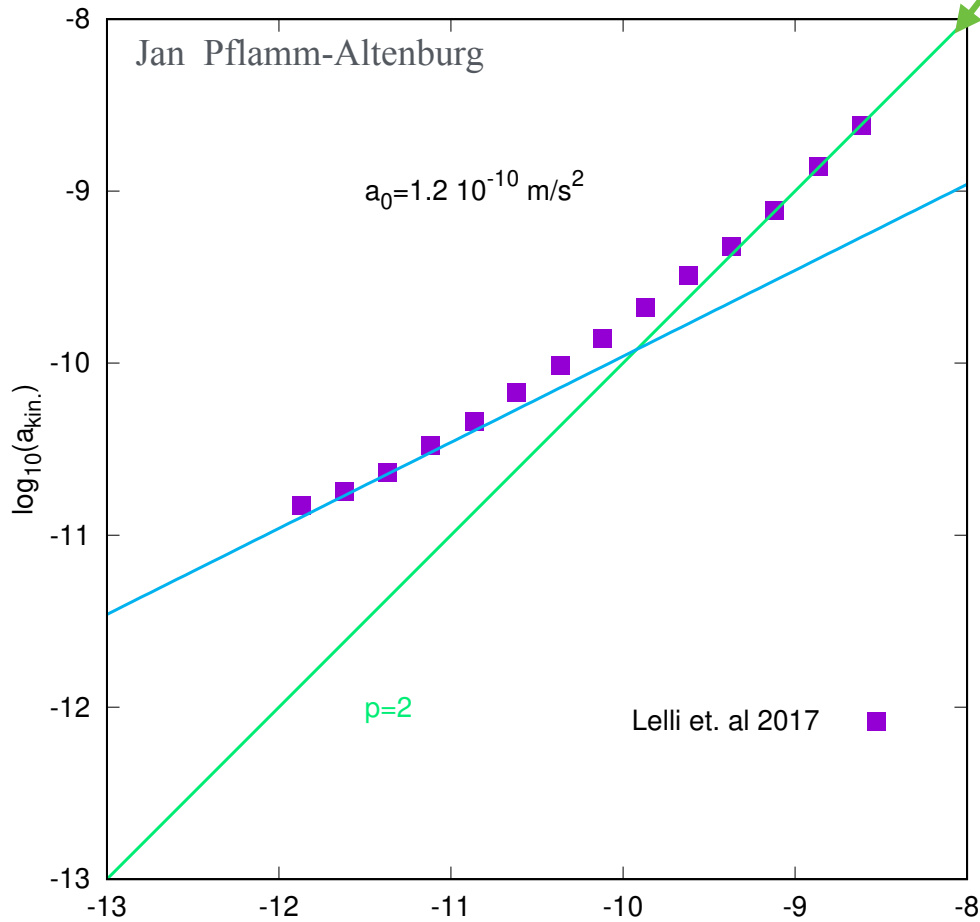
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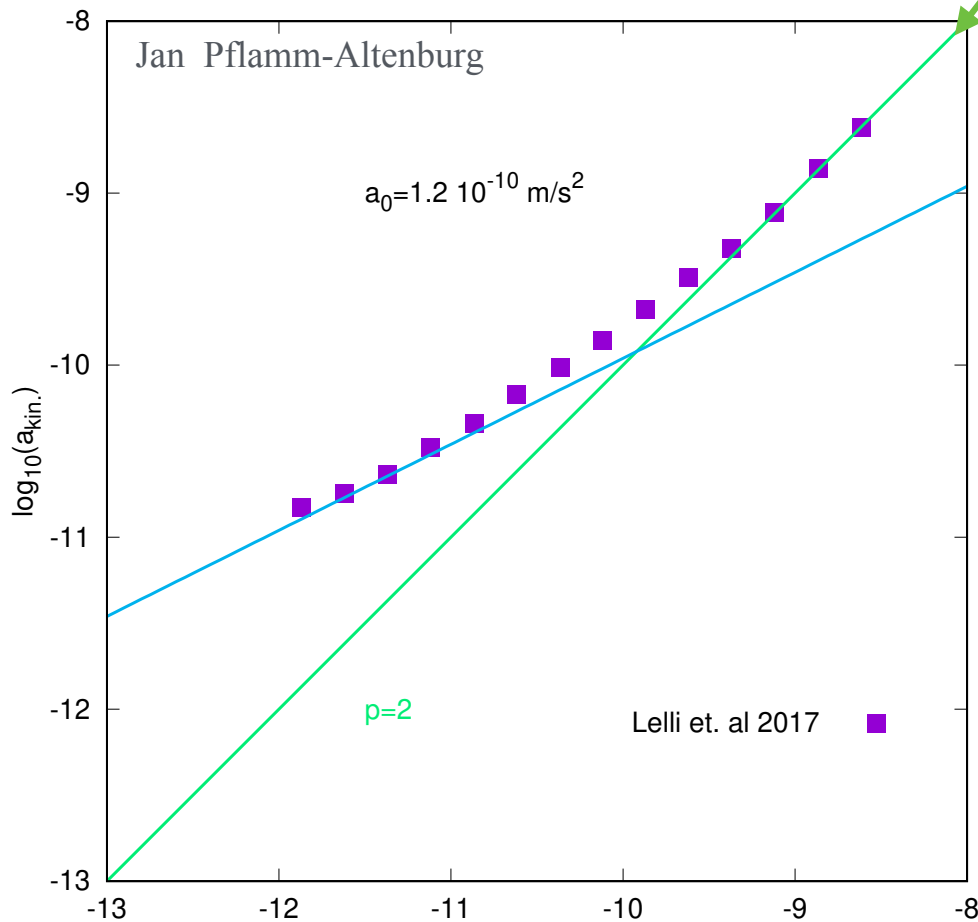
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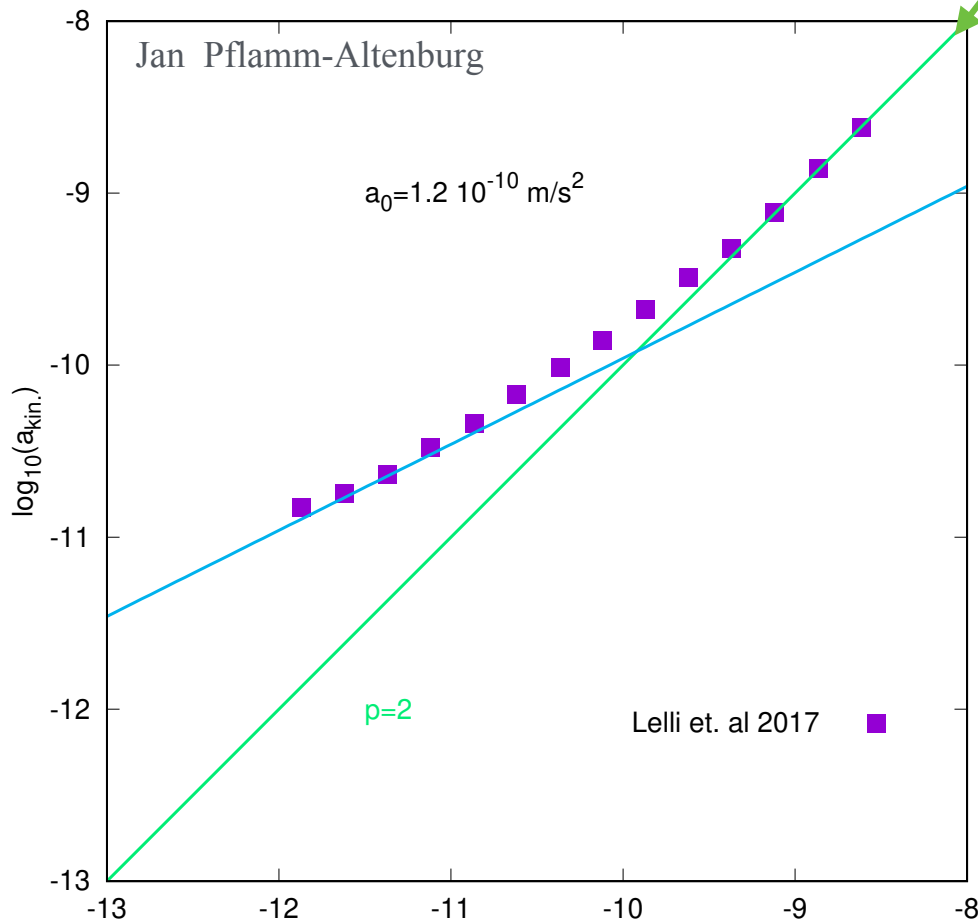
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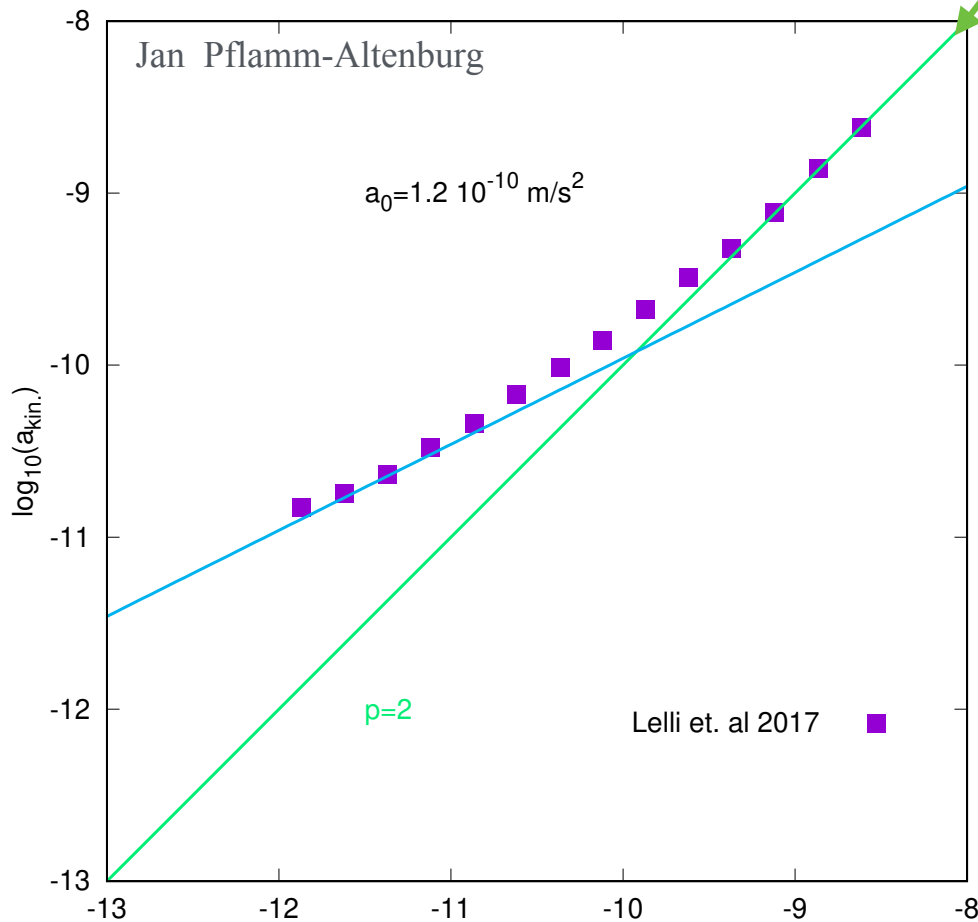
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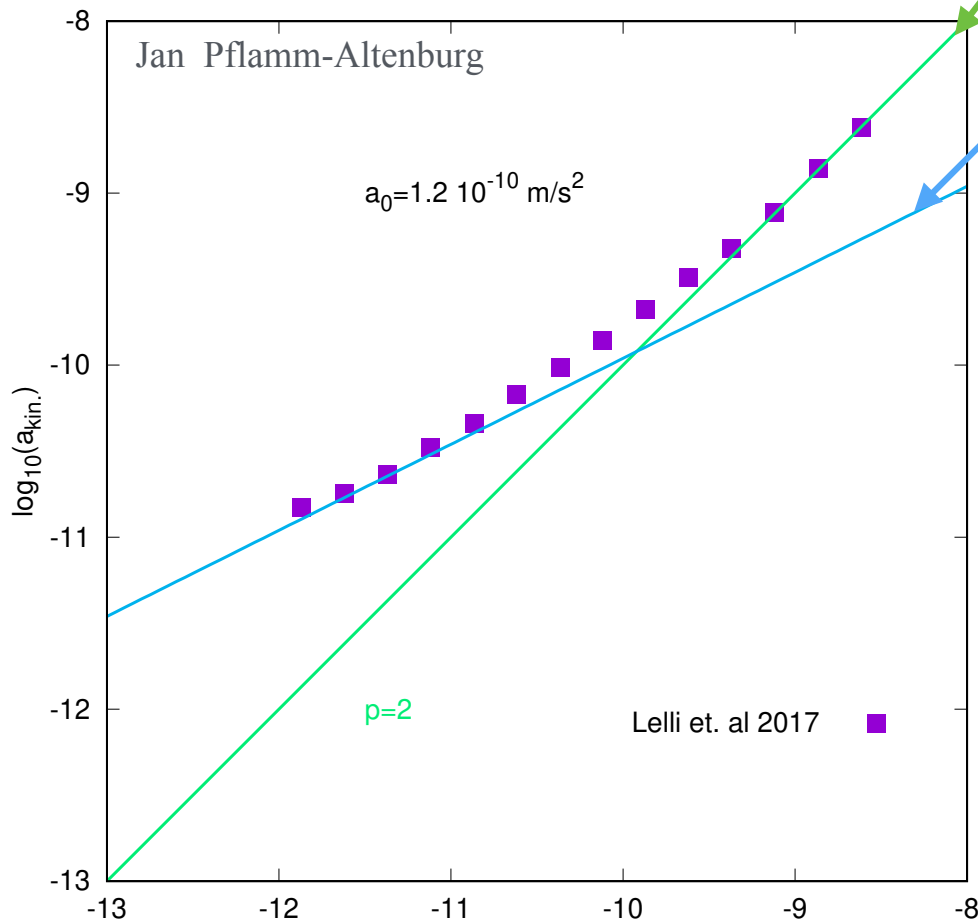
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$p=2$  standard Poisson equation above  
Newtonian gravitation

$p=3$  non-standard Poisson equation  
which gravitational dynamics ?

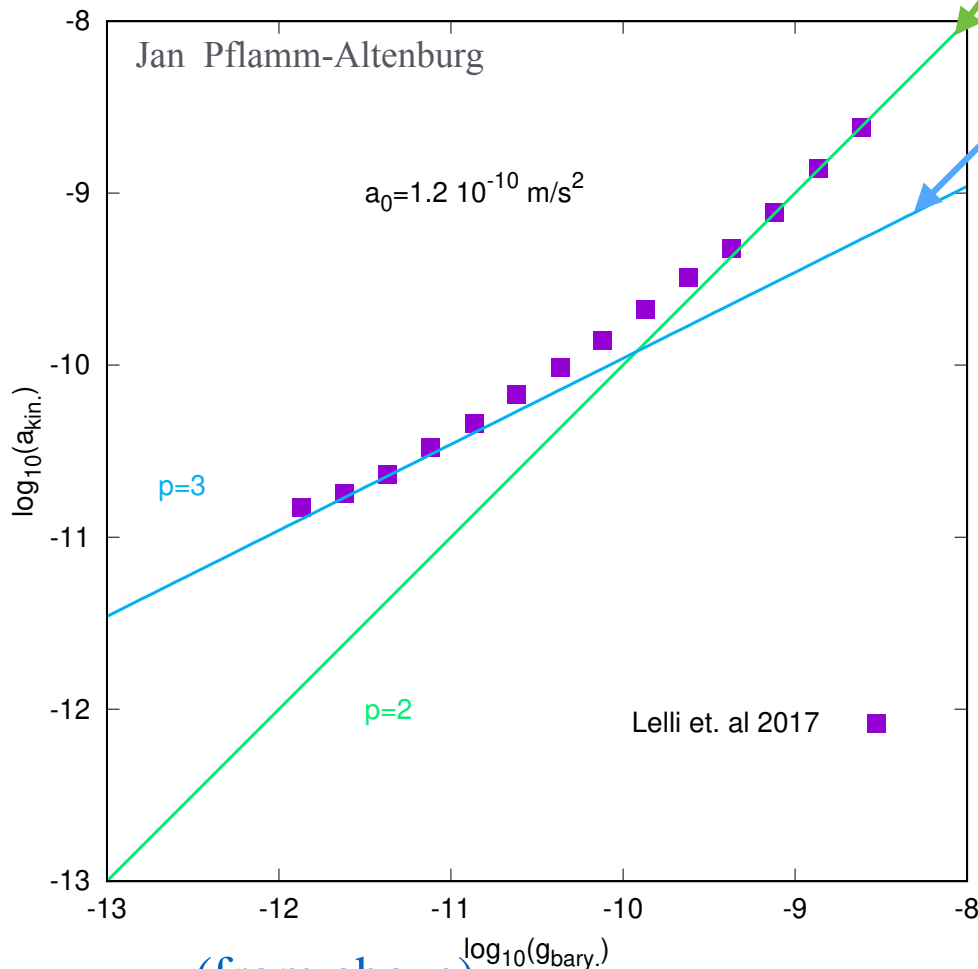
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Sufficiently far from  $\rho$  can assume spherical symmetry - integrate using divergence theorem

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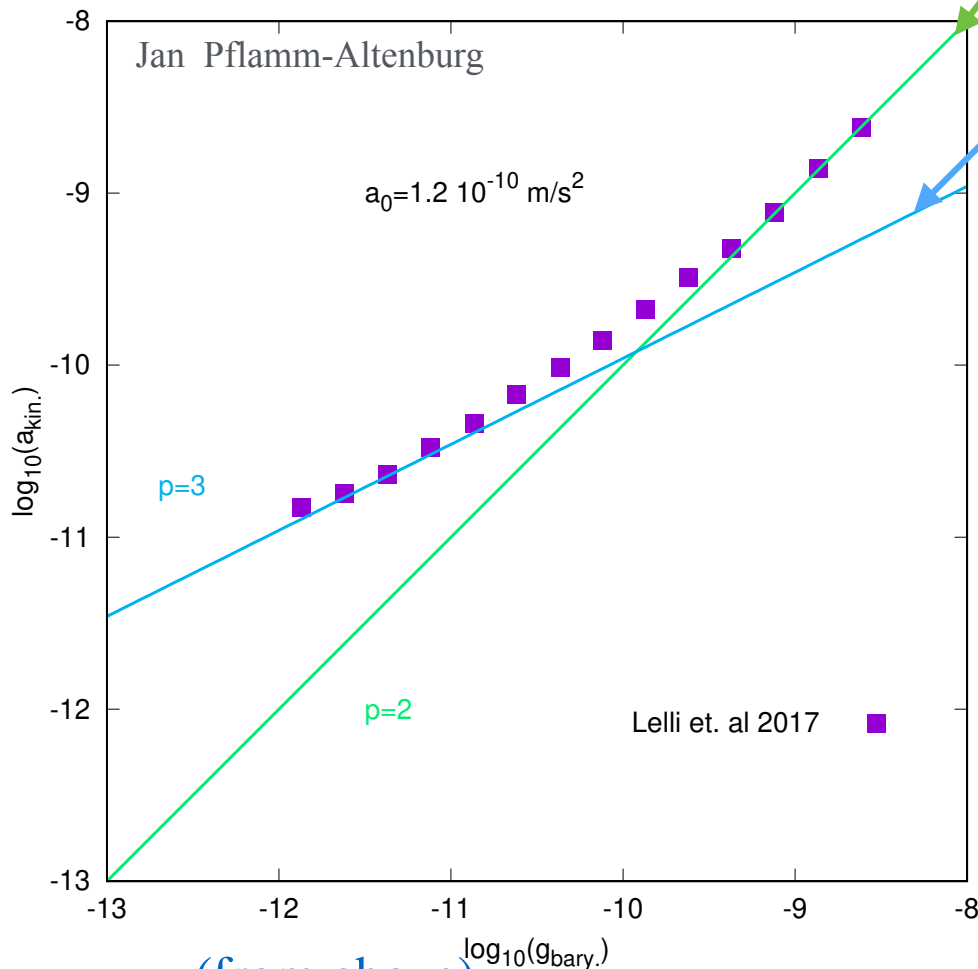
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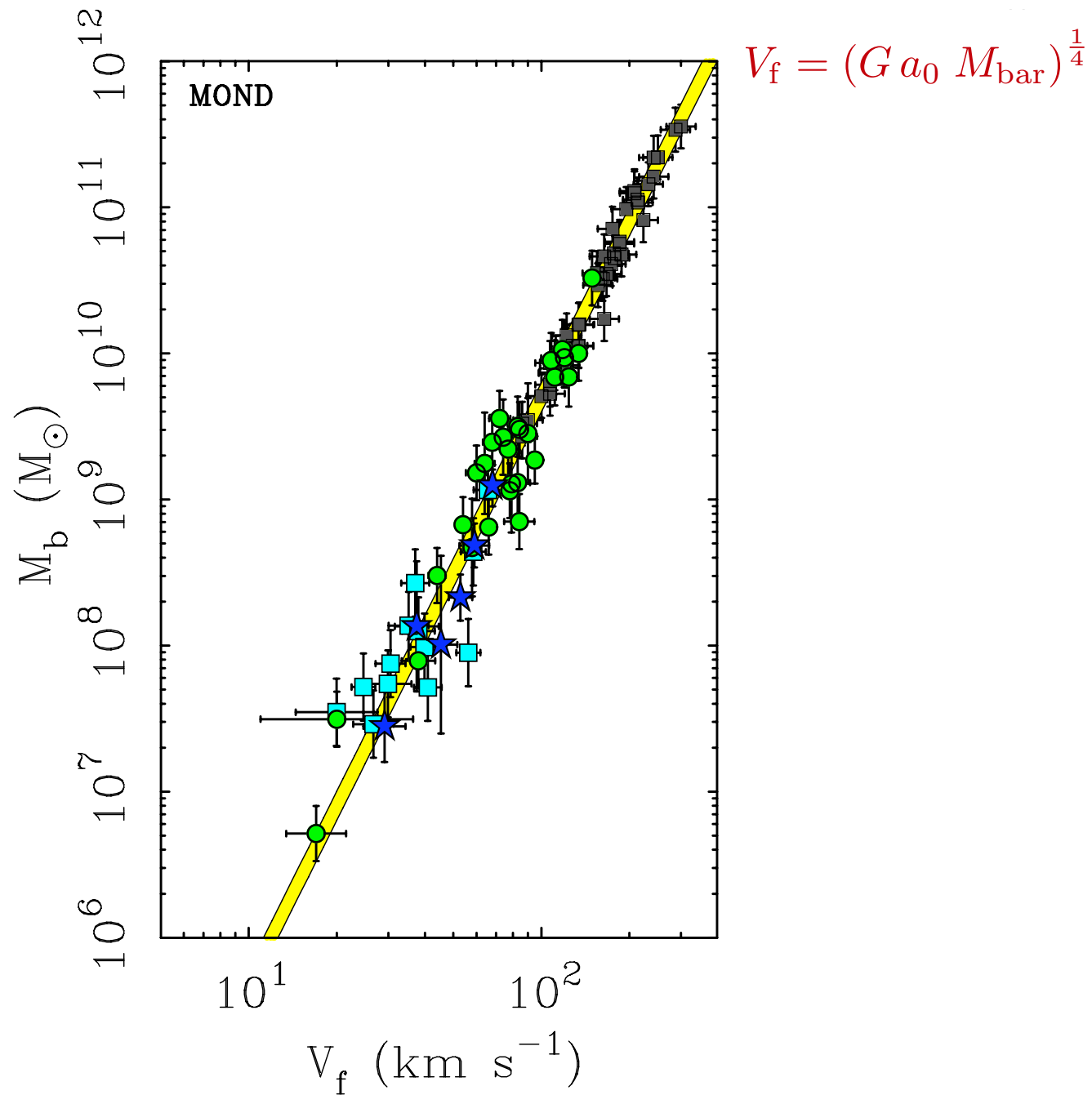
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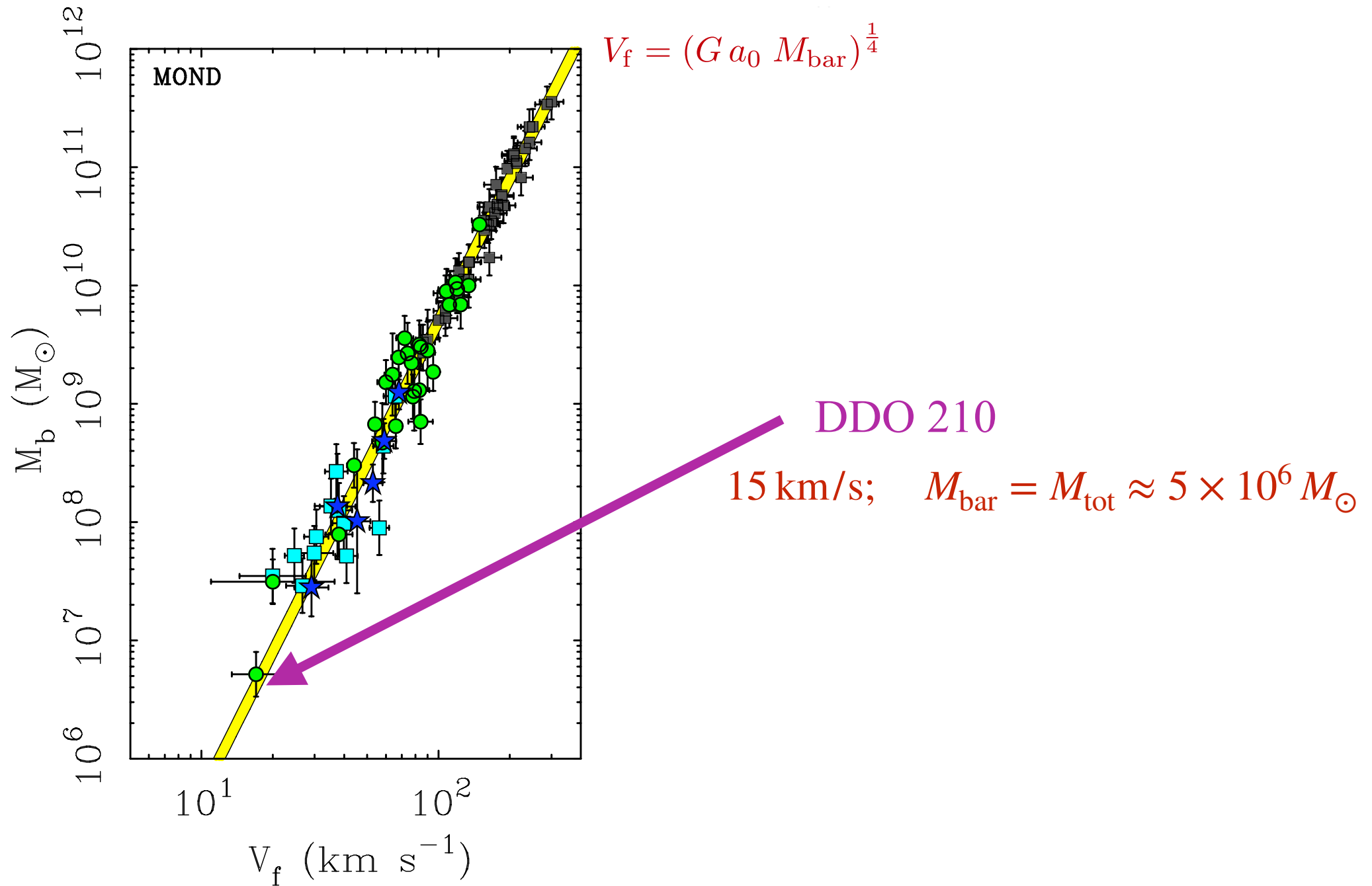
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Famaey & McGaugh 2012



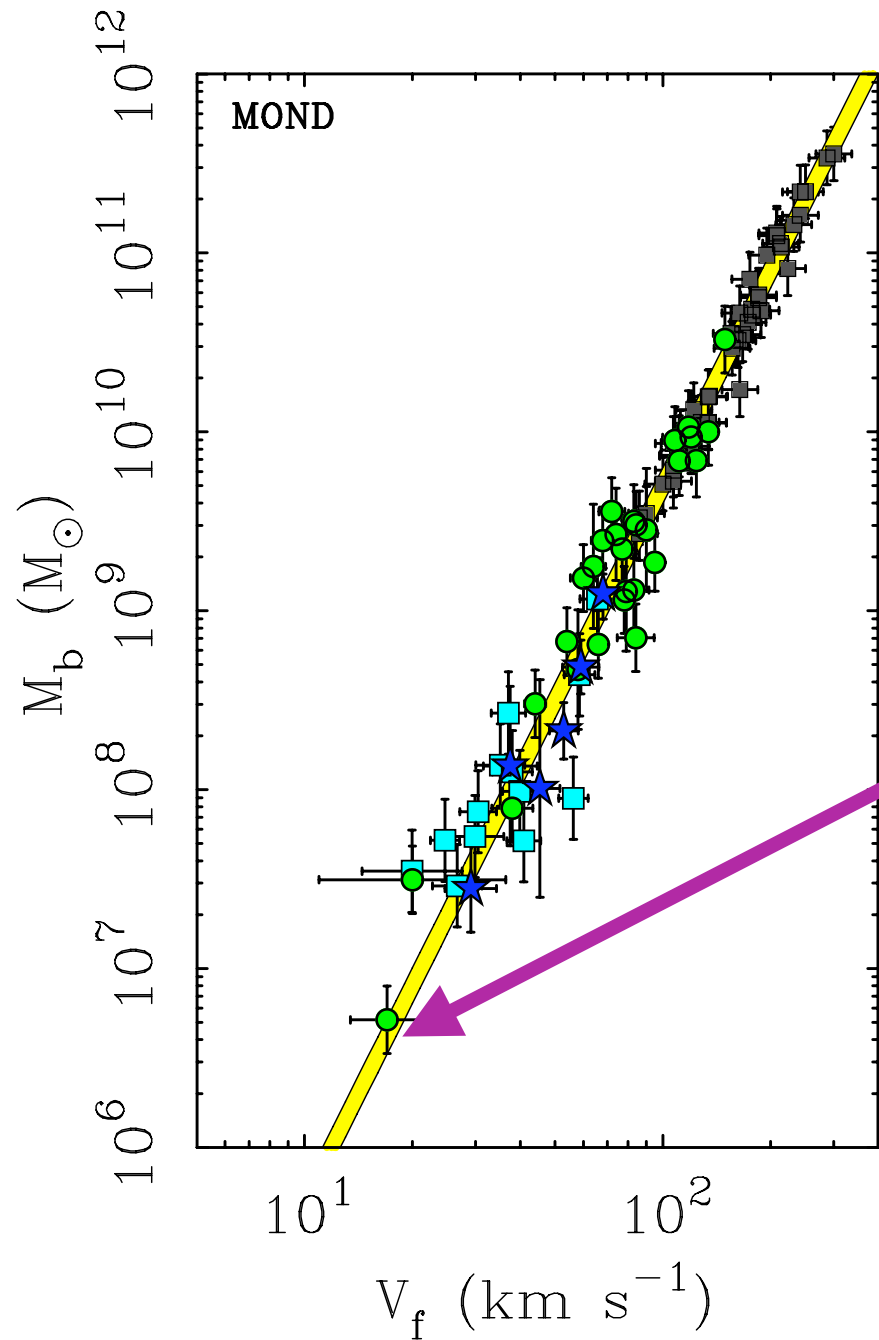
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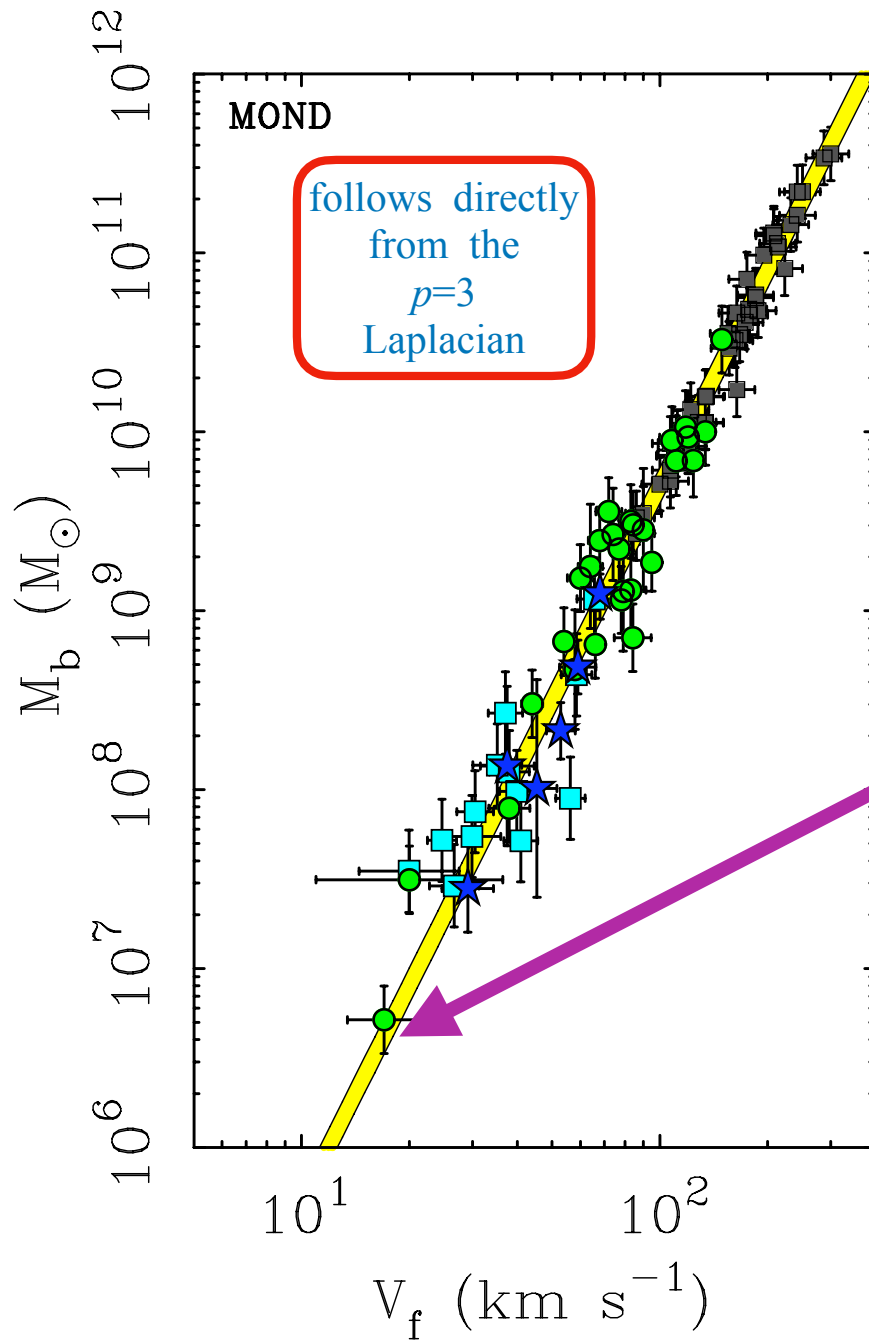
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**Relativistic formulation :** Skordis & Zlosnik (2021, 2020)

**Reviews :** Sanders (2007, 2009a, 2009b, 2015)  
Scarpa (2006)  
Famaey & McGaugh (2012)  
Trippe (2014, ZNatA)  
Milgrom (2014, Scholarpedia)  
Banik & Zhao (2022, Symmetry)

(see Kroupa et al. arXiv2309.11552 for these)